

# PERFORMANCE OF CONTAINMENT VESSEL UNDER SEVERE ACCIDENT CONDITIONS

SPE analysis meeting #2  
*April 13-14, 2011, Washington DC*

## SUMMARY

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- Model 1** : Sensitivity analyses & findings
- Model 2** : Methodology & difficulties



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# Model 1

## SUMMARY

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- Sensitivity analyses** :
- **Mesh discretisation**
  - **Mesh element type**
  - **Concrete constitutive law**
  - **Concrete constitutive law parameters**
  - **Tendon / Duct interaction**

# Modelling technique

## Concrete

Solid element

Linear and quadratic configurations

Mesh size: described in another section

## Liner

Shell elements

Thickness 1.6mm

Liner perfectly bonded with concrete

## Hoop tendons

Truss elements

Tendon / concrete interface: 3 configurations

1- Grouted ducts: perfectly bonded

2- Slippery ducts (perfectly bonded in Z and R direction, free along tendon direction)

3- UngROUTED ducts (perfectly bonded in Z and R direction, friction along tendon direction)

## steel reinforcement

Grid elements

Shell element with uniaxial behaviour

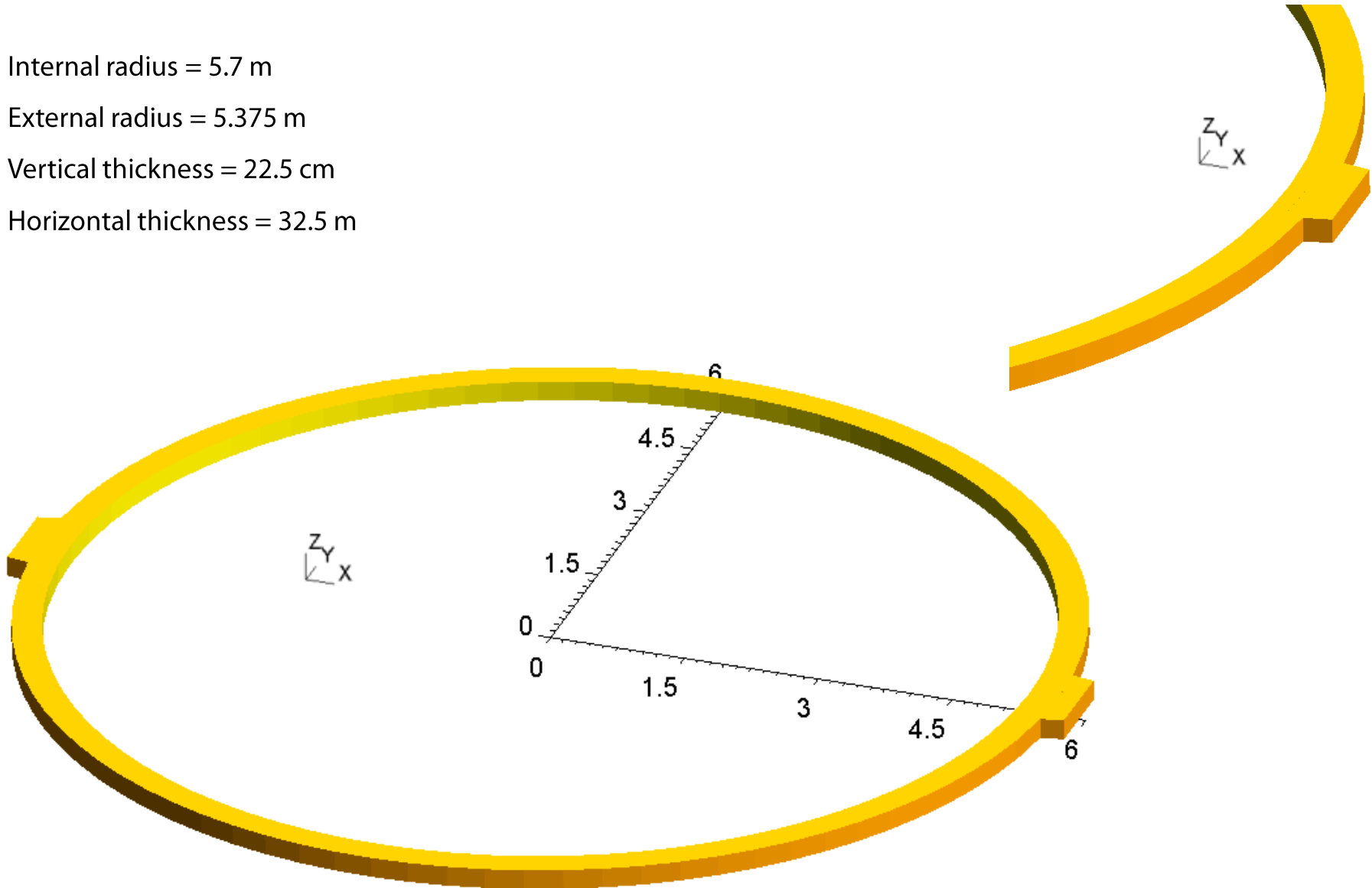
Linear

Rebar / concrete interface: perfectly bonded

Placed on inner and outer surfaces of concrete mesh

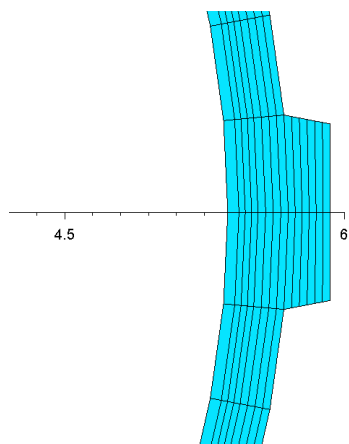
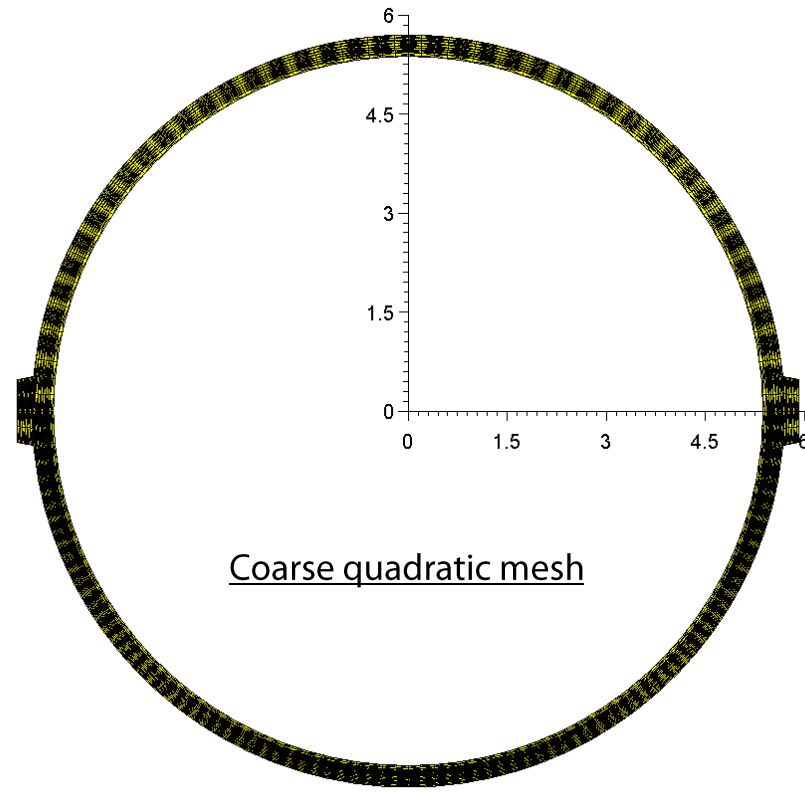
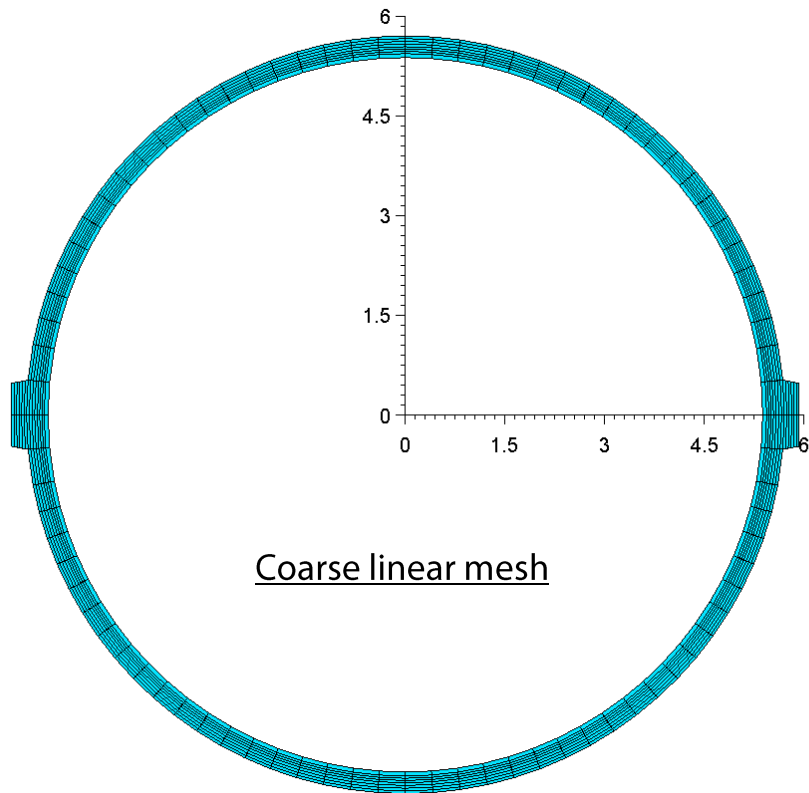
# Model geometry

- Internal radius = 5.7 m
- External radius = 5.375 m
- Vertical thickness = 22.5 cm
- Horizontal thickness = 32.5 m

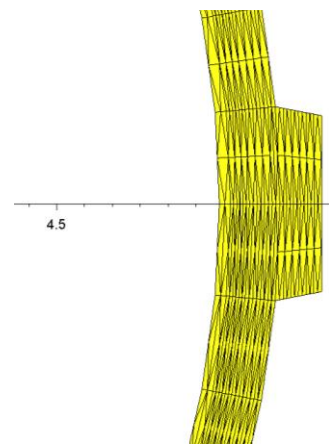


# Mesh discretisation

3 situations

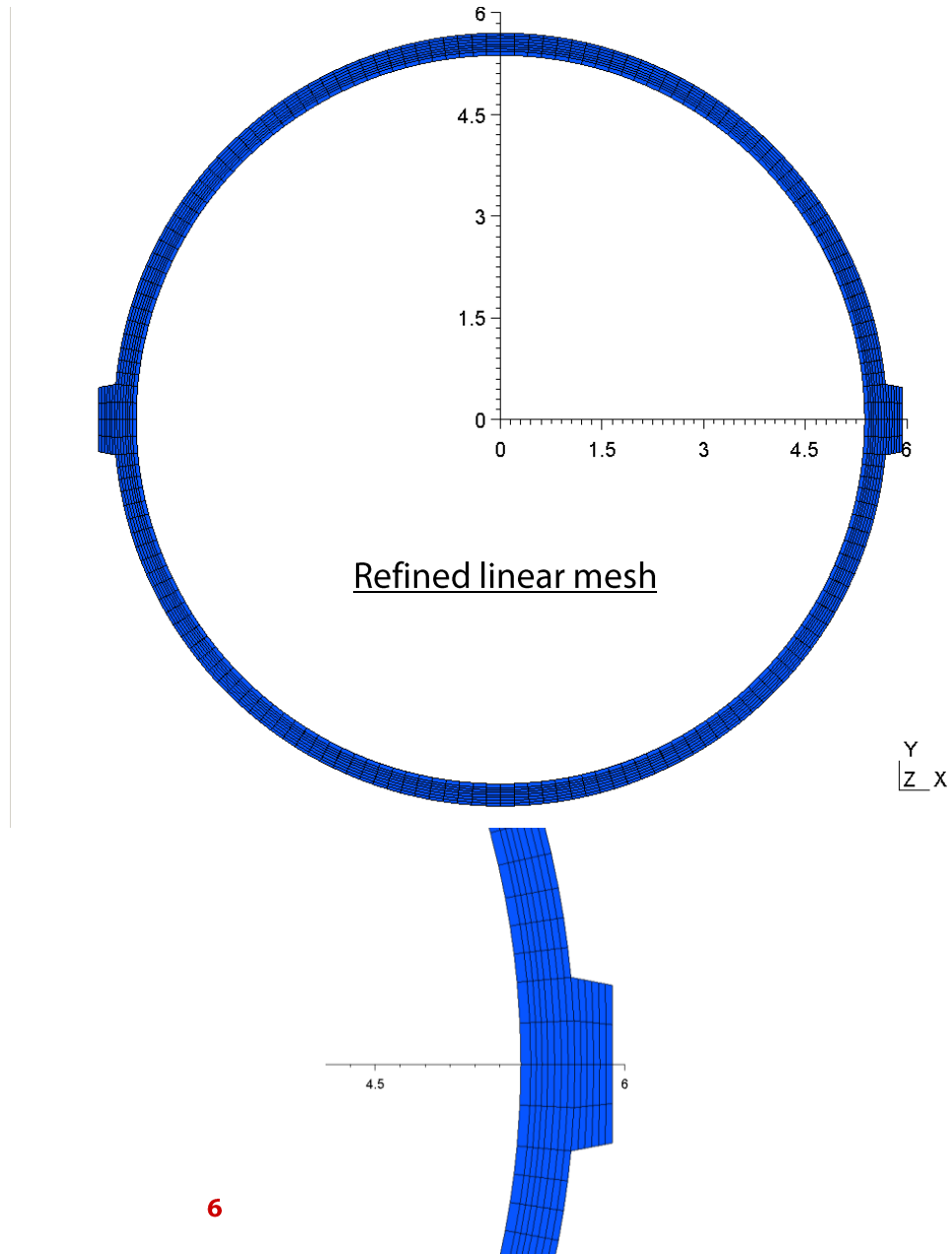


A1



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# Mesh discretisation

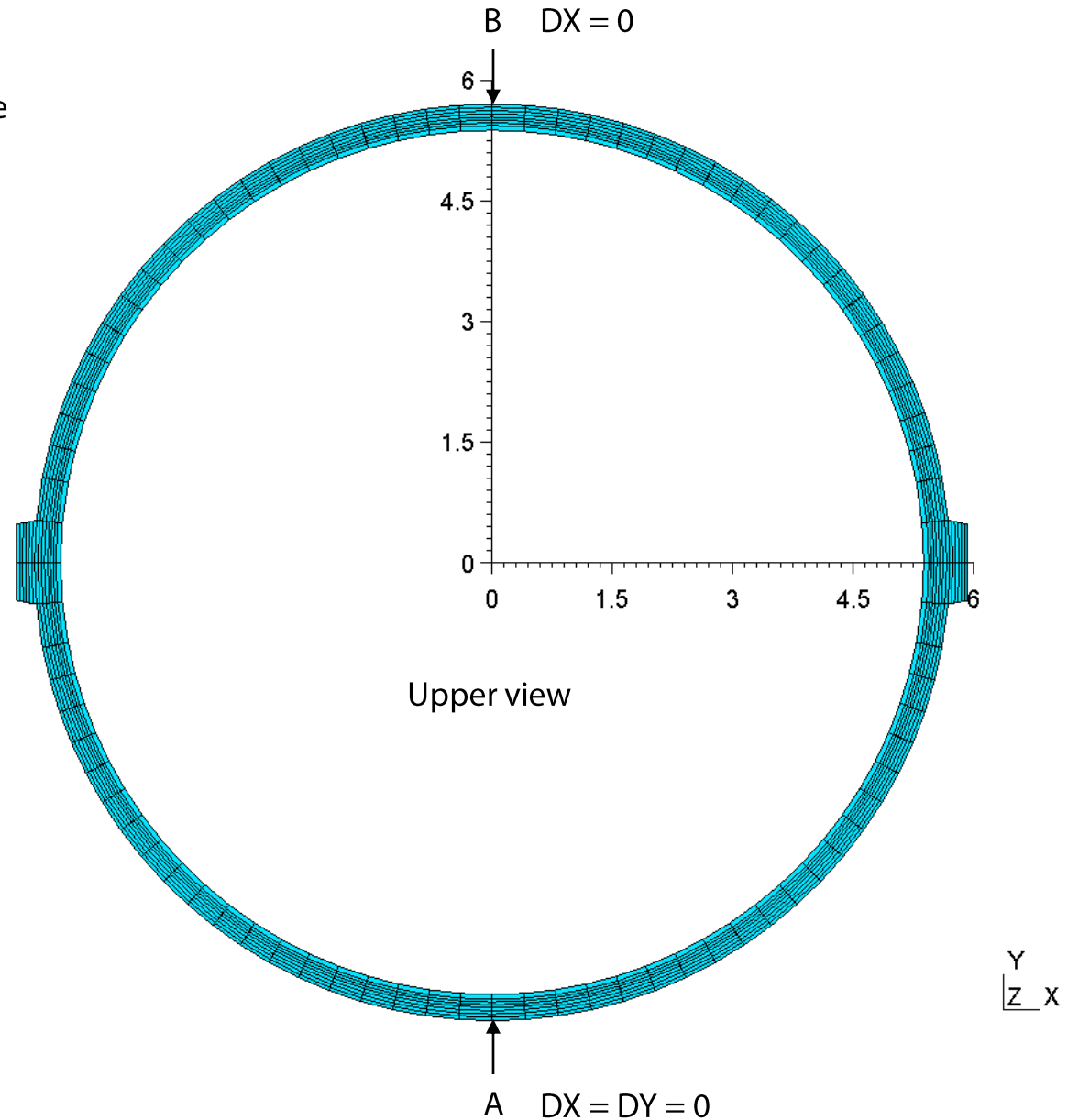


# Boundary conditions

Upper face: Z DOF follow the same value

Lower face:  $DZ=0$

See figure for the others



# Concrete constitutive model

Known as "Mazars"

## Features :

- Based on damage mechanics
- Unilateral behaviour (tension / compression distinction)
- Isotropic damage effect (single scalar damage index D)
- No crack reclosure (not suitable for cyclic loading)

$$\sigma_{ij} = (1 - D) C_{ijkl} \varepsilon_{kl}$$

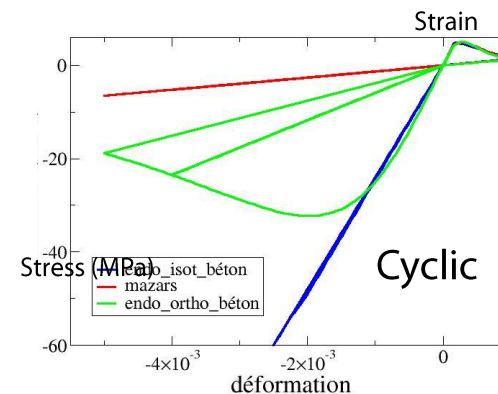
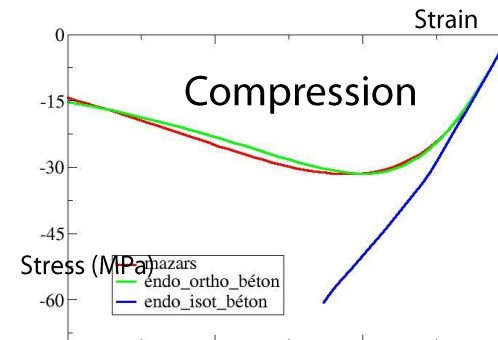
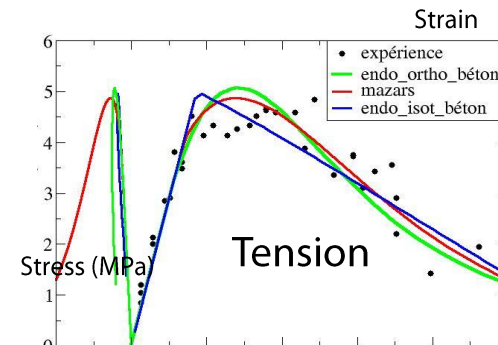
$$D = \alpha_t D_t + \alpha_c D_c$$

$$\alpha_{t,c} = \left( \sum_{i=1}^3 \frac{\langle \varepsilon_i^{t,c} \rangle \langle \varepsilon_i \rangle_+}{\varepsilon_{eq}^2} \right)^\beta$$

$$D_{t,c} = 1 - \frac{\varepsilon_{eq0} (1 - A_{t,c})}{\varepsilon_{eq}} - \frac{A_{t,c}}{\exp[B_{t,c} (\varepsilon_{eq} - \varepsilon_{eq0})]}$$

$$\varepsilon_{eq} = \sqrt{\sum_{i=1}^3 (\langle \varepsilon_i \rangle_+)^2}$$

Mazars : red curves

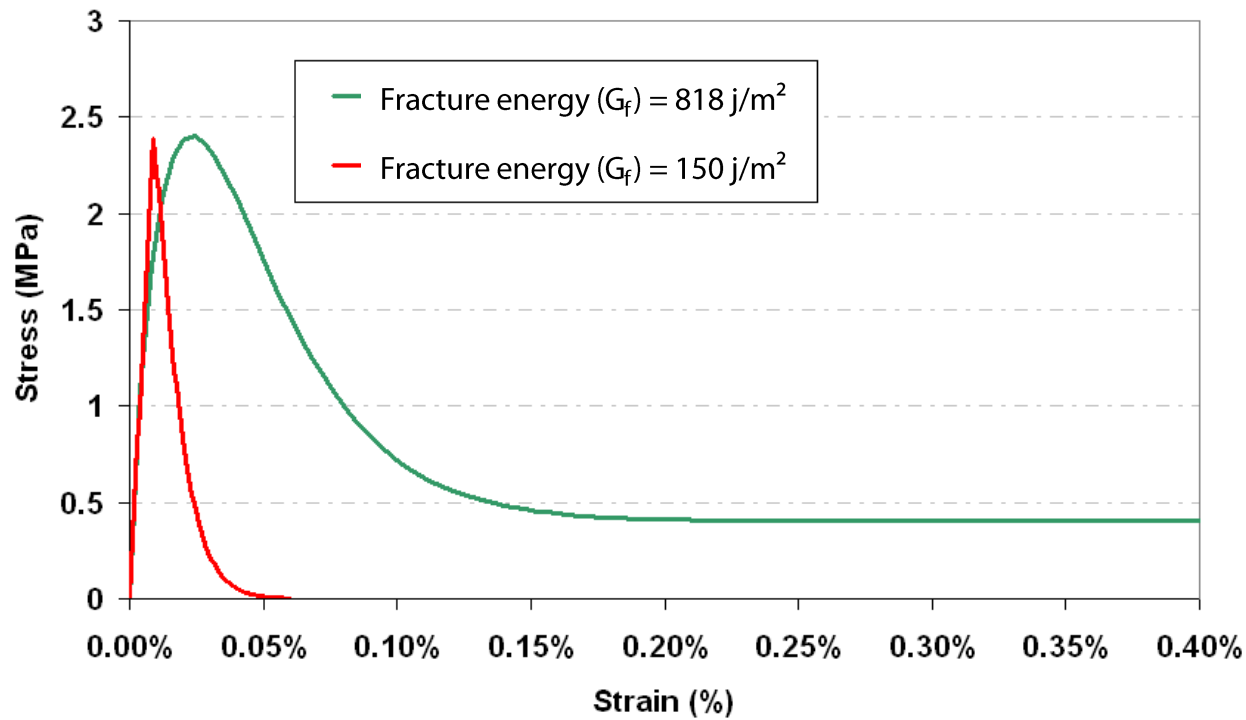




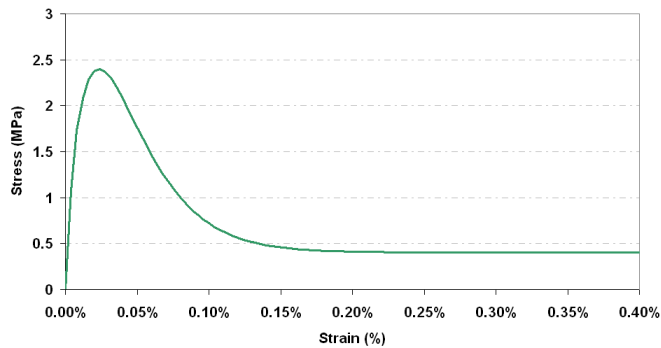
# Concrete constitutive model

Material parameter set	M818	M150
Fracture energy ( $G_f$ )	818 j/m <sup>2</sup>	150 j/m <sup>2</sup>
Mesh size	43 cm	43 cm
Young's Modulus (E)	26 900 MPa	26 900 MPa
Poisson's ratio ( $\nu$ )	0.21	0.21
Density ( $\rho$ )	2 176 kg/m <sup>3</sup>	2 176 kg/m <sup>3</sup>
Tensile Strength ( $f_t$ )	2.4 MPa	2.4 MPa
Strain	0.024%	0.009%
Compressive Strength ( $f_c$ )	61 MPa	62 MPa
Strain	0.54%	0.54%

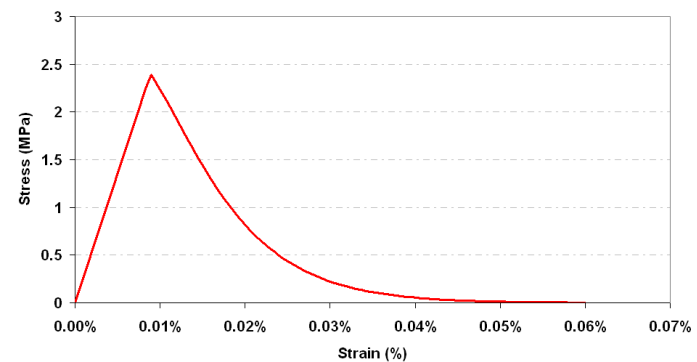
# Concrete constitutive model



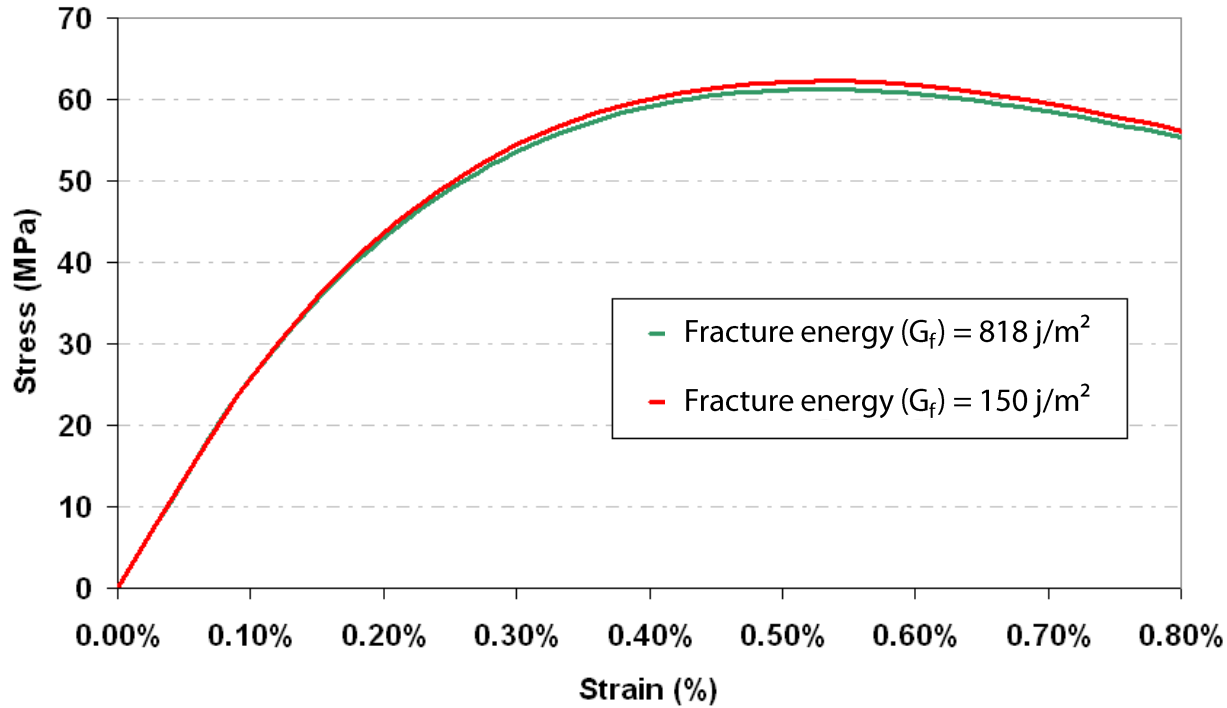
Tensile behaviour (Cracking Energy = 818 N/m)



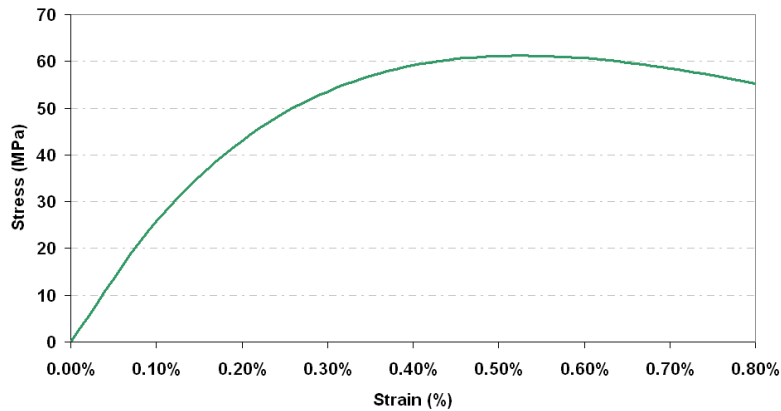
Tensile behaviour (Cracking Energy = 150 N/m)



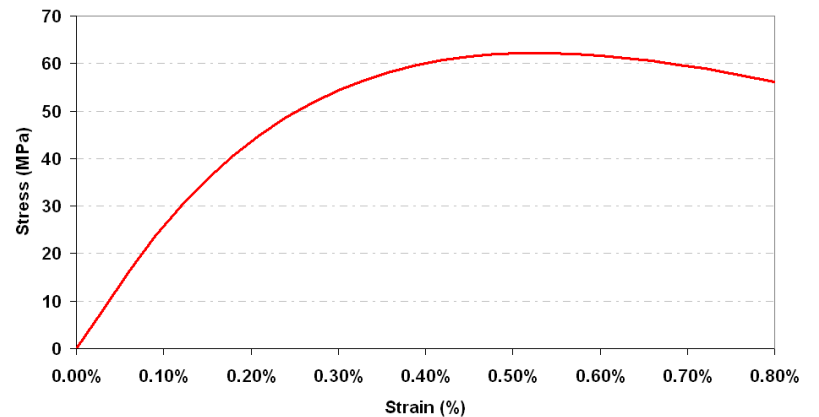
# Concrete constitutive model



Compressive behaviour (Cracking Energy = 818 N/m)



Compressive behaviour (Cracking Energy = 150 N/m)



# Liner steel constitutive model

Elastoplastic

**Parameters:**

Young's Modulus (E) = 210 000 MPa

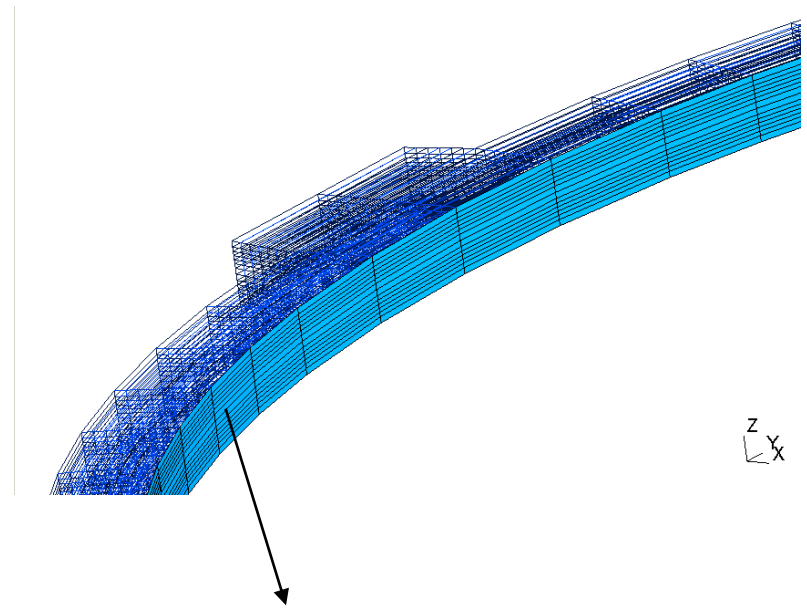
Young Modulus in plastic phase (E) = 927 MPa

Poisson's ratio ( $\nu$ ) = 0.3

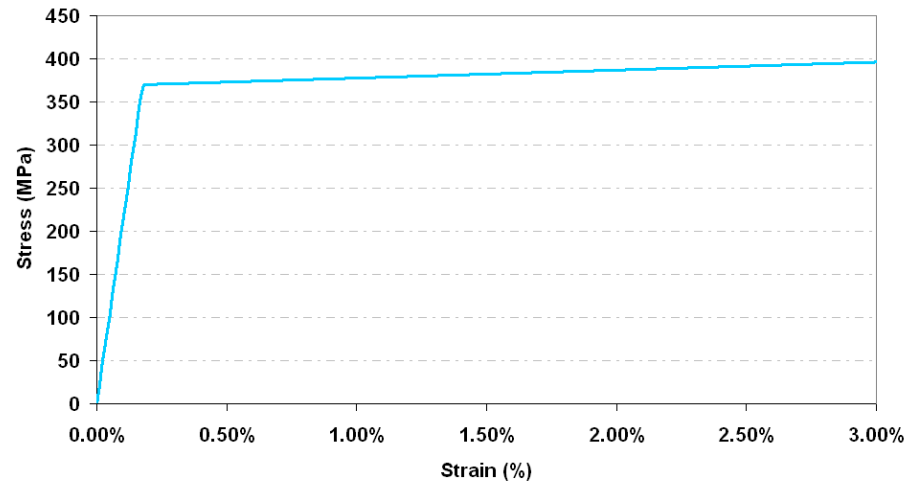
Density ( $\rho$ ) = 7850 kg/m<sup>3</sup>

Yield Strength ( $Y_s$ ) = 370 MPa

Density ( $\rho$ ) = 7 850 kg/m<sup>3</sup>



Liner thickness = 1.6 mm



# Tendon steel constitutive model

Elastoplastic

**Parameters:**

Young Modulus in elastic phase (E) = 191 000 MPa

Young Modulus in plastic phase (E) = 5 894 MPa

Poisson's ratio ( $\nu$ ) = 0.3

Density ( $\rho$ ) = 7850 kg/m<sup>3</sup>

Yield Strength ( $Y_s$ ) = 1 679MPa

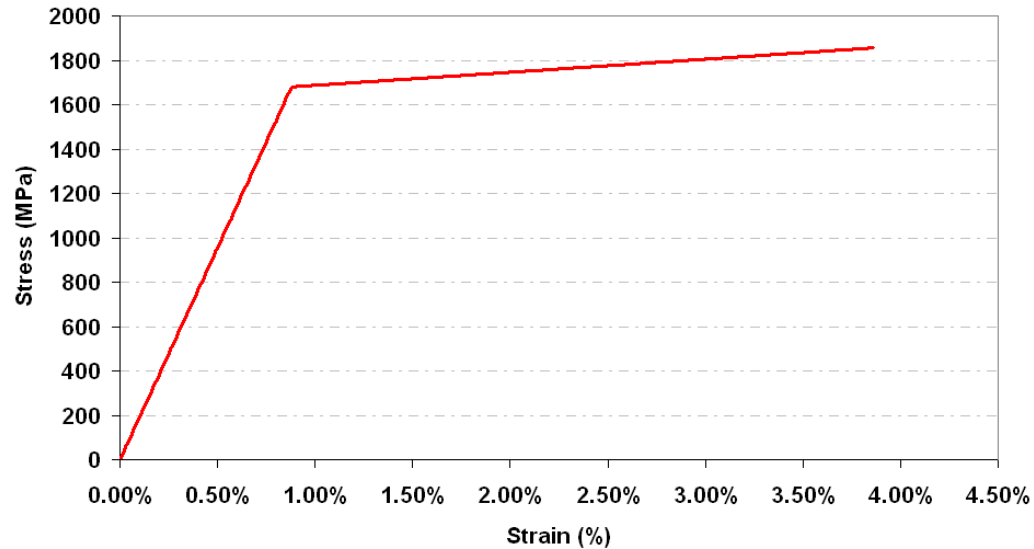
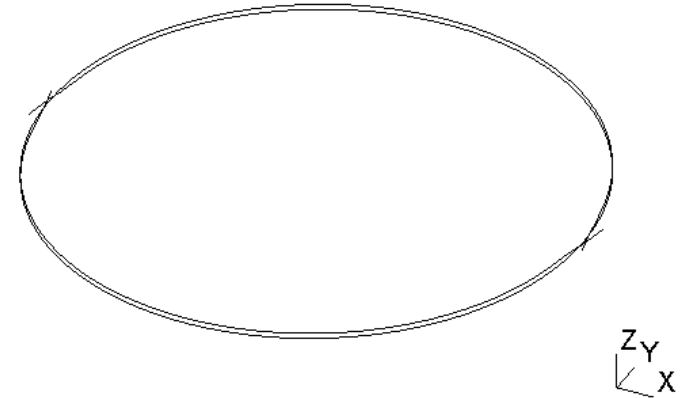
Tensile Strength (XXX) = 1 856.76 MPa

Density ( $\rho$ ) = 7850 kg/m<sup>3</sup>

Setting Losses = 3.95 mm

Angular and wobble friction:  $\mu = 0.21$ ;  $\lambda = 0.001$

Tendons section = 3.393 cm<sup>2</sup> (each tendon)



# Tendon steel constitutive model

Elastoplastic

**Parameters:**

Young Modulus in elastic phase (E) = 185 000 MPa

Young Modulus in plastic phase (E) = 927 MPa

Poisson's ratio ( $\nu$ ) = 0.3

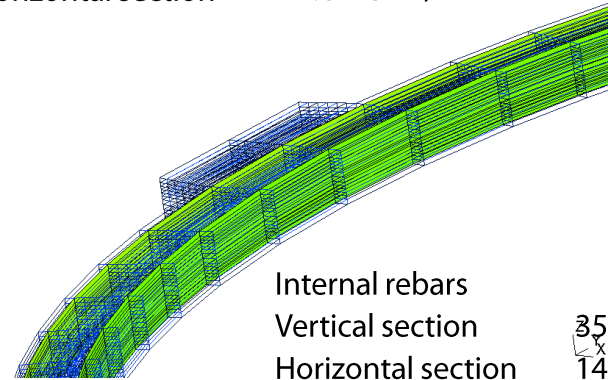
Density ( $\rho$ ) = 7 850 kg/m<sup>3</sup>

Yield Strength ( $Y_s$ ) = 408 MPa

External rebars

Vertical section 35.3 cm<sup>2</sup>/ml

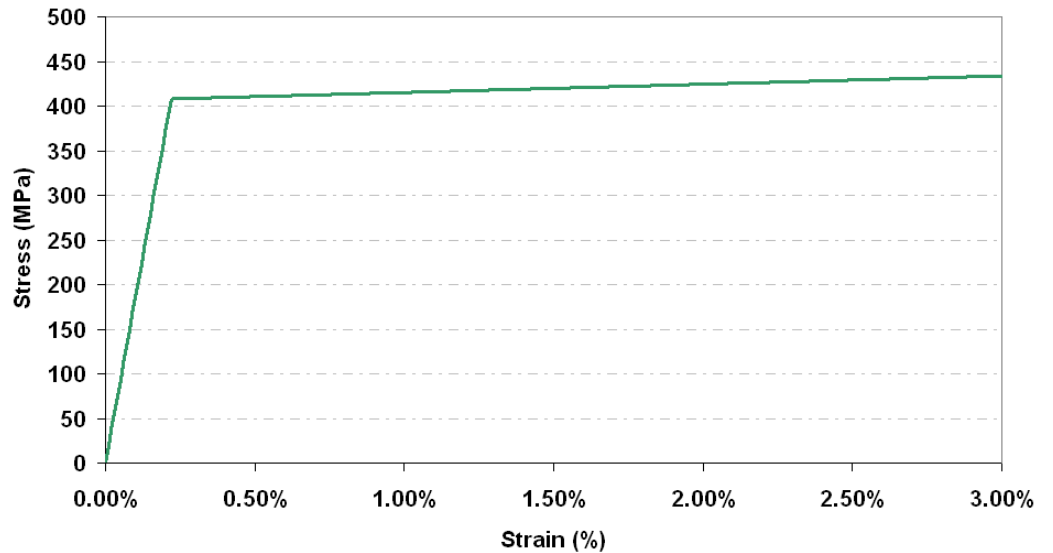
Horizontal section 12.84 cm<sup>2</sup>/ml



Internal rebars

Vertical section 35.3 cm<sup>2</sup>/ml

Horizontal section 14.41 cm<sup>2</sup>/ml



# Loading

Initial condition:

Hoop prestressing of 444 kN

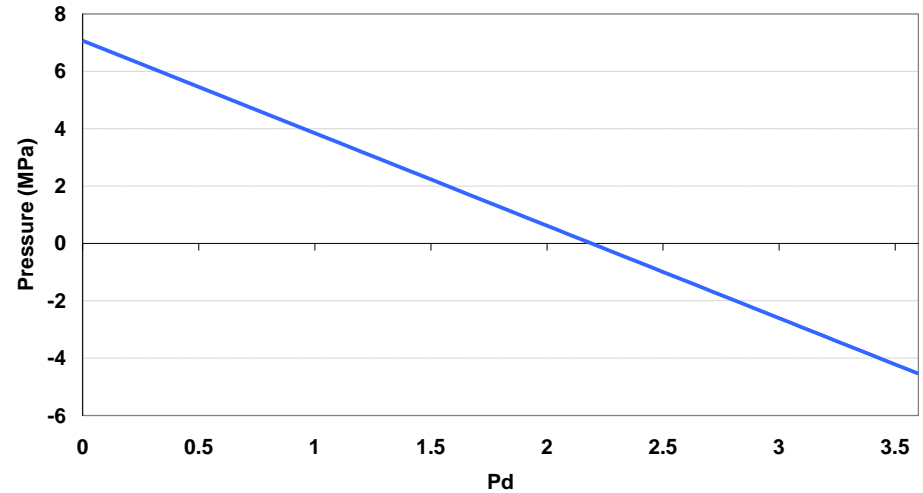
Downward pressure on top surface of 7.02 MPa

followed by:

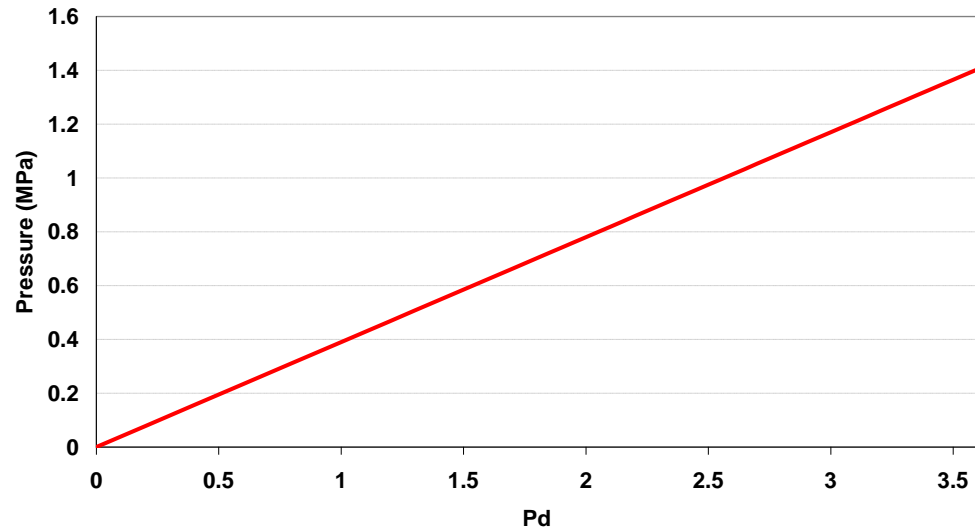
Internal pressure P

Upward pressure on top surface of  $8.27 \times P$  MPa

Upper face pressure



Internal pressure



# Sensitivity analyses

Case study	Mesh	Tendon type	Concrete	Liner	Tendon	Rebar
Tendon type effect (TTE)	GROL	GD	M818	NL	NL	NL
		SD				
		NGD				
Mesh Type Effect (MTE)	GROL	GD	LE	LE	LE	LE
	FINL					
	GROQ					
Cracking energy effect (CEE)	GROL	SD	M818	NL	NL	NL
			M150			

## Rebar behaviour

Linear LE  
Non-linear NL

## Tendon type

Grouted duct GD  
Slippery duct SD  
Ungouted duct UGD

## Concrete behaviour

Linear LE  
EDF\_2005 MEDF  
Mazars (818 j/m<sup>2</sup>, L=0.43 m) M818  
Mazars (150 j/m<sup>2</sup>, L=0.43 m) M150

## Meshing

Coarse - linear GROL  
Refined - linear FINL  
Coarse quadratic GROQ

## Tendon behaviour

Linear LE  
Non-linear NL

## Liner behaviour

Linear LE  
Non-linear NL



# Sensitivity analyses: tendon/duct interaction

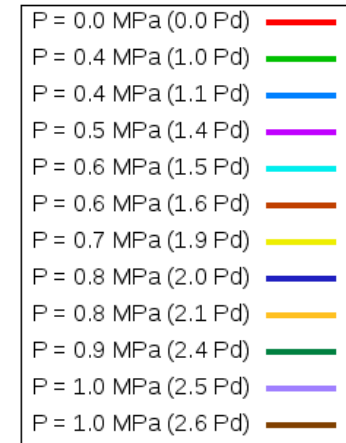
## Nonlinear analysis

With grouted duct, high strain localisation appear where concrete cracks (modelling simplification).

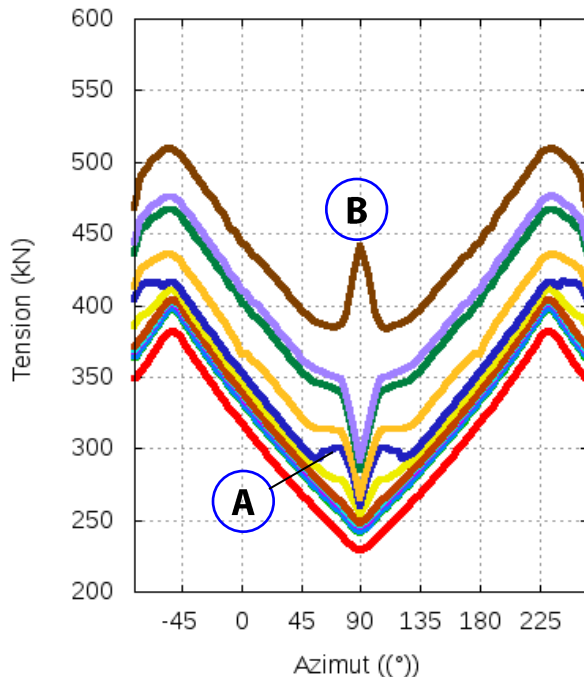
When ducts are ungrouted, localisation is less strong (representative of Sandia test).

Fully slippery ducts produce uniform tendon tension. The initial prestressing should have been lowered to encounter for losses.

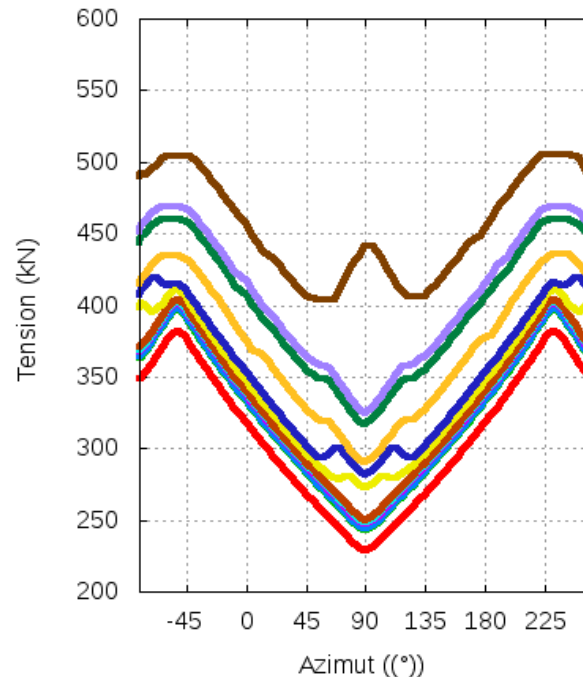
### Tendon H-67 tension distribution



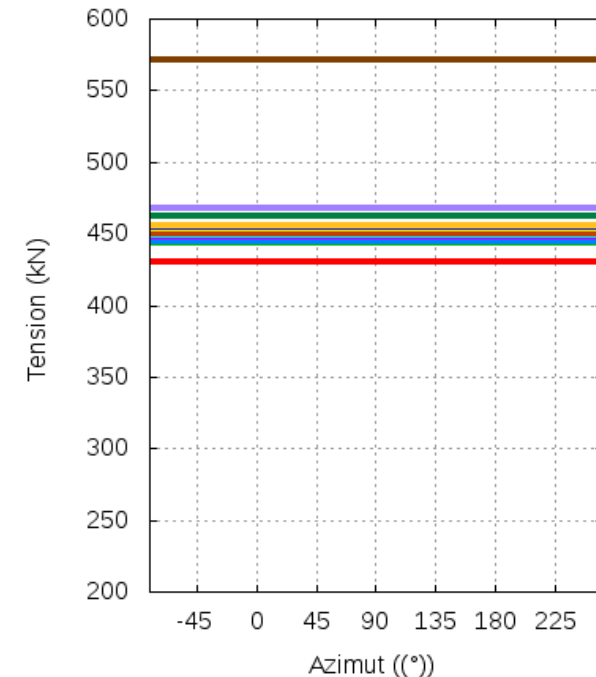
Grouted duct



Ungouted duct



Slippery duct



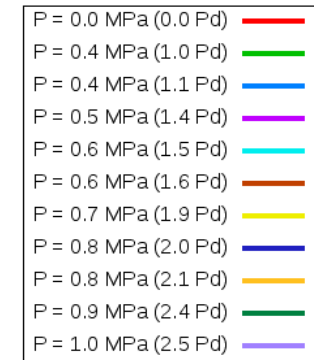
# Sensitivity analyses: tendon/duct interaction

## Nonlinear analysis

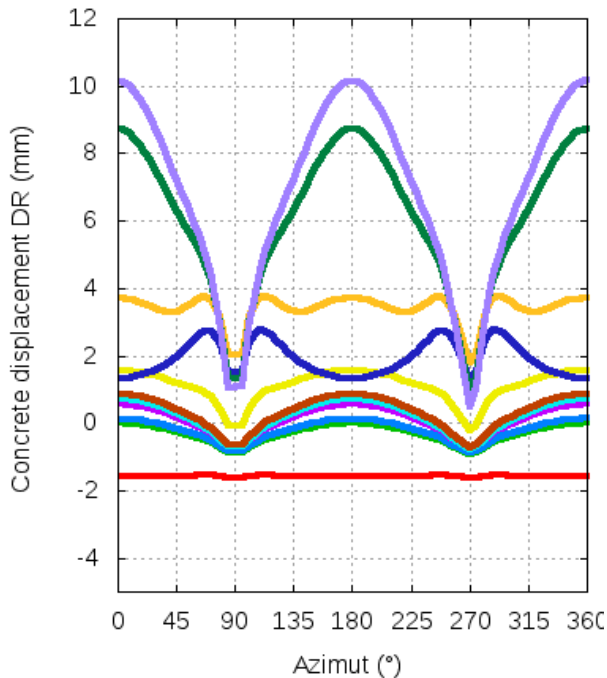
Grouted and ungrouted tendons exhibit the same radial displacements during linear elastic range of behaviour. This is also the case at high internal pressure loading with strong concrete damage. In between, results are significantly different.

For fully slippery duct, deflections are uniform, and lower, due to stronger prestressing.

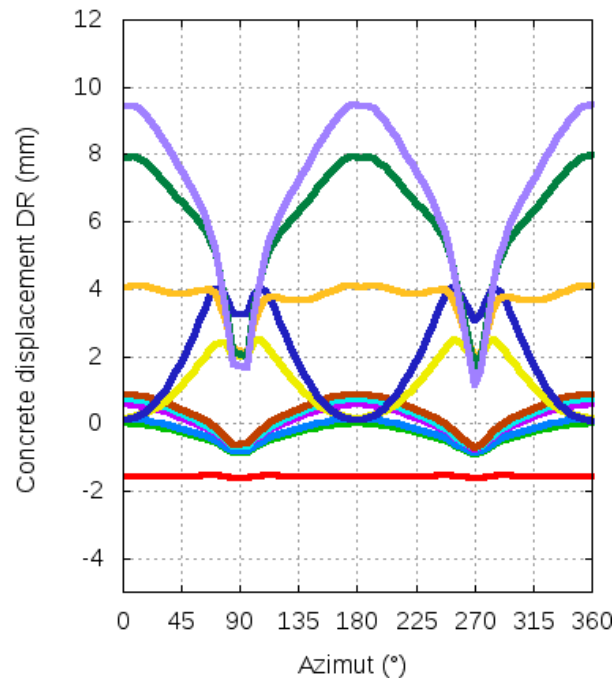
### Radial displacement ( $z = H/2$ , external face)



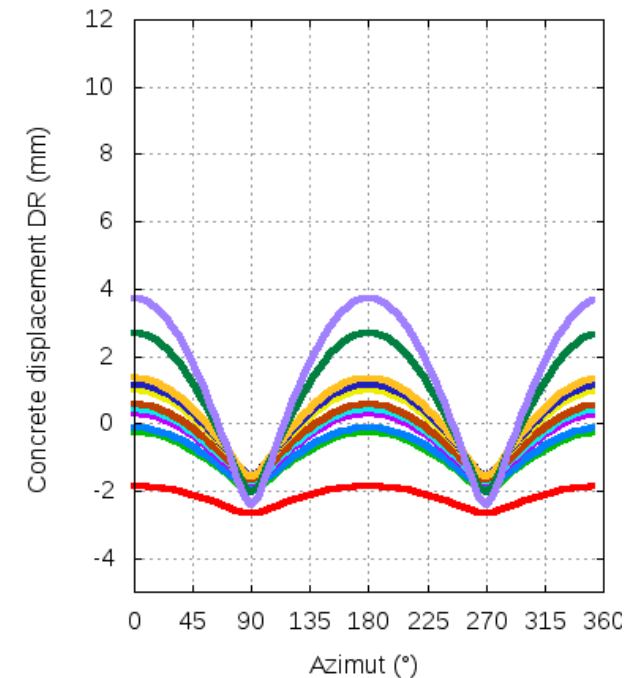
Grouted duct



Ungouted duct



Slippery duct



# Sensitivity analyses: tendon/duct interaction

## Nonlinear analysis

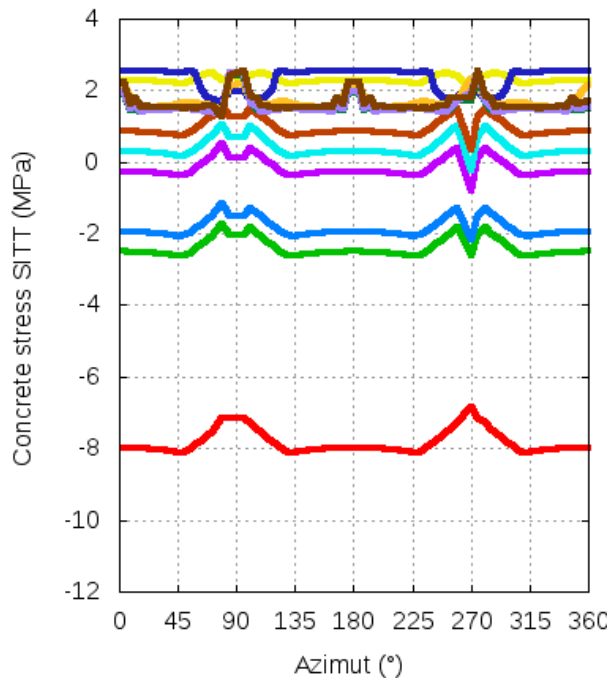
Concrete hoop stresses are quite similar between both grouted and ungrouted tendons.

Slippery ducts lead to late cracking

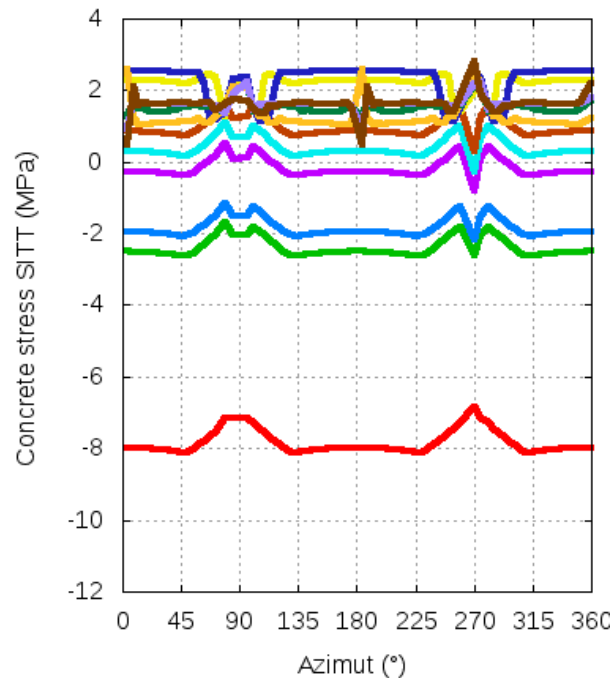
### Concrete hoop stress (z = H/2, mid-section)

P = 0.0 MPa (0.0 Pd)	—
P = 0.4 MPa (1.0 Pd)	—
P = 0.4 MPa (1.1 Pd)	—
P = 0.5 MPa (1.4 Pd)	—
P = 0.6 MPa (1.5 Pd)	—
P = 0.6 MPa (1.6 Pd)	—
P = 0.7 MPa (1.9 Pd)	—
P = 0.8 MPa (2.0 Pd)	—
P = 0.8 MPa (2.1 Pd)	—
P = 0.9 MPa (2.4 Pd)	—
P = 1.0 MPa (2.5 Pd)	—
P = 1.0 MPa (2.6 Pd)	—

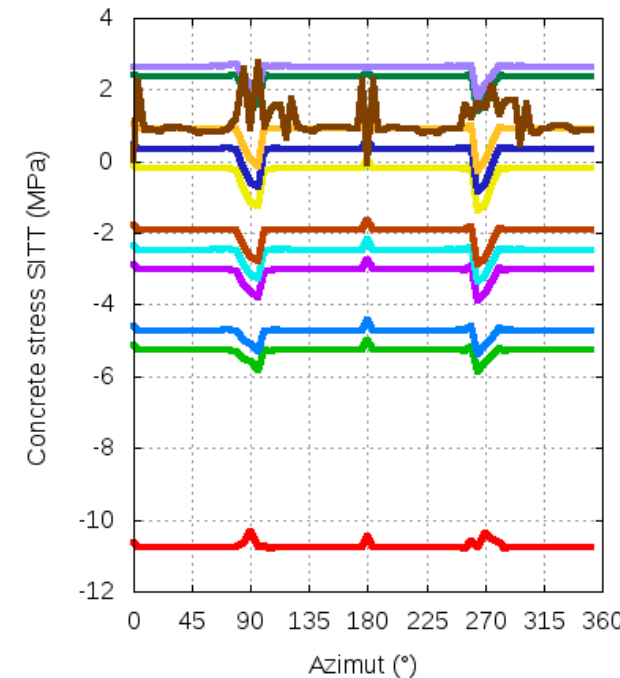
Grouted duct



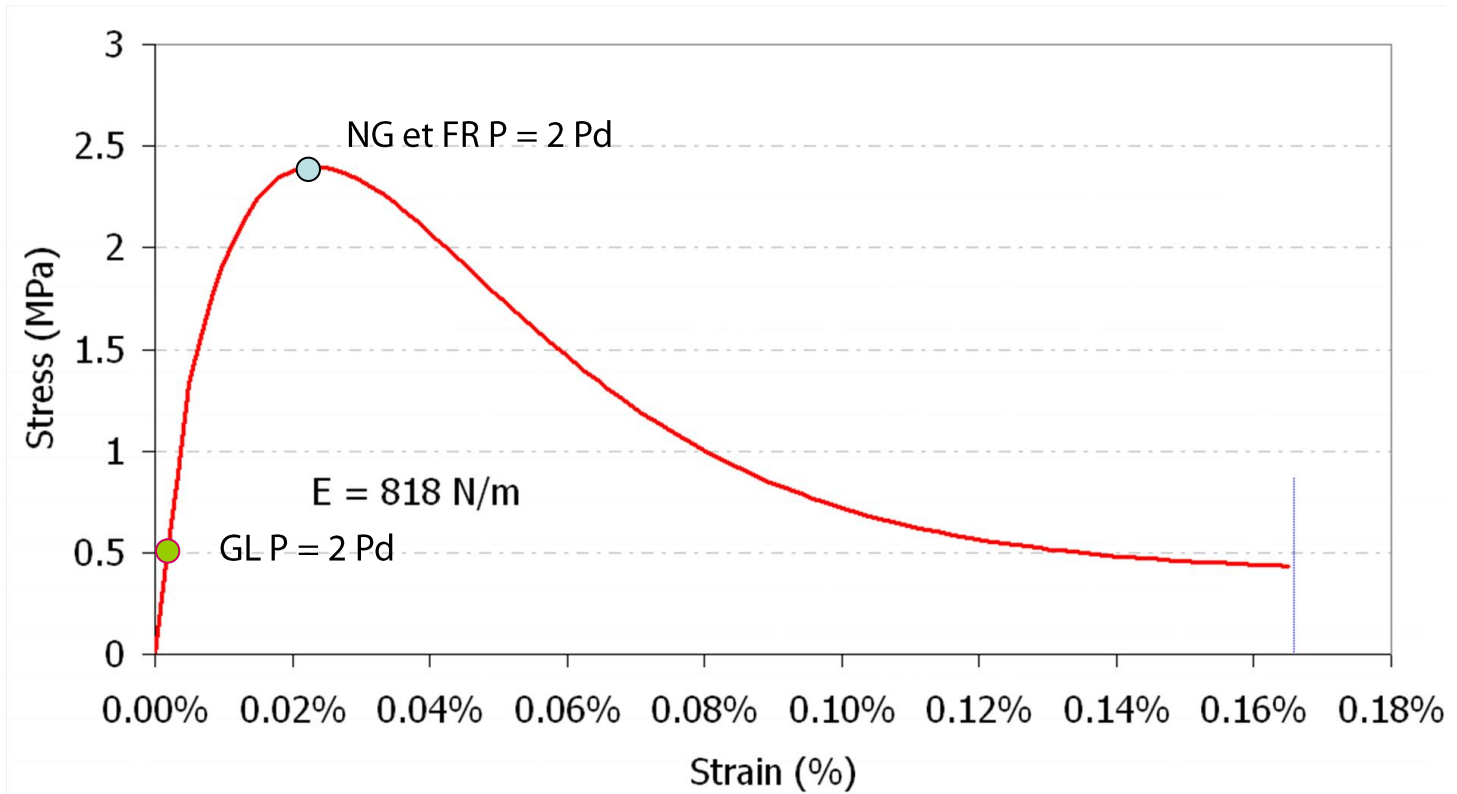
Ungrouped duct



Slippery duct



# Sensitivity analyses



# Sensitivity analyses: mesh element type

## Grouted ducts – Linear elastic analysis

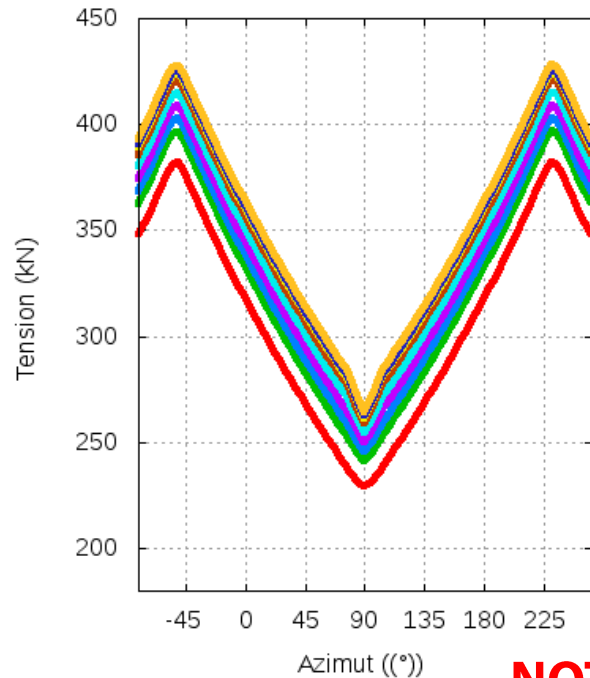
Very slight differences on tendon tensile forces (higher values for linear elements).

Variations are more emphasised with quadratic elements.

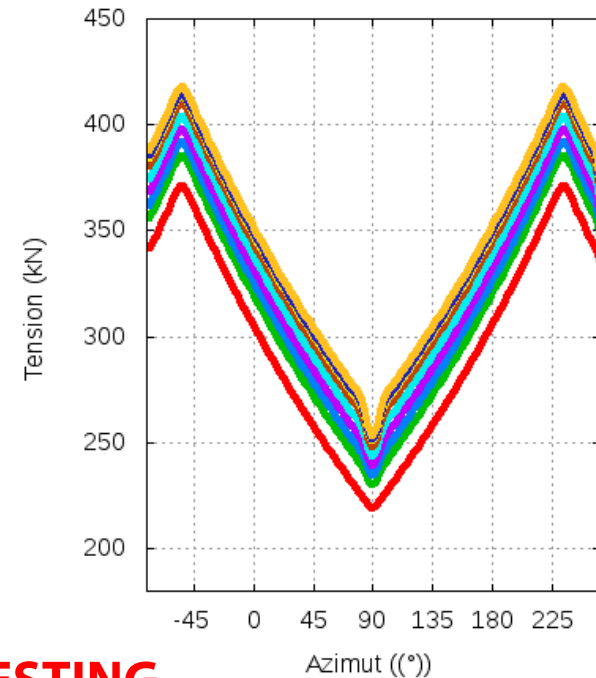
### Tendon 67 tension

P = 0.0 MPa (0.0 Pd)	<span style="color: red;">—</span>
P = 0.4 MPa (1.0 Pd)	<span style="color: green;">—</span>
P = 0.6 MPa (1.5 Pd)	<span style="color: blue;">—</span>
P = 0.8 MPa (2.0 Pd)	<span style="color: purple;">—</span>
P = 1.0 MPa (2.5 Pd)	<span style="color: cyan;">—</span>
P = 1.2 MPa (3.0 Pd)	<span style="color: brown;">—</span>
P = 1.3 MPa (3.3 Pd)	<span style="color: yellow;">—</span>
P = 1.3 MPa (3.4 Pd)	<span style="color: darkblue;">—</span>
P = 1.4 MPa (3.6 Pd)	<span style="color: orange;">—</span>

Coarse linear meshing



Coarse quadratic meshing



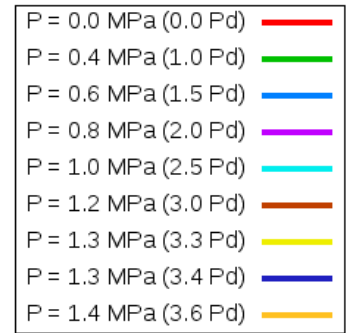
**NOT VERY INTERESTING**

# Sensitivity analyses: mesh element type

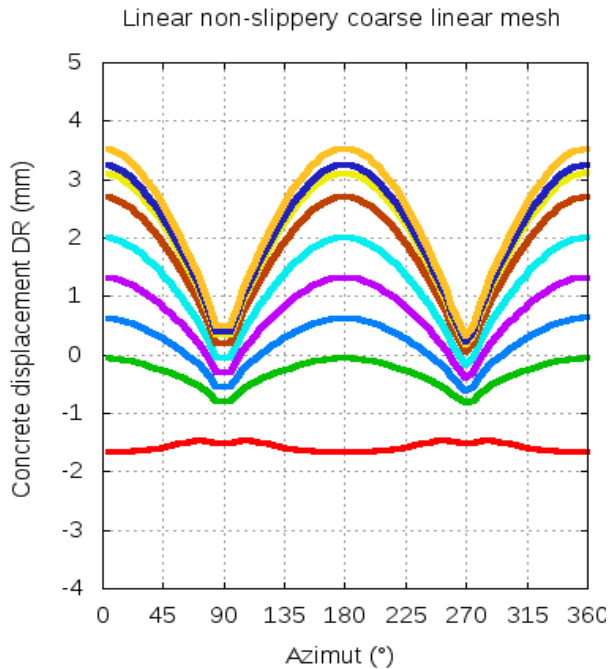
## Grouted ducts – Linear elastic analysis

Refined and quadratic meshing produce larger displacement. This is due to the presence of flexural deflection of the model

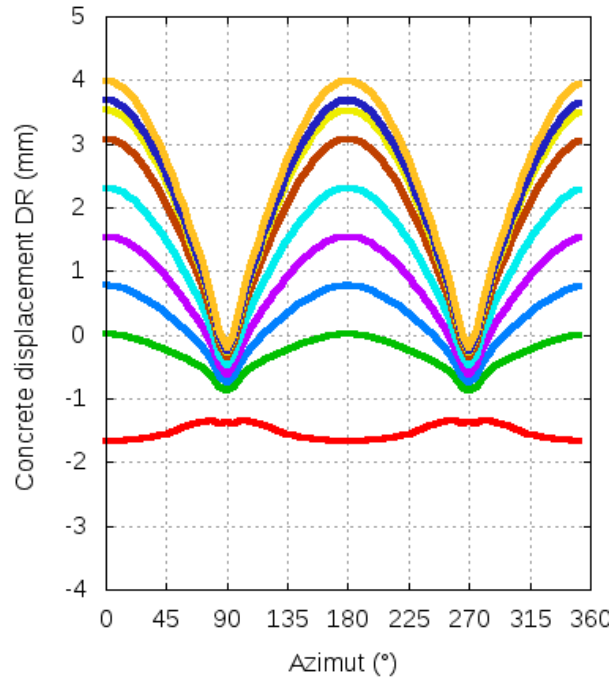
### Radial displacement (z = H/2, external face)



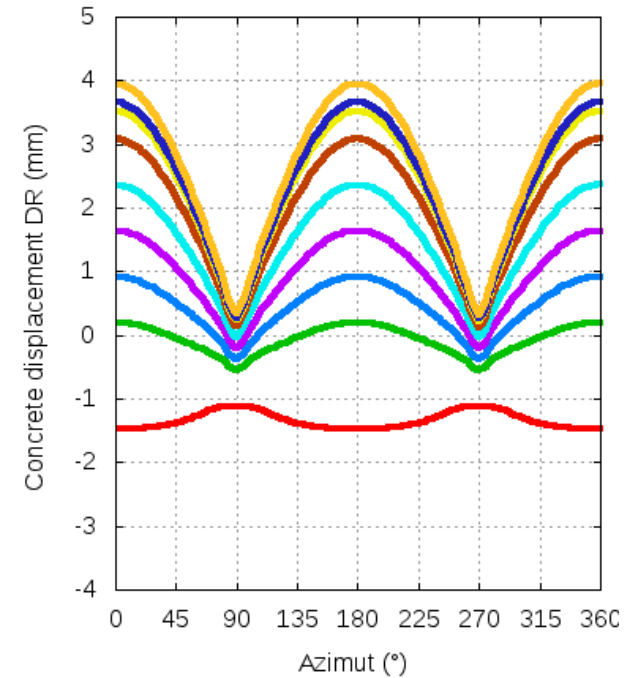
Coarse linear meshing



Coarse quadratic meshing



Refined linear meshing



# Sensitivity analyses: mesh element type

*Grouted ducts – Linear elastic analysis*

Mesh discretisation has a little effect on hoop stress.

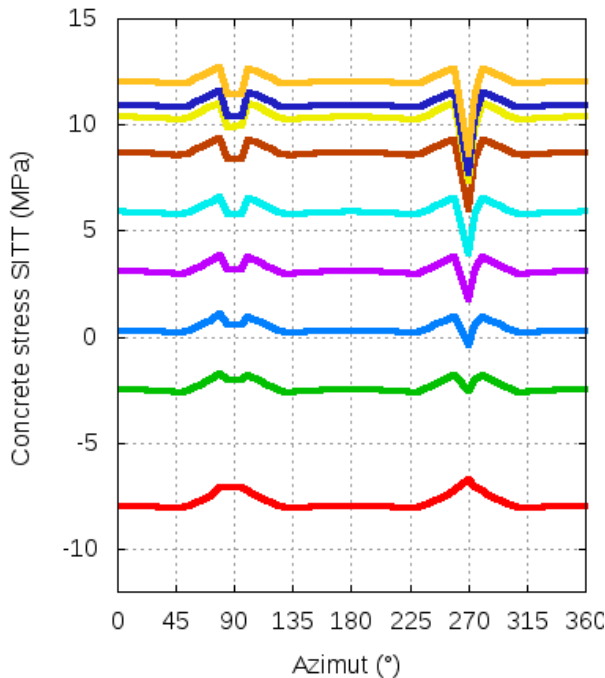
Globally, refined mesh produces lower stresses.

Locally there are slight differences between all cases.

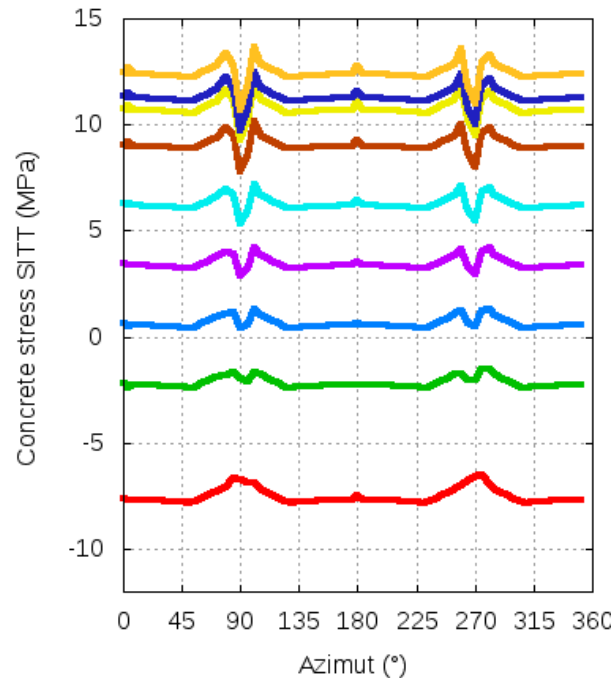
**Concrete hoop stress**  
(z = H/2, mid section)

- P = 0.0 MPa (0.0 Pd) —
- P = 0.4 MPa (1.0 Pd) —
- P = 0.6 MPa (1.5 Pd) —
- P = 0.8 MPa (2.0 Pd) —
- P = 1.0 MPa (2.5 Pd) —
- P = 1.2 MPa (3.0 Pd) —
- P = 1.3 MPa (3.3 Pd) —
- P = 1.3 MPa (3.4 Pd) —
- P = 1.4 MPa (3.6 Pd) —

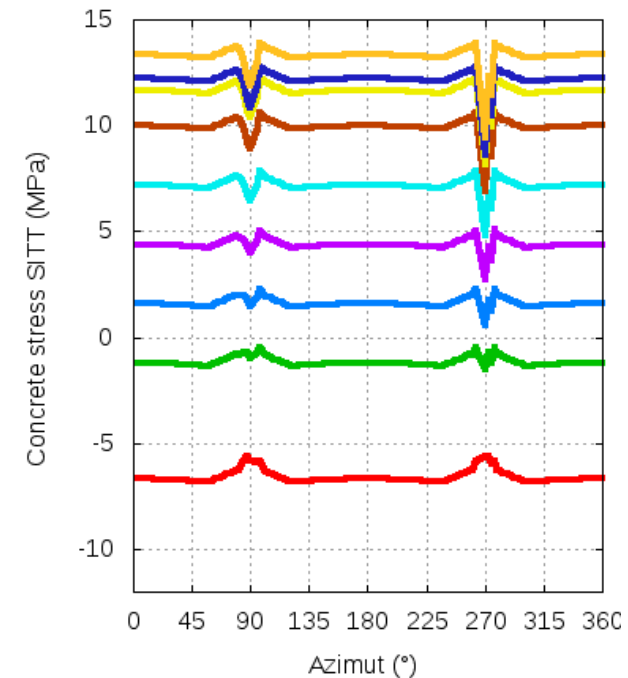
Coarse linear meshing



Coarse quadratic meshing



Refined linear meshing

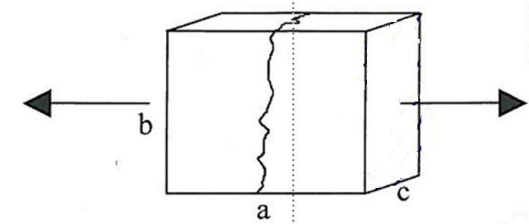


# Sensitivity analyses: $G_f$ fracture energy

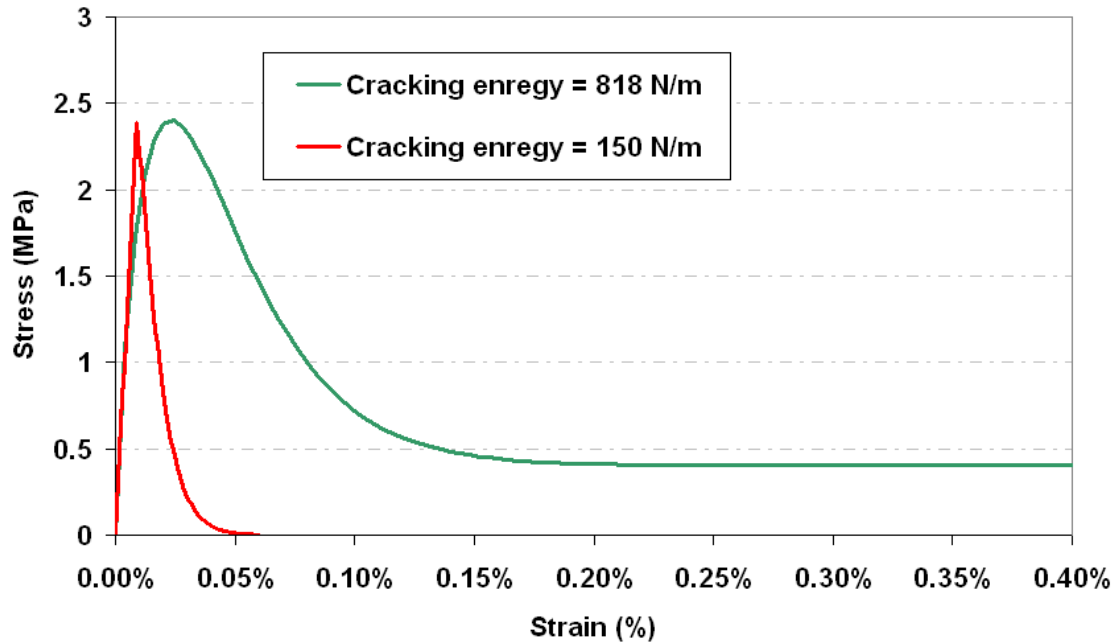
*UngROUTED ducts*

**Cracking energy effect (CEE): Cracking energy. Non-GROUTED duct**

Energy needed to fracture a concrete bloc =  $G_f \times b \times c$



**Concrete behavior: Cracking energy 818 N/m vs 150 N/m**





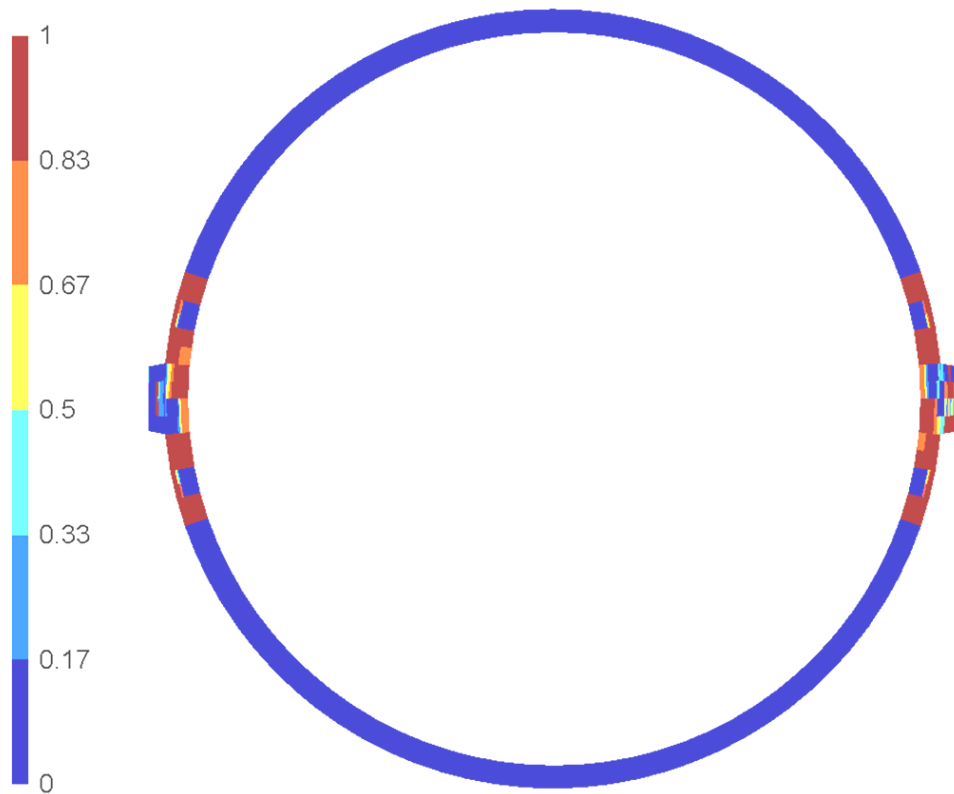
# Sensitivity analyses: $G_f$ fracture energy

*UngROUTED ducts*

**Cracking energy effect (CEE): Cracking energy. Non-GROUTED duct**

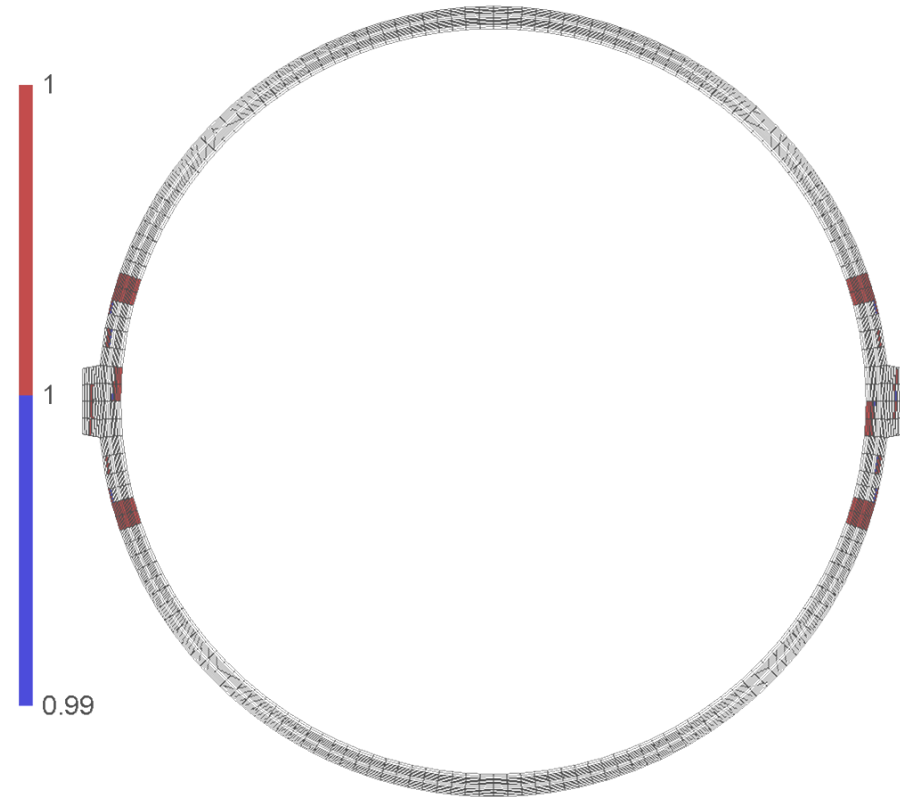
**Damage index D at  $1.7 \times P_d$  ( $G_f = 150 \text{ j/m}^2$ )**

At  $P = 1.7 P_d$  full thickness is damaged ( $D = 1$ ) so it can not be loaded any more



**A1**

$0 < D < 1$



**25**

**ZOOM :**  
 $0.99 < D < 1$

# Sensitivity analyses: fracture energy effect

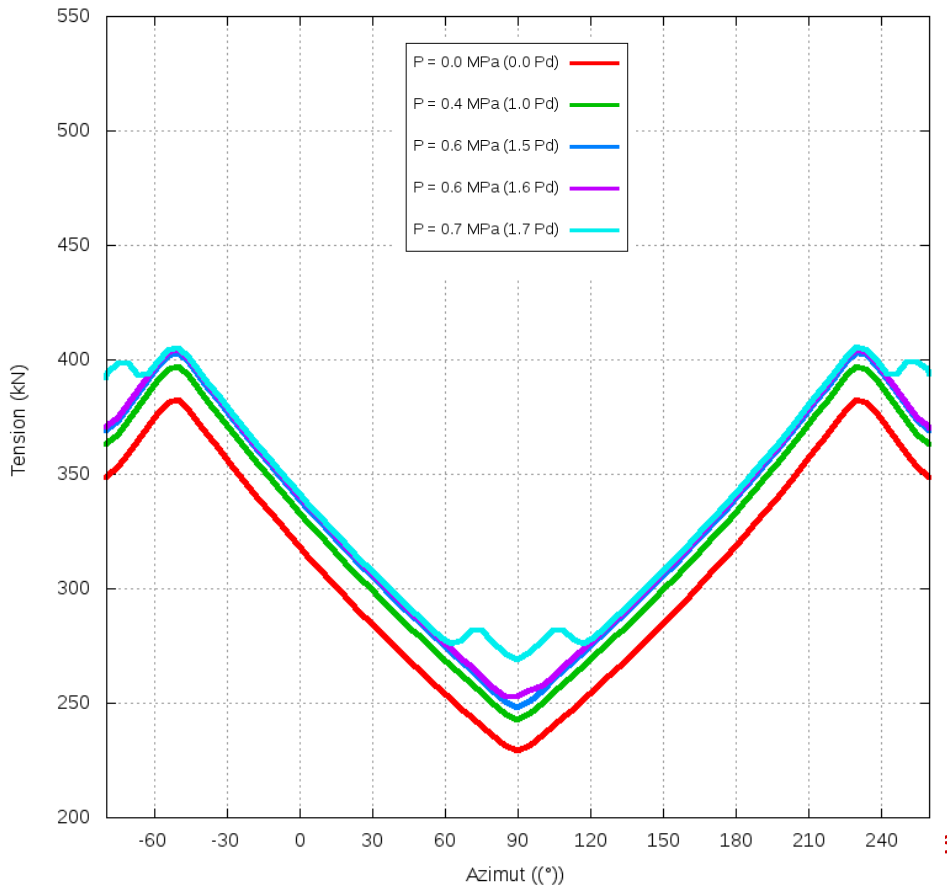
## UngROUTED ducts – Nonlinear analysis

Tendon tension

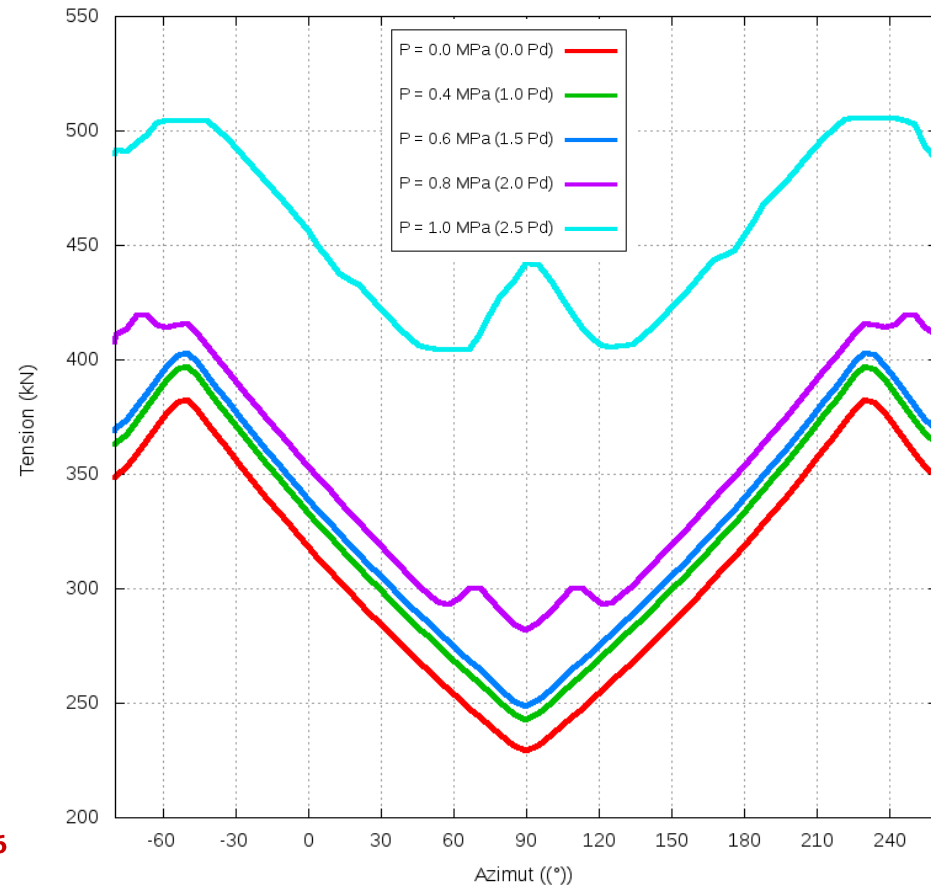
Low  $G_f$  produces early damaging. Thus early stress concentration in tendons.

Low  $G_f$  raised more difficulties to pursuit calculation (reasons are under investigation). While high  $G_f$  allow to reach higher values.

Concrete M150

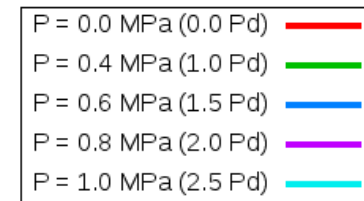
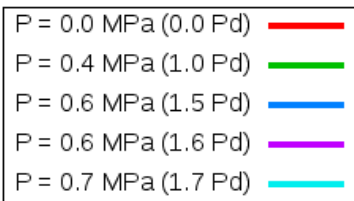


Concrete M818

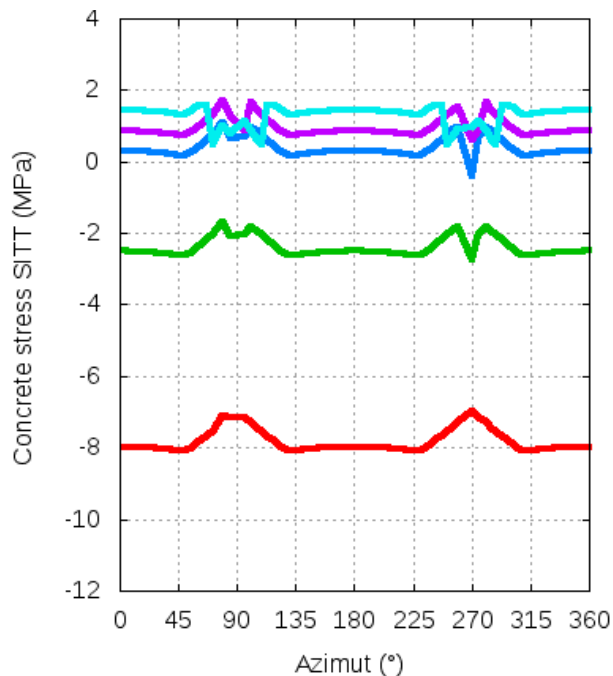


## Cracking energy effect (CEE): Concrete hoop stress ( $z = H/2$ , half thickness). Non-Gouted duct

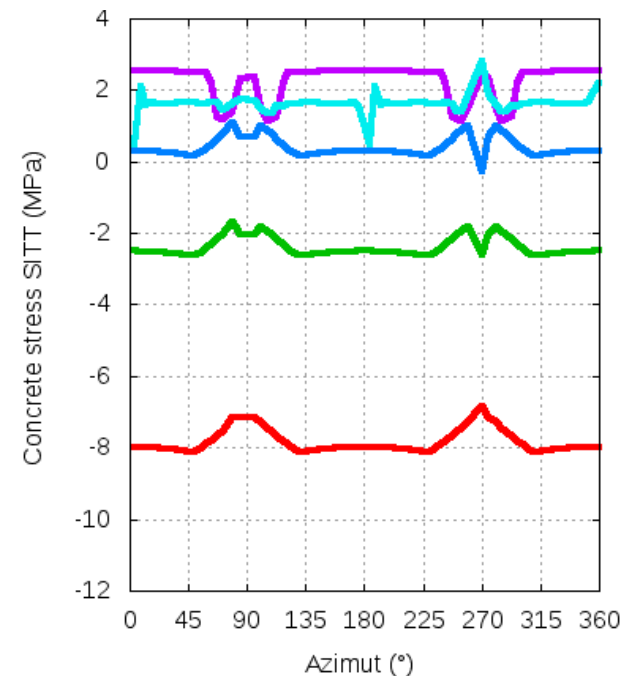
1. Avec l'énergie de fissuration plus basse (150 N/m) à  $P = 1.5$  Pd on est proche du pic de contrainte en traction (2.4 MPa) et la partie post-pic de la loi de comportement a une descente brutale ce qui fait que à partir de cette pression l'anneau s'endommage brutalement et le calcul ne converge plus .
2. Avec l'énergie de fissuration plus élevée, à  $P = 1.5$  Pd on est loin du pic en traction.
3. Avec l'énergie de fissuration de (150 N/m) on a un comportement plus réaliste mais le fait de n'avoir pas un résidu de résistance au béton complique la convergence du calcul



Non linear (M150) Non-gouted duct



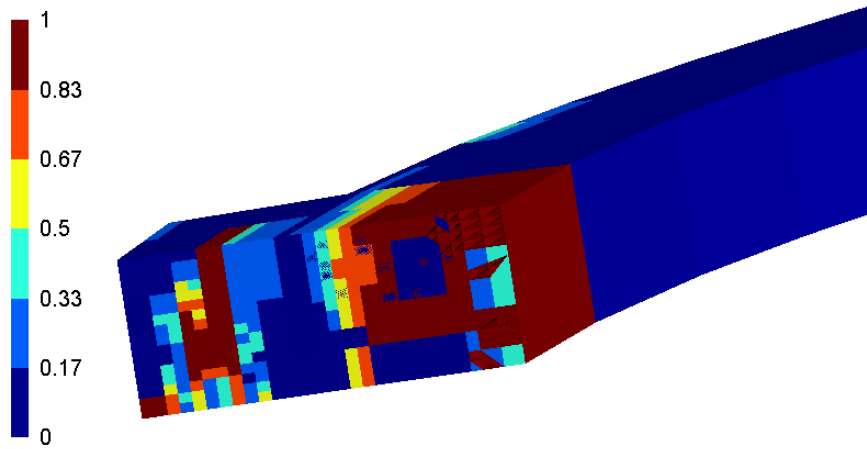
Non linear (M818) Non-gouted duct



## Cracking energy effect (CEE): Concrete damage. Non-Grouted duct

1. Quand l'énergie de fissuration es plus basse (gauche), l'anneau commence à endommager plus tôt (pour la même pression  $P = 1.6Pd$  on voit un endommagement plus élevé pour MM150)

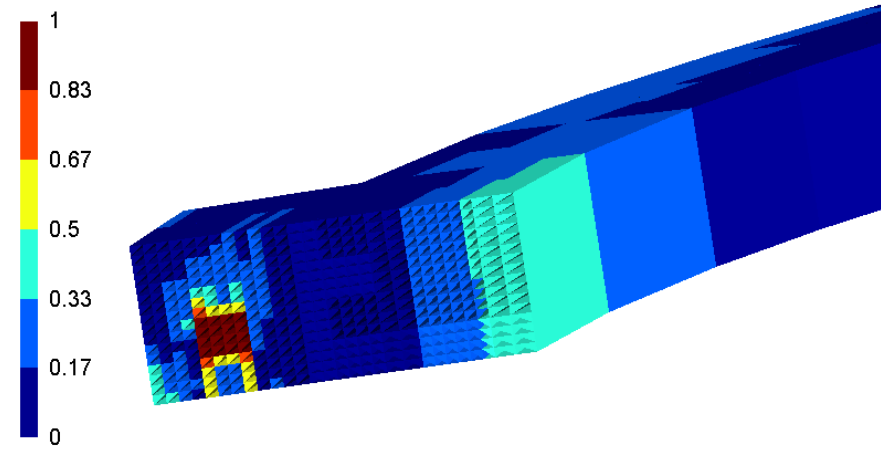
Non linear (M150) Non-grouted duct



Damages at  $P = 1.6 Pd$

Z  
Y X

Non linear (M818) Non-grouted duct



Damages at  $P = 1.6 Pd$

Z  
Y X

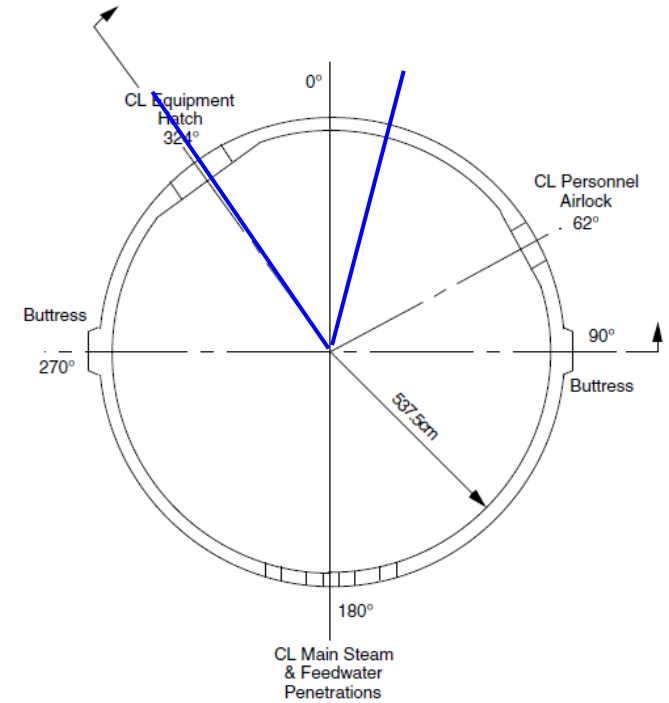
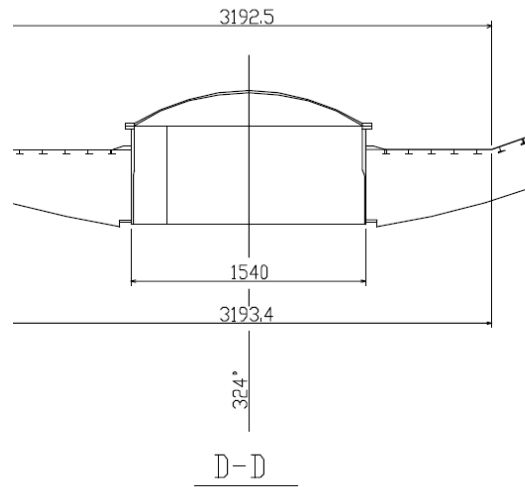
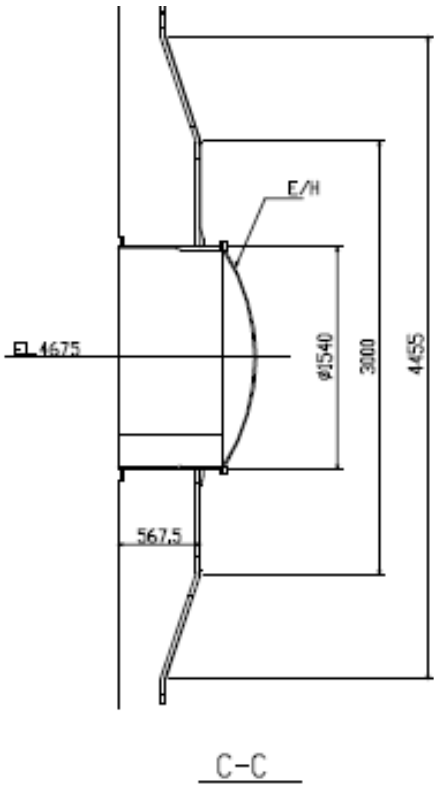
# Model 2

## SUMMARY

---

- **Description of equipment hatch geometry**
- **Modeling assumptions and phenomenological models**
- **Description of liner tearing criteria used**
- Deformed shape
- Liner seals state at  $p = 0$  (prestress applied),  $p = 1.0$  pd

# Model geometrical description



From NUREG\_CR-6810-appendices.pdf (A-28)

And PCCV-QCON-01

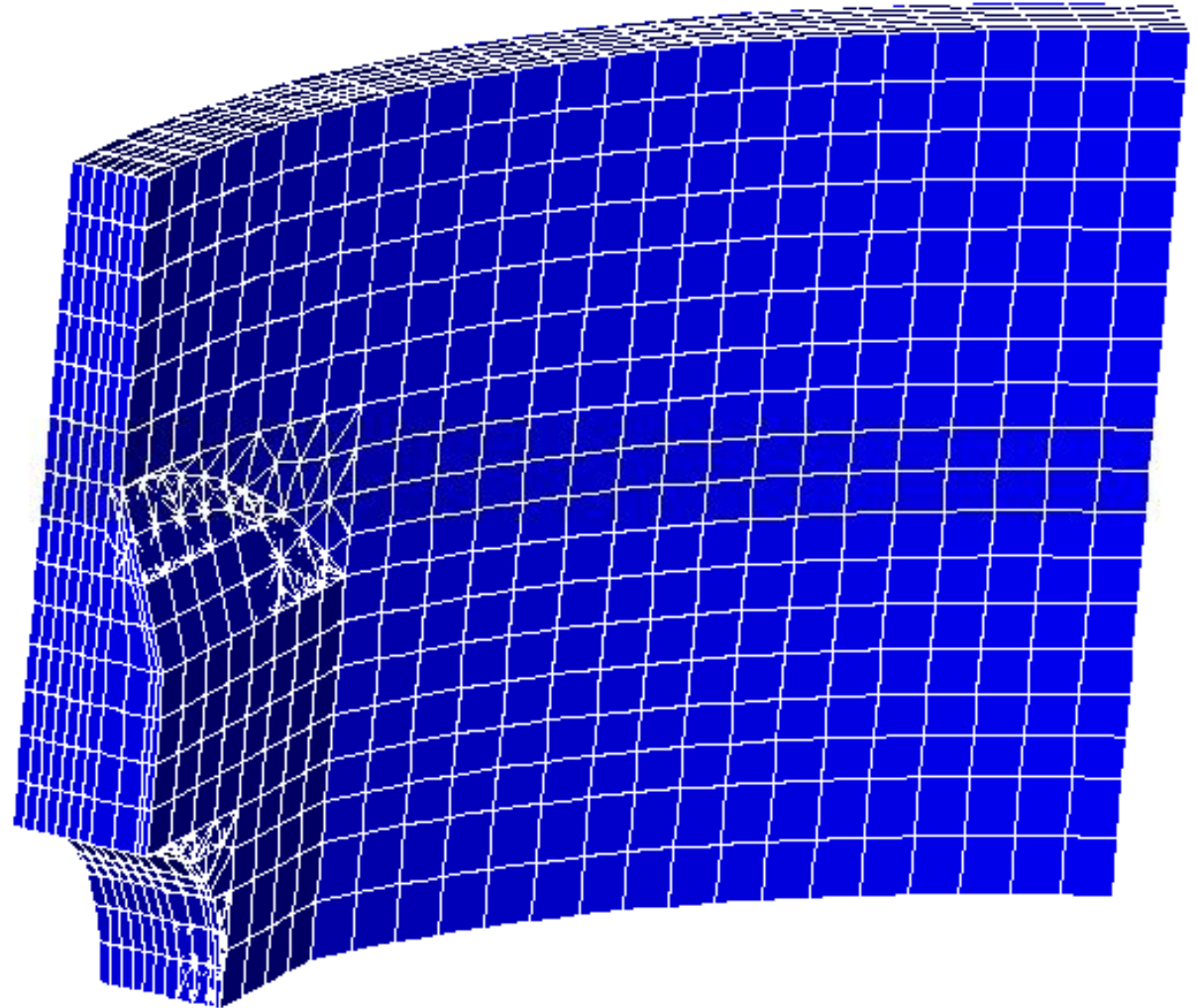
# Meshing: concrete

Solid element

Quadratic

Average size = anchorage spacing

Properties: same as for model 1



# Meshing: liner

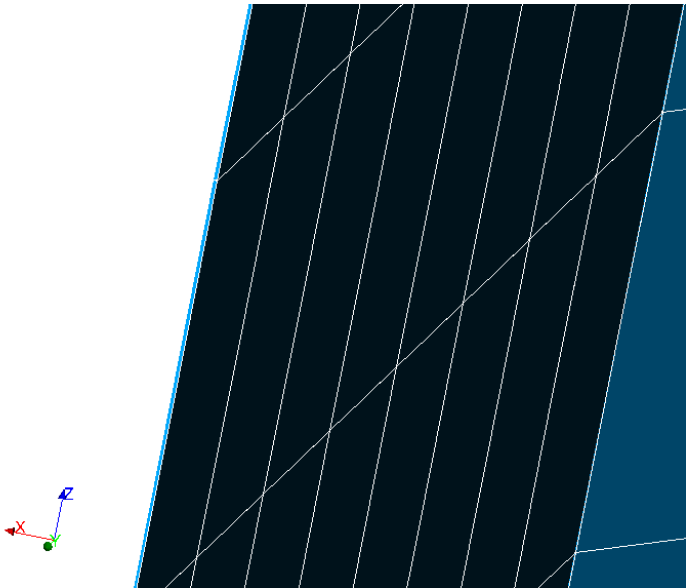
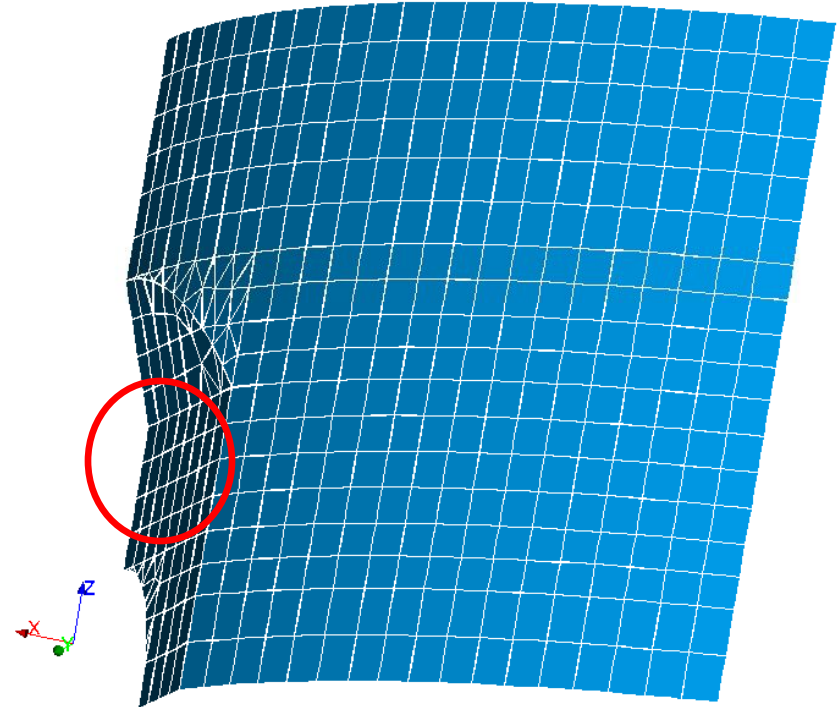
Solid element

Quadratic

Thickness 1.6mm

Liner perfectly bonded with concrete at nodes except at seal lines (same  $U_r$ )

Properties: same as for model 1





# Meshing: seal

Cohesive zone model elements

Hexa-CZE (zero volume element)

Quadratic number of nodes with special shape function

Liner / concrete interface: same radial displacement

$E = 223 \text{ GPa}$

$\nu = 0$

$\rho = 7\,850 \text{ kg/m}^3$

$GC = 130 \text{ MPa}\cdot\mu\text{m}$

$SIGM\_C = 498 \text{ MPa}$

$COEF\_EXTR = 0.$

$COEF\_PLAS = 0.5$

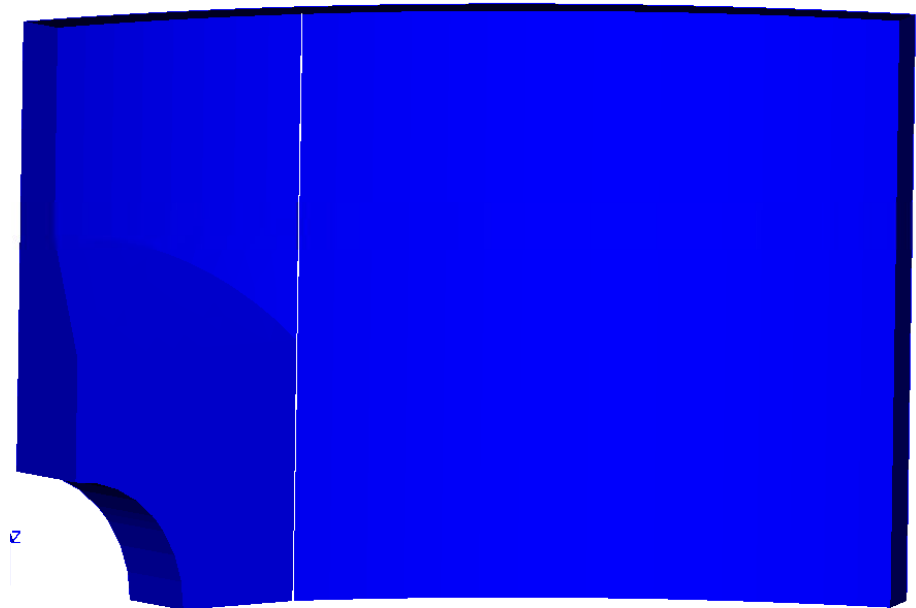
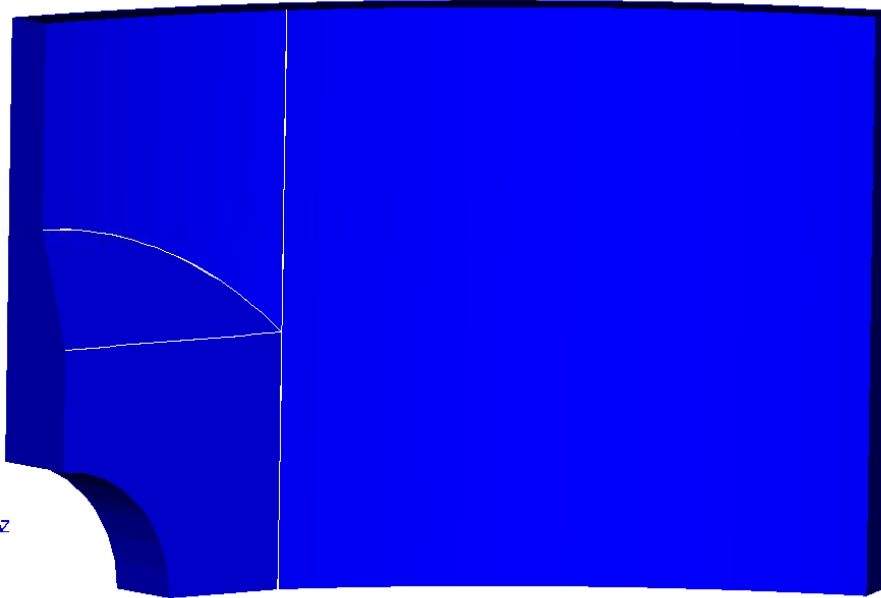
Surface energy density

Failure stress

Shape of stress vs jump displacement curve - Mode I crack opening

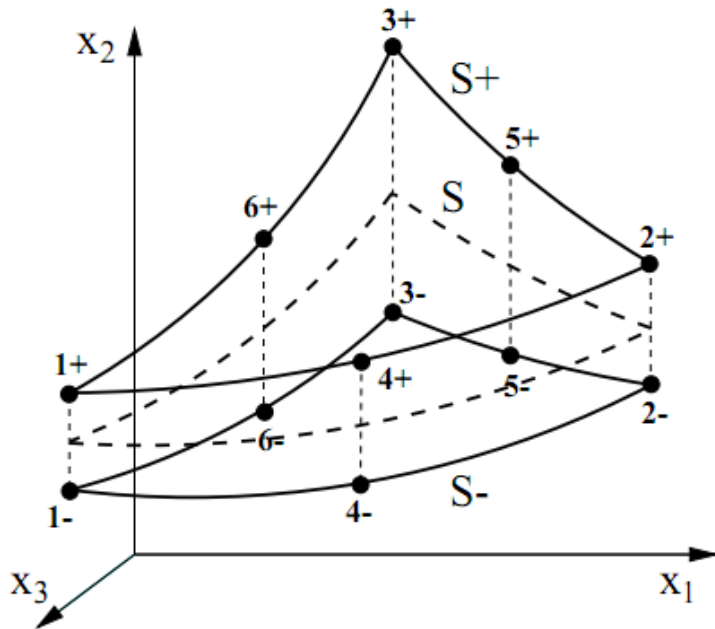
*Seals surrounding the E/H*

*One vertical seal*

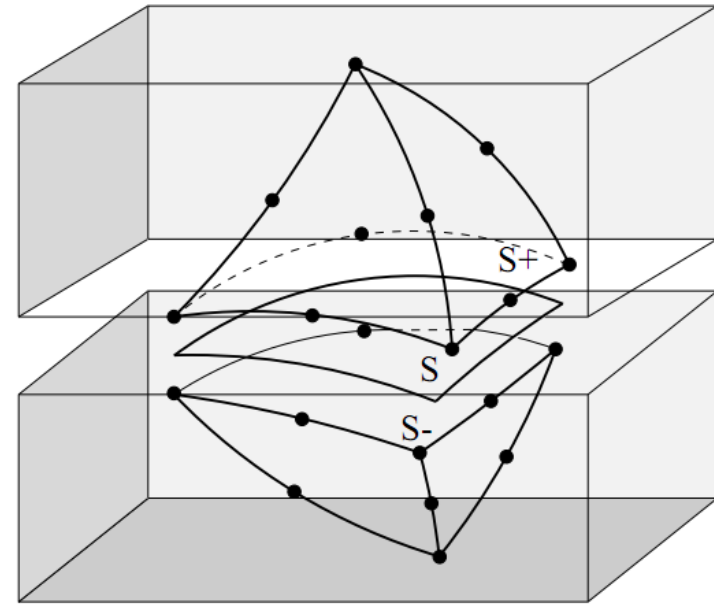


# Cohesive zone model elements

Example of tetra-cohesive zone elements. In model 2 we use hexa-CZE.



Geometry of a cohesive element  
 $S^+$  and  $S^-$  are coincident in initial state



Assembly of a cohesive element with adjacent liner elements

# Liner tearing constitutive model

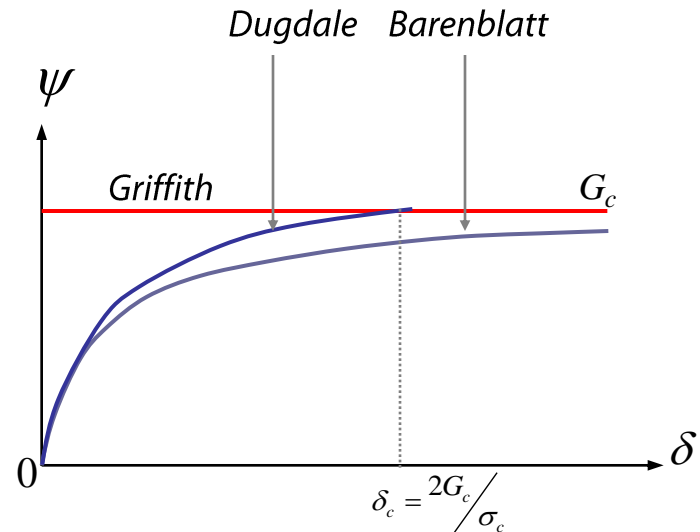
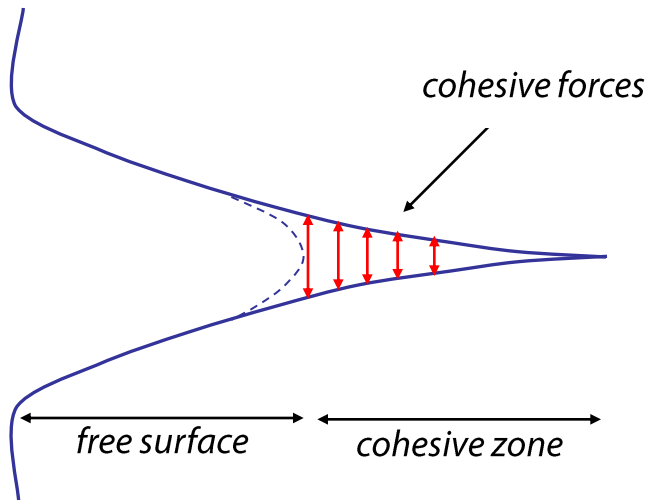
Known as "CZM", Cohesive zone model

## Features :

- Energy formulation for failure: minimization of the total energy

$$E_T = \Phi + \Psi - W^{ext}$$

(deformation, external forces, surface)

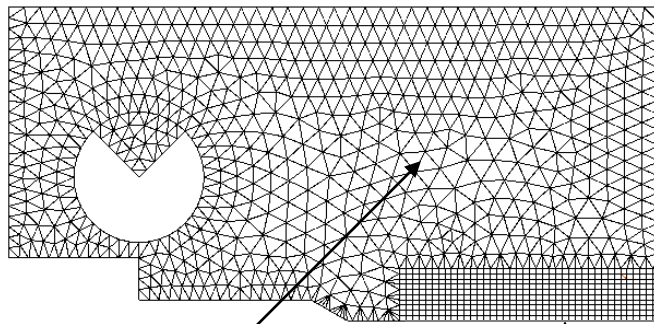
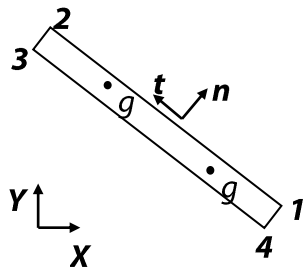


Surface energy density vs. jump displacement

# Liner tearing constitutive model

Known as "CZM", Cohesive zone model

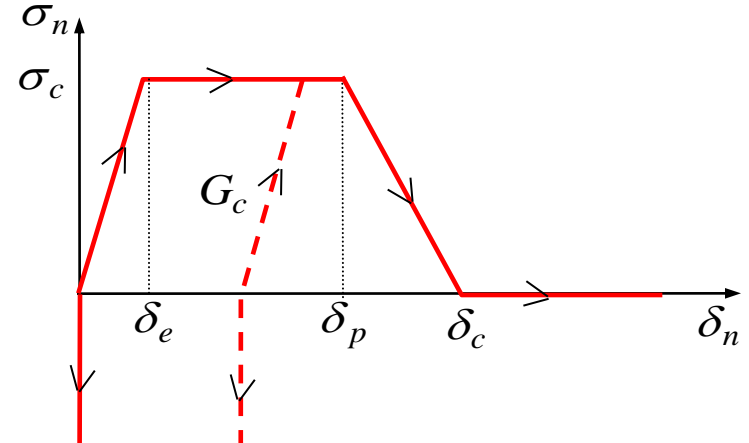
Interface elements introduced along the « supposed » crack path



Sound material  
(elastic or elastoplastic)

Interface elements

The cohesive law for ductile fracture

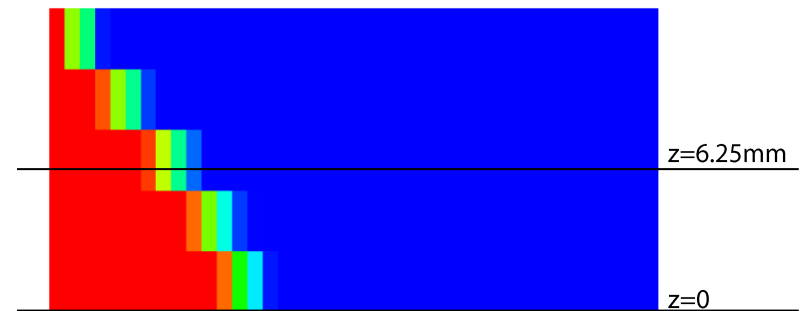
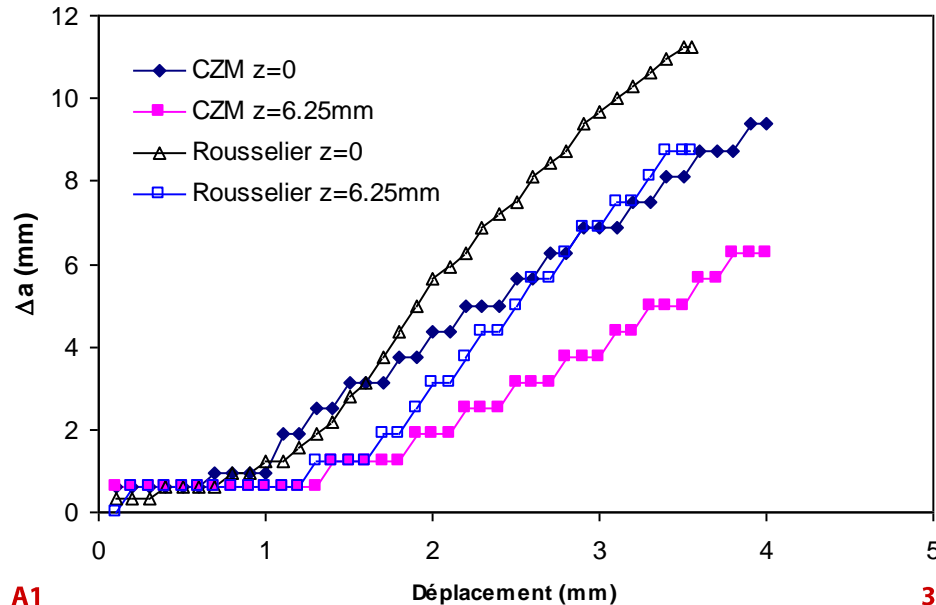
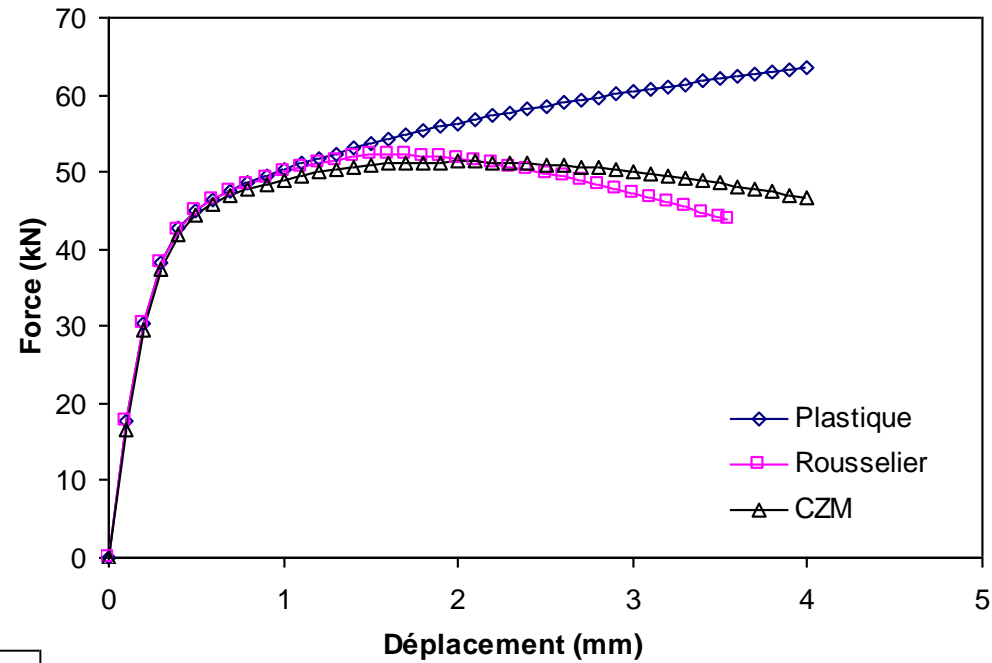
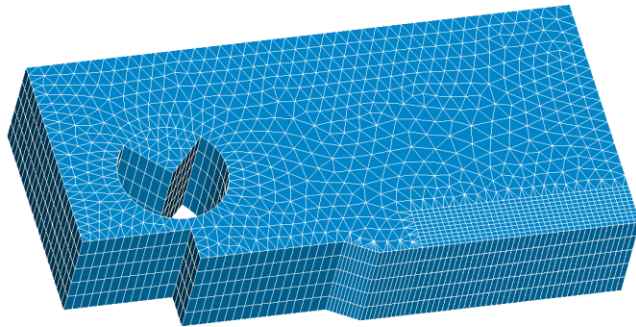


$$\sigma_n(\delta_n) = \sigma_c \begin{cases} \frac{\delta_n}{\delta_e} & \text{if } \delta_n \leq \delta_e \\ 1 & \text{if } \delta_e < \delta_n < \delta_p \\ \frac{\delta_c - \delta_n}{\delta_c - \delta_p} & \text{if } \delta_p \leq \delta_n < \delta_c \\ 0 & \text{if } \delta_n \geq \delta_c \end{cases}$$

$$\delta_c = 2G_c / \sigma_c + \delta_e - \delta_p \quad \delta_e \leq \delta_p < \delta_c$$

# Liner tearing constitutive model

Known as "CZM", Cohesive zone model  
Test case





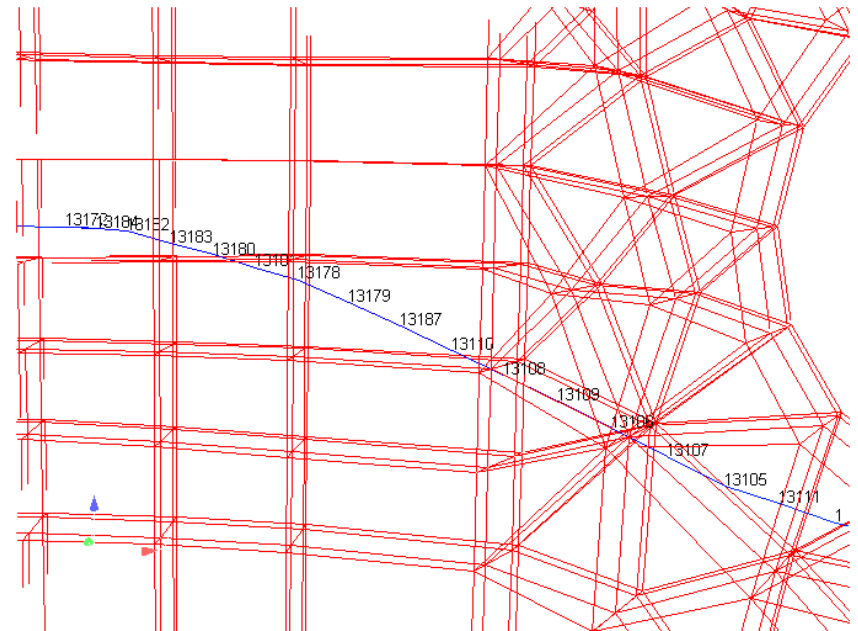


# Meshing: tendons

Truss elements

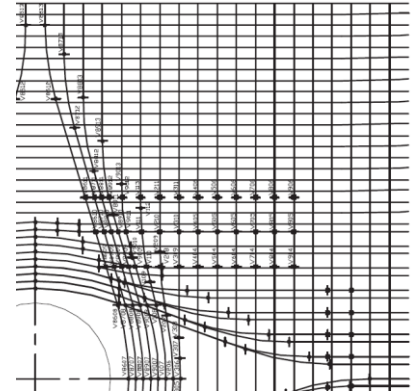
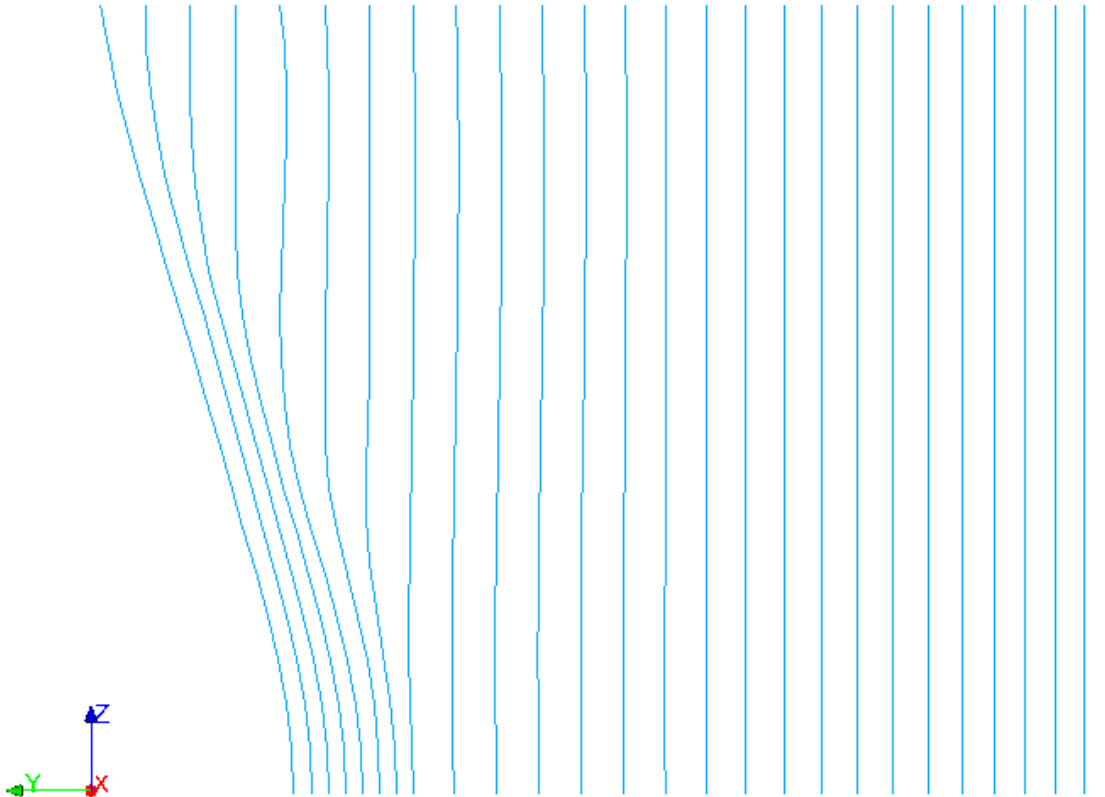
Tendon / concrete interface:

- perfectly bonded in vertical and radial directions
- friction elements between tendon / concrete elements



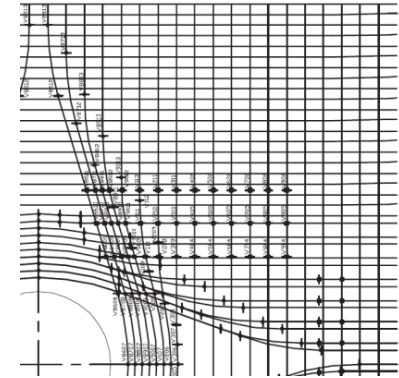
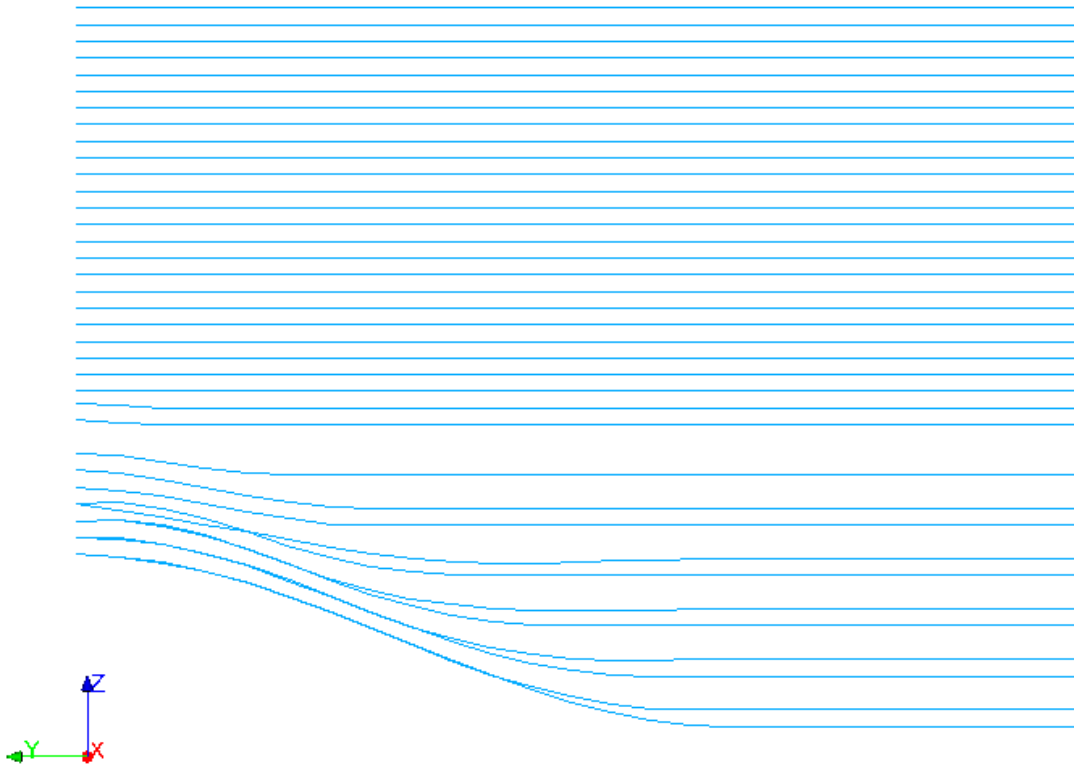


# Meshing: tendons



*Actual vertical tendons position and inflections  
(from PCCV-QCON-07 and PCCV-QCON-08)*

# Meshing: tendons



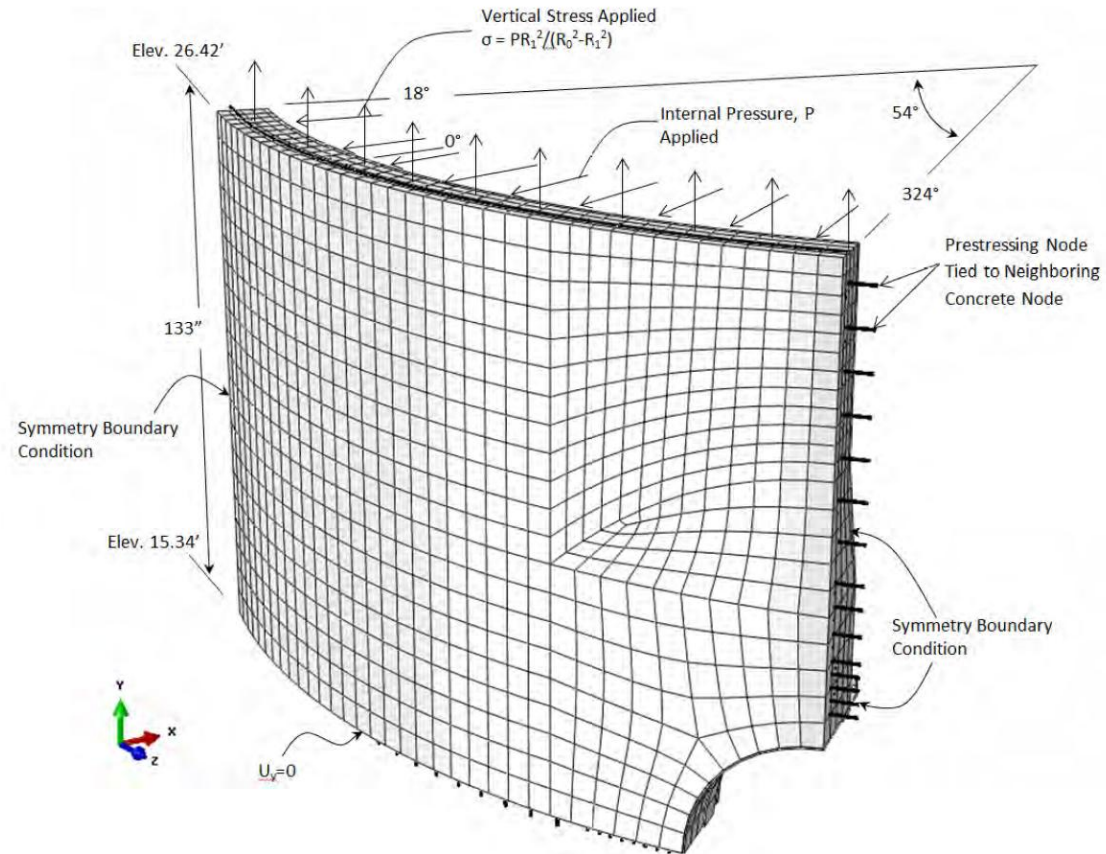
*Actual horizontal tendons position and inflections (from PCCV-QCON-07 and PCCV-QCON-08)*

# Boundary conditions

Lateral surface: rotation constrained to zero

Bottom surface: no vertical displacement

Top surface: vertical stress applied (same as model 1)



# Preliminary analyses

Numerical and implementation of CZM elements checks (recently implemented in Code\_Aster)

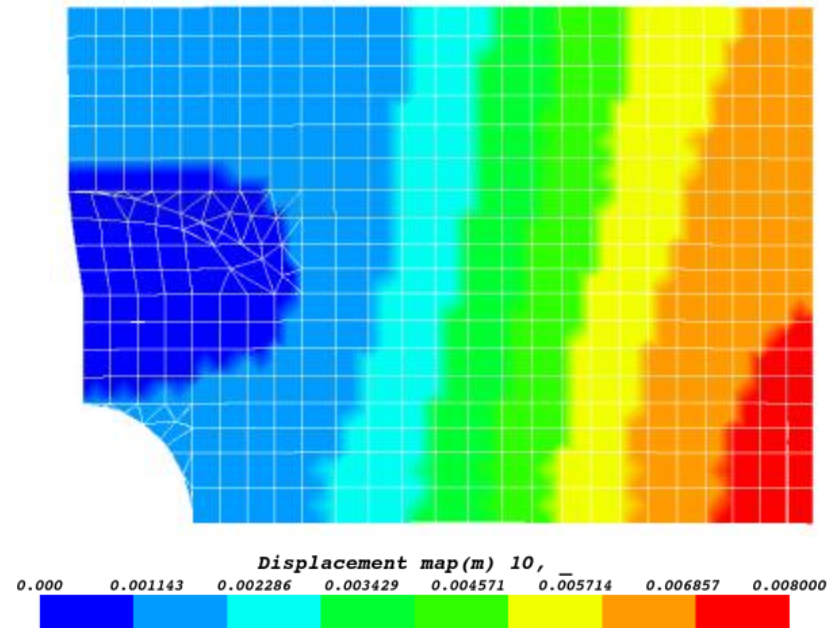
Test analysis 1:

- Concrete remains elastic for tests
- Only one vertical seal
- Prestressing= initial tension set to mean value of tendons A and B close to the E/H
- Increase of internal pressure from 0 up to  $3xP_d$  in 30 uniform load steps

## Test 1: displacement map of liner at $3xP_d$ (elastic concrete)

Maximum radial displacement of 7.5mm (half of nonlinear forecasts)

Embossment stiffer than current zone



# Preliminary analyses

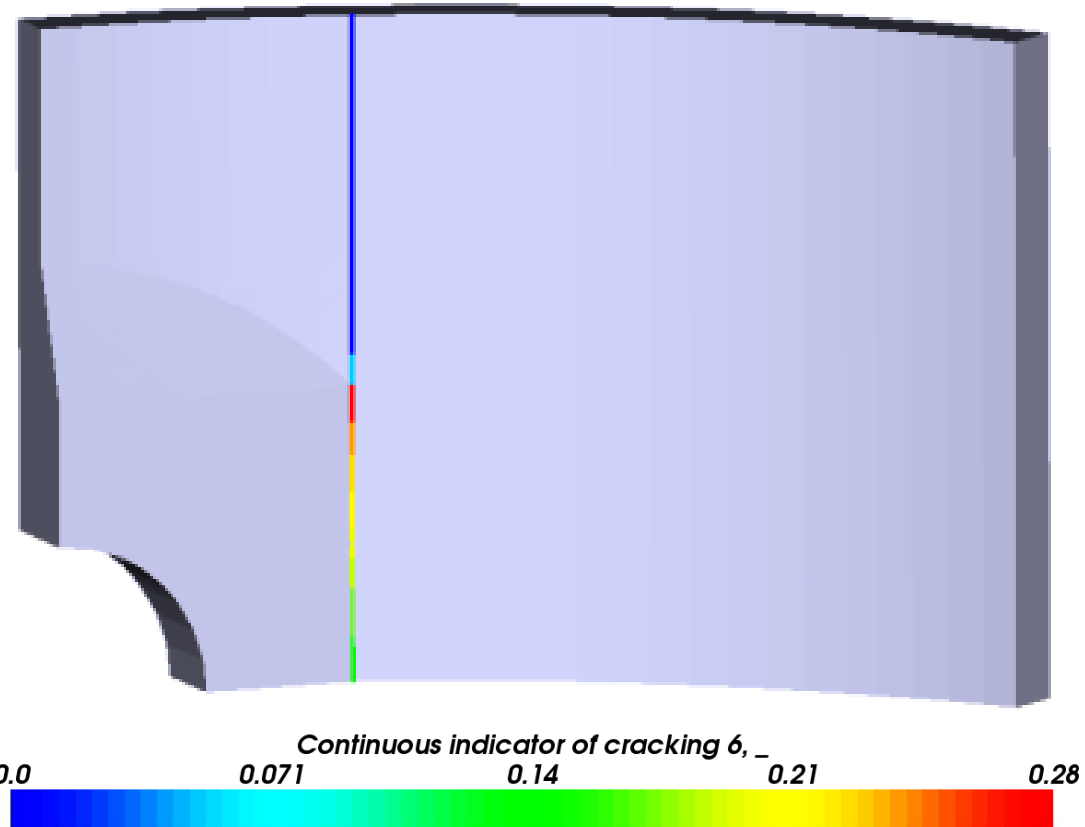
## Test 1: liner tearing within seals (fracture indicator)

Initiation of crack at geometrical and stiffness discontinuity (stress concentration)

Relatively stable calculation

Mesh to refined

Addition numerical implementations needed allowing to simultaneously use both CZM and nonlinear concrete constitutive models



0= sound element

0.5= damaged

1= fractured