Ballistic Asynchronous Reversible Computing in Superconducting Circuits

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with Rupert Lewis (Quantum Phenomena Dept.)

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Contributors to our Reversible Computing research program

- Full group of recent staff at Sandia:
  - Michael Frank (Cognitive & Emerging Computing)
  - Robert Brocato (RF MicroSystems) – now retired
  - David Henry (MESA Hetero-Integration)
  - Rupert Lewis (Quantum Phenomena)
    - Terence “Terry” Michael Bretz-Sullivan
  - Nancy Missert (Nanoscale Sciences) – now retired
    - Matt Wolak (now at Northrop-Grumman)
  - Brian Tierney (Rad Hard CMOS Technology)

- Thanks are also due to the following colleagues & external research collaborators:
  - Karpur Shukla (CMU → Flame U. → Brown U.)
    - Currently in Prof. Jimmy Xu’s Lab for Emerging Techs.
  - Hannah Earley (Cambridge U. → startup)
  - Erik DeBenedictis (Sandia → Zettaflops, LLC)
  - Joseph Friedman (UT Dallas)
  - Kevin Osborn (LPS/JQI)
    - Liuqi Yu, Ryan Clarke, Han Cai
  - Steve Kaplan
  - Rudro Biswas (Purdue)
    - Dewan Woods & Rishabh Khare
  - Tom Conte (Georgia Tech/CRNCH)
    - Anirudh Jain, Gibran Essa
  - David Guéry-Odelin (Toulouse U.)
  - FAMU-FSU College of Engineering:
    - Sastry Pamidi (ECE Chair) & Jerris Hooker (Instructor)
    - 2019-20 students:
      - Frank Allen, Oscar L. Corces, James Hardy, Fadi Matloob
    - 2020-21 students:
      - Marshal Nachreiner, Samuel Perlman, Donovan Sharp, Jesus Sosa
Ballistic Asynchronous Reversible Computing in Superconducting Circuits

**Background: Why Reversible Computing?**
- Relevant classic results in the thermodynamics of computing
  - Recently generalized to quantum case
- Two major types of approaches to reversible computing in superconducting circuits:
  - *Adiabatic* approaches – Well-developed today.
    - Likharev’s parametric quantron (1977); more recent QFP tech (YNU & collabs.) w. substantial demo chips.
  - *Ballistic* approaches – Much less mature to date.
    - Fredkin & Toffoli’s early concepts (1978–’81); much more recent work at U. Maryland, Sandia, UC Davis

**Review:** The relatively new *asynchronous* ballistic approach to RC in SCE.
- Addresses concerns w instability of the synchronous ballistic approach
- Potential advantages of asynchronous ballistic RC (vs. adiabatic approaches)
- Implementation w. superconducting circuits (BARCS effort).

**Focus of this Talk:**
- Presenting our recent work on enumerating/classifying possible BARCS functions w. ≤3 ports and ≤2 states.
Can we envision reversible computing as a deterministic elastic interaction process?

Historical origin of this concept:
- Fredkin & Toffoli’s *Billiard Ball Model of computation* (“Conservative Logic,” IJTP 1982).
- Based on elastic collisions between moving objects.
- Spawned a subfield of “collision-based computing.”
  - Using localized pulses/solitons in various media.

No power-clock driving signals needed!
- Devices operate when data signals arrive.
- The operation energy is carried by the signal itself.
  - Most of the signal energy is preserved in outgoing signals.

However, all (or almost all) of the existing design concepts for ballistic computing invoke implicitly synchronized arrivals of ballistically-propagating signals…
- Making this work in reality presents some serious difficulties, however:
  - Unrealistic in practice to assume precise alignment of signal arrival times.
  - Thermal fluctuations & quantum uncertainty, at minimum, are always present.
  - Any relative timing uncertainty leads to chaotic dynamics when signals interact.
    - Exponentially-increasing uncertainties in the dynamical trajectory.
    - Deliberate resynchronization of signals whose timing relationship is uncertain incurs an inevitable energy cost.

Can we come up with a new ballistic model that avoids these problems?
Ballistic Asynchronous Reversible Computing (BARC)

**Problem:** Conservative (dissipationless) dynamical systems generally tend to exhibit chaotic behavior…
- This results from direct nonlinear interactions between multiple continuous dynamical degrees of freedom (DOFs), which amplify uncertainties, exponentially compounding them over time…
- E.g., positions/velocities of ballistically-propagating “balls”
- Or more generally, any localized, cohesive, momentum-bearing entity: Particles, pulses, quasiparticles, solitons…

**Core insight:** In principle, we can greatly reduce or eliminate this tendency towards dynamical chaos…
- We can do this simply by avoiding any direct interaction between continuous DOFs of different ballistically-propagating entities

Require localized pulses to arrive asynchronously—and furthermore, at clearly distinct, non-overlapping times
- Device’s dynamical trajectory then becomes independent of the precise (absolute and relative) pulse arrival times
- As a result, timing uncertainty per logic stage can now accumulate only linearly, not exponentially!
  - Only relatively occasional re-synchronization will be needed
- For devices to still be capable of doing logic, they must now maintain an internal discrete (digitally-precise) state variable—a stable (or at least metastable) stationary state, e.g., a ground state of a well

No power-clock signals, unlike in adiabatic designs!
- Devices simply operate whenever data pulses arrive
- The operation energy is carried by the pulse itself
  - Most of the energy is preserved in outgoing pulses
  - Signal restoration can be carried out incrementally

**Goal of current effort at Sandia:** Demonstrate BARC principles in an implementation based on fluxon dynamics in SuperConducting Electronics (SCE)

(BARCS 🐶 effort)
Simplest Fluxon-Based (bipolarized) BARC Function

One of our early tasks: Characterize the simplest nontrivial BARC device functionalities, given a few simple design constraints applying to an SCE-based implementation, such as:

- (1) Bits encoded in fluxon polarity;
- (2) Bounded planar circuit conserving flux;
- (3) Physical symmetry.

Determined through theoretical hand-analysis that the simplest such function is the **1-Bit, 1-Port Reversible Memory Cell (RM):**

- Due to its simplicity, this was then the preferred target for our subsequent detailed circuit design efforts…

<table>
<thead>
<tr>
<th>Input Syndrome</th>
<th>Output Syndrome</th>
</tr>
</thead>
<tbody>
<tr>
<td>+1(+1)</td>
<td>(+1)+1</td>
</tr>
<tr>
<td>+1(−1)</td>
<td>(+1)−1</td>
</tr>
<tr>
<td>−1(+1)</td>
<td>(−1)+1</td>
</tr>
<tr>
<td>−1(−1)</td>
<td>(−1)−1</td>
</tr>
</tbody>
</table>

RM icon: — o

Simplest Fluxon-Based (bipolarized) BARC Function

Stationary SFQ

Moving fluxon

Ballistic interconnect (PTL or LJJ)

Some planar, unbiased, reactive SCE circuit w. a continuous superconducting boundary

- Only contains L's, M's, C's, and unshunted JJs
- Junctions should mostly be subcritical (avoids $R_N$)
- Conserves total flux, approximately nondissipative

Desired circuit behavior (NOTE: conserves flux, respects T symmetry & logical reversibility):

- If polarities are opposite, they are swapped (shown)
- If polarities are identical, input fluxon reflects back out with no change in polarity (not shown)
- *(Deterministic) elastic ‘scattering’* type interaction: Input fluxon kinetic energy is (nearly) preserved in output fluxon
RM—First working (in simulation) implementation!

Erik DeBenedictis: “Try just strapping a JJ across that loop.”
◦ This actually works!

“Entrance” JJ sized to = about 5 LJJ unit cells (~1/2 pulse width)
◦ I first tried it twice as large, & the fluxons annihilated instead…
◦ “If a 15 μA JJ rotates by 2π, maybe ½ that will rotate by 4π” 😊

Loop inductor sized so ±1 SFQ will fit in the loop (but not ±2)
◦ JJ is sitting a bit below critical with ±1

WRspice simulations with ±1 fluxon initially in the loop
◦ Uses ic parameter, & uic option to tran command
◦ Produces initial ringing due to overly-constricted initial flux
◦ Can damp w. small shunt G

Polarity mismatch → Exchange  Polarity match → Reflect (=Exchange)
Resettable version of RM cell—Designed & Fabricated!

Apply current pulse of appropriate sign to flush the stored flux (the pulse here flushes out positive flux)

- To flush either polarity → Do both (±) resets in succession

Fabrication at SeeQC with support from ACI
**barc tool** for enumerating/classifying BARCS device functions

Custom Python program with 16 modules.

Tool is now complete; will be open-sourced.

Layer-cake view of software architecture:
- Modules only import modules from lower-numbered layers.

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<table>
<thead>
<tr>
<th>Layer</th>
<th>Module Names &amp; Descriptions</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
<td><strong>barc</strong> (top-level program)</td>
</tr>
<tr>
<td>3</td>
<td><strong>deviceType</strong> – Classification of devices with given dimensions.</td>
</tr>
<tr>
<td>2</td>
<td><strong>deviceFunction</strong> – Device with a specific transition function. <strong>stateSet</strong> – Identifies a set of accessible device states.</td>
</tr>
<tr>
<td>1</td>
<td><strong>pulseAlphabet</strong> – Sets of pulse types. <strong>pulseType</strong> – Identifies a specific type of pulse. <strong>state</strong> – Identifies an internal state of a device. <strong>symmetryGroup</strong> – Equivalence class of device functions. <strong>transitionFunction</strong> – Bijective map, input → output syndromes.</td>
</tr>
<tr>
<td>0</td>
<td><strong>characterClass</strong> – Defines a type of signal characters. <strong>deviceDimensions</strong> – Defines size parameters of devices. <strong>dictPermuter</strong> – Used to enumerate transition functions. <strong>signalCharacter</strong> – Identifies I/O event type (pulse type &amp; port). <strong>symmetryTransform</strong> – Invertibly transforms a device function. <strong>syndrome</strong> – An initial or final condition for a device transition. <strong>utilities</strong> – Defines some low-level utility functions.</td>
</tr>
</tbody>
</table>

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Symmetry group #38 has 6 functions:

Function #155.
Function #340.
Function #481.
Function #285.
Function #365.
Function #185.

Example: Function #155 = \(1\)!3(L,R):

1(L) → (R)2
1(R) → (L)3
2(L) → (R)1
2(R) → (L)3
3(L) → (L)2
3(R) → (L)1

Function #155 has the following symmetry properties:
- It is D-dual to function #481
- It is S-dual to function #481
- It is E(1,2)-dual to function #340
- It is E(1,3)-dual to function #185
- It is E(2,3)-dual to function #481
- It R(-1)-transforms to function #365
- It R(1)-transforms to function #285

Example description of a symmetry-equivalence group as output by the *barc* tool.
Symmetry Relations of Interest

The following symmetry relations on BARC functions are considered in this work:

- **Direction-reversal symmetry** $\mathcal{D}$ –
  Symmetry under exchange of input & output syndromes (involution of transition func.)

- **State-exchange symmetry** $\mathcal{S}$ –
  Symmetry under an exchange of state labels (and fluxes, for flux-polarized states).

- **Flux-negation symmetry** $\mathcal{F}$ –
  Symmetry under negation of all (I/O flux & internal state) flux polarities.

- **Moving-flux negation symmetry** $\mathcal{M}$ – Symmetry under negation of all moving (I/O) flux polarities.
  - **Input flux negation symmetry** $\mathcal{I}$ – Symmetry under negation of all input flux polarities.
  - **Output flux negation symmetry** $\mathcal{O}$ – Symmetry under negation of all output flux polarities.

- **Port-relabeling symmetries** $\mathcal{R}_p$ – Symmetry under a particular permutation $P$ of the port labels.
  - **Port exchange symmetry** $\mathcal{E}(p_i, p_j)$ – Symmetry wrt an exchange of labels between a particular pair of ports.
  - **Rotational symmetry** $\mathcal{R}_r$ – Relevant for $n \geq 3$ ports. Symmetry under (planar) rotation of port labels.
  - **Reflection across port axis** $\mathcal{R}_{\{p_i\}}$ – Symmetry under reflection of ports on either side of port $p_i$.
  - **Mirror symmetry** $\mathcal{M}_2, \mathcal{M}_3$ – Symmetry under port exchange for a 2-port device, or any reflection for a rotationally symmetric 3-port device.
  - **Complete port symmetry** $\mathcal{R}(n)$ – Symmetry under all possible relabelings of the ports.
Equivalence Groups For the 24 One-Port, Two-State Elements:

$2 \cdot 1 \cdot 2 = 4$ I/O syndromes $\Rightarrow 4! = 24$ permutations (raw reversible transition functions).

**Stateful Reflector**

-State Unused—Not Atomic

**Configurable Inverter**

-Doesn’t Change State

**Toggle**

-Doesn’t Use State

**Toggle & Conditional Invert**

-Neither flux-negation symmetric nor flux-conserving

**Exchange (RM)**

**Conditional Toggle**

-Doesn’t Use State

**Type 4**

**Type 5**

(Neither flux-negation symmetric nor flux-conserving)
Two-Port, Two-State, Flux-Polarized Elements

There are $2^3 = 8$ I/O syndromes, thus $8! = 40,320$ raw reversible transition functions.

- But only 96 of them satisfy the flux conservation constraint.
- And only 10 of these are nontrivial primitives satisfying all constraints.

These 10 functions sort into 7 equivalence groups as follows:

<table>
<thead>
<tr>
<th>Self-Symmetry Group Size</th>
<th>Equivalence Group Size</th>
<th>Number of Equiv. Groups</th>
<th>Total # of Raw Trans. Funcs.</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
<td>1</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>2</td>
<td>2</td>
<td>3</td>
<td>8</td>
</tr>
<tr>
<td>TOTALS:</td>
<td></td>
<td>4</td>
<td>14</td>
</tr>
</tbody>
</table>

The corresponding functional behaviors can be described as:

1. Reversible Shift Register (RSR)
2. Directed Reversible Shift Register (DRSR)
3. Filtering RM Cell (FRM)
4. Directed Filtering RM Cell (DFRM)
5. Polarized Flipping Diode (PFD)
6. Asymmetric Polarity Filter (APF)
7. Two-Port Reversible Memory Cell (RM2)
Illustrations of 2-port, 2-state, flux-polarized elements:

(Table Rows Shown for ↑ Initial State Only)

1. Reversible Shift Register (RSR):

<table>
<thead>
<tr>
<th>Input syndrome</th>
<th>Output syndrome</th>
</tr>
</thead>
<tbody>
<tr>
<td>↑)A(↑)</td>
<td>(↑)B(↑)</td>
</tr>
<tr>
<td>↓)A(↑)</td>
<td>(↓)B(↑)</td>
</tr>
<tr>
<td>↑)B(↑)</td>
<td>(↑)A(↑)</td>
</tr>
<tr>
<td>↓)B(↑)</td>
<td>(↓)A(↑)</td>
</tr>
</tbody>
</table>

2. Directed Reversible Shift Register (DRSR):

<table>
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<th>Input syndrome</th>
<th>Output syndrome</th>
</tr>
</thead>
<tbody>
<tr>
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</tr>
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<td>(↓)B(↑)</td>
</tr>
<tr>
<td>↑)B(↑)</td>
<td>(↑)A(↑)</td>
</tr>
<tr>
<td>↓)B(↑)</td>
<td>(↑)A(↑)</td>
</tr>
</tbody>
</table>

3. Filtering RM Cell (FRM):

<table>
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<th>Output syndrome</th>
</tr>
</thead>
<tbody>
<tr>
<td>↑)A(↑)</td>
<td>(↑)B(↑)</td>
</tr>
<tr>
<td>↓)A(↑)</td>
<td>(↓)A(↑)</td>
</tr>
<tr>
<td>↑)B(↑)</td>
<td>(↑)A(↑)</td>
</tr>
<tr>
<td>↓)B(↑)</td>
<td>(↓)B(↑)</td>
</tr>
</tbody>
</table>
4. Directed Filtering RM Cell (DFRM):

<table>
<thead>
<tr>
<th>Input syndrome</th>
<th>Output syndrome</th>
</tr>
</thead>
<tbody>
<tr>
<td>↑⟩A(↑)</td>
<td>(↑)B(↑)</td>
</tr>
<tr>
<td>↓⟩A(↑)</td>
<td>(↓)A(↑)</td>
</tr>
<tr>
<td>↑⟩B(↑)</td>
<td>(↑)A(↑)</td>
</tr>
<tr>
<td>↓⟩B(↑)</td>
<td>(↓)B(↑)</td>
</tr>
</tbody>
</table>

5. Polarized Flipping Diode (PFD):

<table>
<thead>
<tr>
<th>Input syndrome</th>
<th>Output syndrome</th>
</tr>
</thead>
<tbody>
<tr>
<td>↑⟩A(↑)</td>
<td>(↑)A(↑)</td>
</tr>
<tr>
<td>↓⟩A(↑)</td>
<td>(↓)B(↑)</td>
</tr>
<tr>
<td>↑⟩B(↑)</td>
<td>(↑)B(↑)</td>
</tr>
<tr>
<td>↓⟩B(↑)</td>
<td>(↓)A(↑)</td>
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5. Asymmetric Polarity Filter (APF):

<table>
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</thead>
<tbody>
<tr>
<td>↑⟩A(↑)</td>
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</tr>
<tr>
<td>↓⟩A(↑)</td>
<td>(↓)B(↑)</td>
</tr>
<tr>
<td>↑⟩B(↑)</td>
<td>(↑)B(↑)</td>
</tr>
<tr>
<td>↓⟩B(↑)</td>
<td>(↓)A(↑)</td>
</tr>
</tbody>
</table>
Two-Port, Two-State, Flux-Neutral Elements

There are \((2^2)! = 24\) raw flux-symmetric transition functions.
- 14 of these are nontrivial, atomic functional primitives.

These sort into 4 equivalence groups as follows:

<table>
<thead>
<tr>
<th>Self-Symmetry Group Size</th>
<th>Equivalence Group Size</th>
<th>Number of Equiv. Groups</th>
<th>Total # of Raw Trans. Funcs.</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
<td>2</td>
<td>3</td>
<td>6</td>
</tr>
<tr>
<td>1</td>
<td>8</td>
<td>1</td>
<td>8</td>
</tr>
<tr>
<td><strong>TOTALS:</strong></td>
<td></td>
<td><strong>4</strong></td>
<td><strong>14</strong></td>
</tr>
</tbody>
</table>

There are 5 distinct functional behaviors (described in forwards time direction):
1. Alternating Barrier (AB), 2 reps. – See next slide.
2. Polarized Flipping Diode (PFD), 2 reps.
3. Variant Polarized Flipping Diode (VPFD), 2 reps.
4. Asymmetric Polarized Flipping Diode (APFD), 4 reps.,
   (\(D\)-dual to)
5. Selectable Barrier (SD), 4 reps.
Ex. 2-port, 2-state neutral element: **Alternating Barrier (AB)**

Flux-conserving, flux-negation symmetric element.
- Also has mirror ($\mathcal{M}_2$) symmetry.
- Has two $\mathcal{D}, \mathcal{S}$ dual representations.

Flux-neutral internal states $\rightarrow$ Doesn’t change fluxon polarity.

State descriptions:
- $S^+_{-B}$: *Positive-wire, negative-barrier.*
  - Transmits positive (↑) fluxons, reflects negative (↓) fluxons.
- $S^+_{+B}$: *Positive-Barrier, negative-wire.*
  - Reflects positive (↑) fluxons, transmits negative (↓) fluxons.

Transition function description:
- Fluxons arriving at either port are routed as per the state descriptions above.
- State toggles with every interaction.

<table>
<thead>
<tr>
<th>Input Syndrome</th>
<th>Output Syndrome</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\uparrow)p_1(S^+_{-B})$</td>
<td>$(S^+_{+B})p_2) \uparrow$</td>
</tr>
<tr>
<td>$\downarrow)p_1(S^+_{-B})$</td>
<td>$(S^+_{+B})p_1) \downarrow$</td>
</tr>
<tr>
<td>$\uparrow)p_2(S^+_{+B})$</td>
<td>$(S^+_{+B})p_1) \uparrow$</td>
</tr>
<tr>
<td>$\downarrow)p_2(S^+_{+B})$</td>
<td>$(S^+_{+B})p_2) \downarrow$</td>
</tr>
<tr>
<td>$\uparrow)p_1(S^+_{+B})$</td>
<td>$(S^+_{+B})p_1) \uparrow$</td>
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<tr>
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<td>$(S^+_{+B})p_2) \downarrow$</td>
</tr>
<tr>
<td>$\uparrow)p_2(S^+_{+B})$</td>
<td>$(S^+_{+B})p_2) \uparrow$</td>
</tr>
<tr>
<td>$\downarrow)p_2(S^+_{+B})$</td>
<td>$(S^+_{+B})p_1) \downarrow$</td>
</tr>
</tbody>
</table>
Results for Three-Port, Two-State Elements:

Devices with flux-polarized states:
- $2 \cdot 3 \cdot 2 = 12$ I/O syndromes
- $12! = 497,001,600$ raw reversible funcs.
- $25,920$ of these are flux-conserving.
- $288$ of those are flux-negation symmetric.
- $245$ of those are atomic (primitives).
- $219$ of those use the state non-trivially.
- Sort into $39$ equiv. groups as follows →

<table>
<thead>
<tr>
<th>Equivalence Class Size:</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>6</th>
<th>12</th>
<th>Tot.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Self-Symmetry Group Size:</td>
<td>12</td>
<td>6</td>
<td>4</td>
<td>2</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>No. of Equivalence Classes:</td>
<td>1</td>
<td>4</td>
<td>6</td>
<td>24</td>
<td>4</td>
<td>39</td>
</tr>
<tr>
<td>Total number of Functions:</td>
<td>1</td>
<td>8</td>
<td>18</td>
<td>144</td>
<td>48</td>
<td>219</td>
</tr>
</tbody>
</table>

Devices with flux-neutral states:
- $1 \cdot 3 \cdot 2 = 6$ I/O syndromes (for ↑ inputs)
- $6! = 720$ permutations.
- $653$ of them are atomic primitives.
- $600$ of those use the state non-trivially.
- Sort into $45$ equiv. groups as follows:

<table>
<thead>
<tr>
<th>Equivalence Class Size:</th>
<th>2</th>
<th>4</th>
<th>6</th>
<th>12</th>
<th>24</th>
<th>Tot.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Self-Symmetry Group Size:</td>
<td>12</td>
<td>6</td>
<td>4</td>
<td>2</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>No. of Equivalence Classes:</td>
<td>1</td>
<td>1</td>
<td>9</td>
<td>23</td>
<td>11</td>
<td>45</td>
</tr>
<tr>
<td>Total number of Functions:</td>
<td>2</td>
<td>4</td>
<td>54</td>
<td>276</td>
<td>264</td>
<td>600</td>
</tr>
</tbody>
</table>
Illustrations of some 3-port, 2-state flux-neutral elements

Recall there are 45 different non-trivial, atomic functional behaviors (counting $\mathcal{D}$-duals as equivalent). Of these, only a few exemplar behaviors are illustrated here. Still seeking implementations of any of these….

(All state behaviors shown are for + fluxons only; − fluxons interact oppositely w states)
Some Next Steps for the BARCS effort

1. Document classification results more fully.

2. Finish developing **SCIT** (Superconducting Circuit Innovation Tool) tool to facilitate discovery of circuit-level implementations of BARCS functions.

3. Better understand role of physical symmetries in the circuit design of BARCS elements.

4. Identify a computation-universal set of primitive elements that we also know how to implement!

5. Additional work on fabrication & empirical validation of BARCS circuit designs.

6. Understand the limits of energy efficiency of this approach.

Much work remains to be done!
- We would be very happy to recruit new collaborators
Conclusion

The long-neglected *ballistic* mode of reversible computing has recently attracted renewed interest.

- Classic problems with synchronization & chaotic instability in ballistic computing schemes seem to be resolvable via the asynchronous approach.
- Method appears to hold promise for possibly achieving improved energy-delay products vs. adiabatic approaches.

Also, note that ballistic approaches are not viable *at all* in CMOS!

- CMOS has nothing like a ballistic flux soliton, & has no nonlinear reactive elements like JJs…
- Thus, we are leveraging unique advantages of superconducting electronics in this approach.

In this paper & talk, we reported our progress on enumerating & classifying possible BARCS functions…

- assuming logical reversibility, flux conservation, & flux negation symmetry.

Multiple US-based research groups in superconductor physics & engineering are now making early progress along this line of work…

- We invite additional domestic & international colleagues to join us in investigating this interesting line of research!