



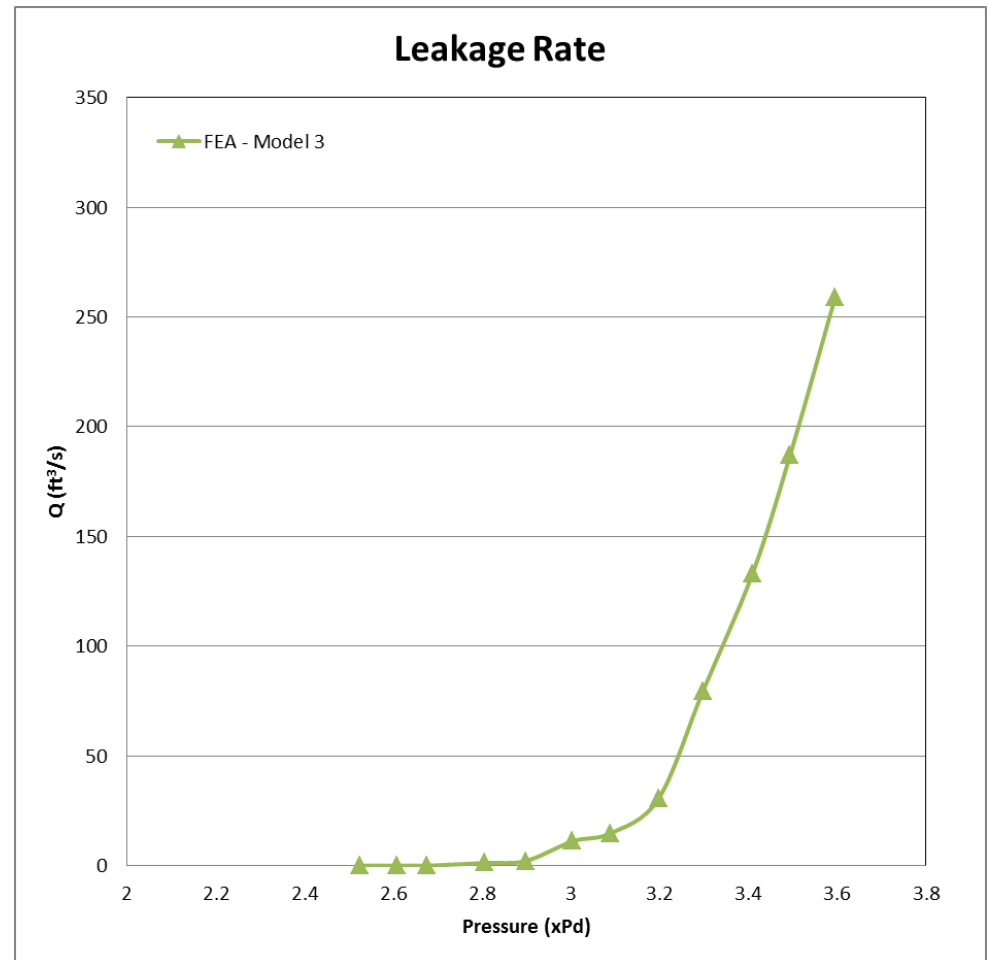
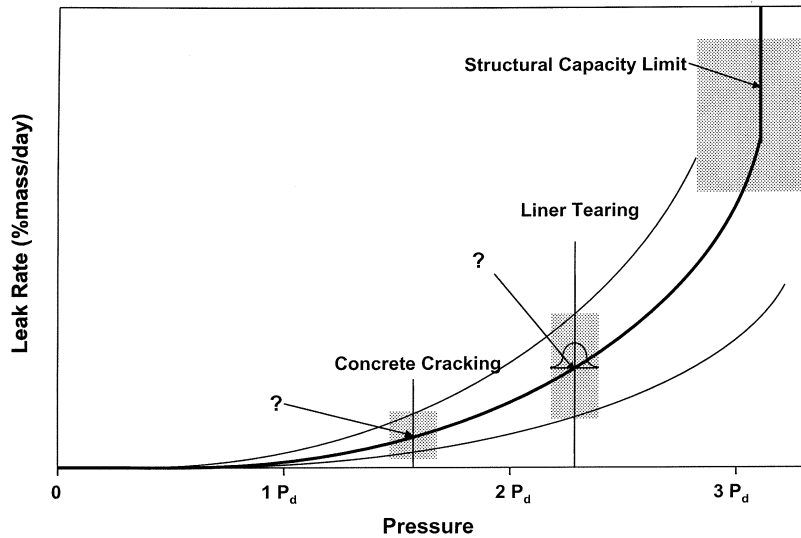
# Standard Problem Exercise No. 3

## Transition to Probabilistic Space

March 27-29, 2012

**Herman Graves**  
**Madhumita Sircar**  
**Lili Akin**  
**Robert Dameron**  
**Christopher Jones**

# Pressure Versus Leak Rate





# Approaches to Assessing Uncertainty

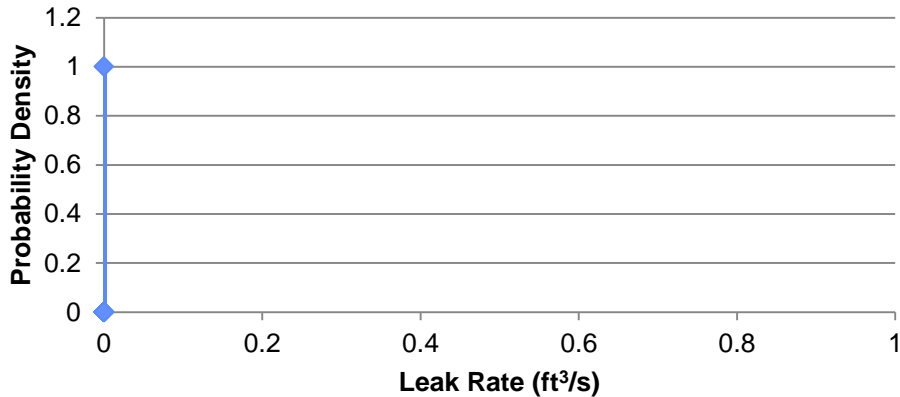
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- Start with global strain from FEA model
- Use Monte Carlo simulation to vary K in:
  - $\varepsilon_p = K B \varepsilon_{\text{global}}$
- Vary K using two different approaches
  - Multiply by a random number between 0.8 and 1.2
  - Multiply by a random number with normal distribution between 0.8 and 1.2
- Complete 2148 trials for each method
- Use this peak strain to calculate tearing and then leakage using the Rizkalla equation



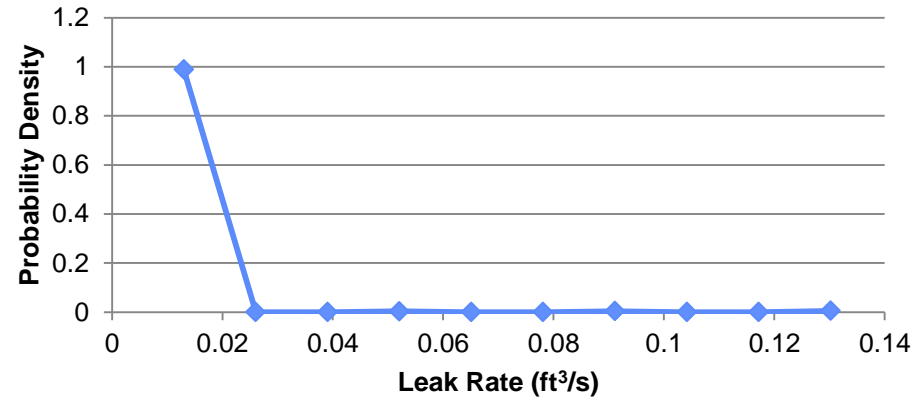
# Comparison of Probability Densities at $2.5xP_d$

## Probability of Leak Rate at $2.5xP_d$



**Random Number**

## Probability of Leak Rate at $2.5xP_d$

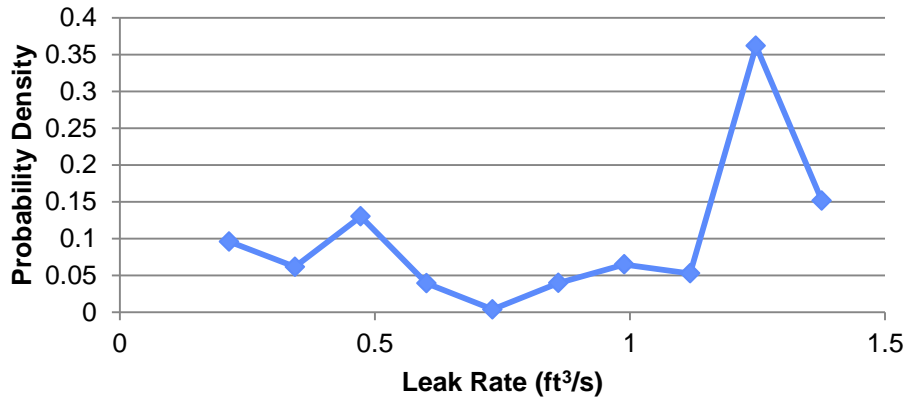


**Normal Distribution**



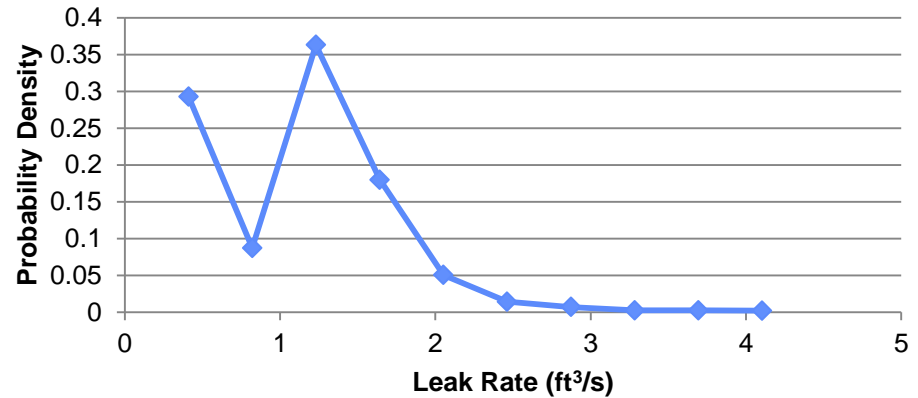
# Comparison of Probability Densities at $3.0xP_d$

## Probability of Leak Rate at $3.0xP_d$



**Random Number**

## Probability of Leak Rate at $3.0xP_d$

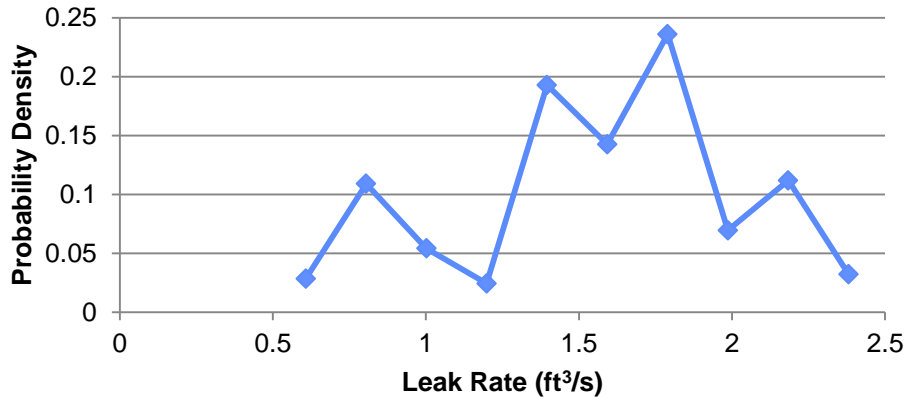


**Normal Distribution**



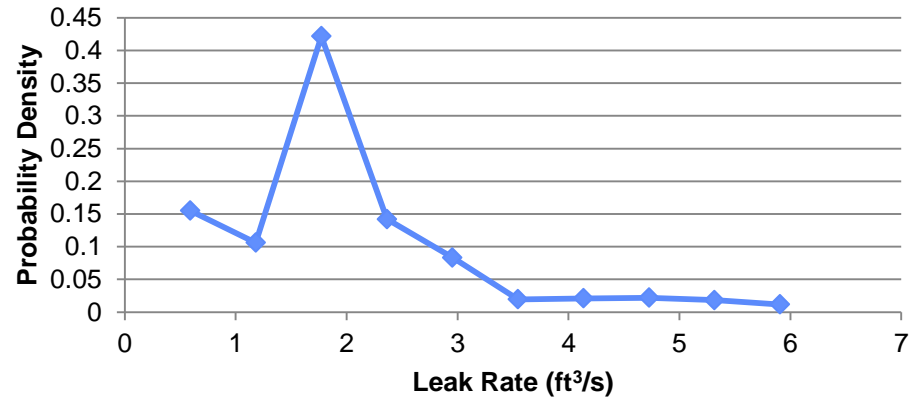
# Comparison of Probability Densities at $3.1xP_d$

## Probability of Leak Rate at $3.1xP_d$



**Random Number**

## Probability of Leak Rate at $3.1xP_d$

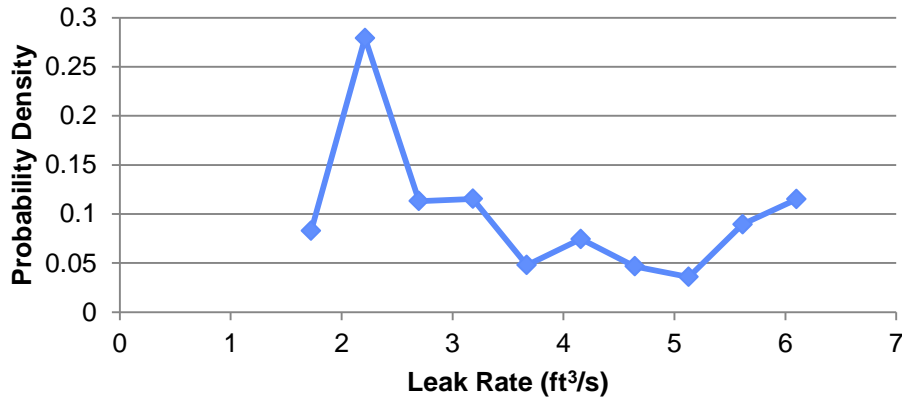


**Normal Distribution**



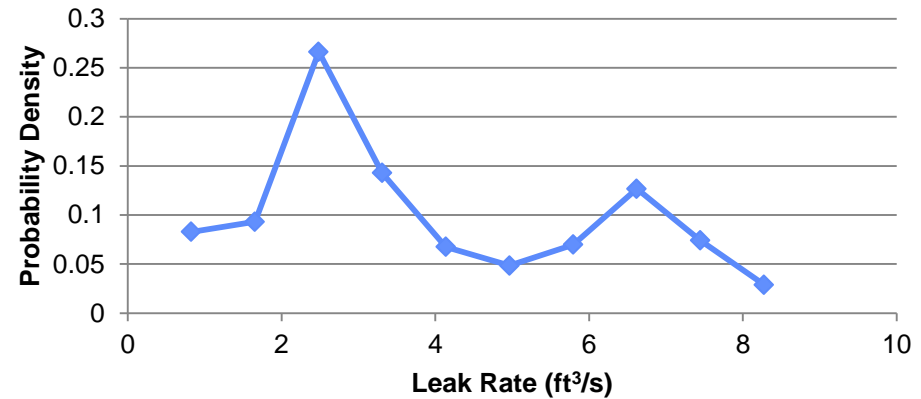
# Comparison of Probability Densities at $3.2xP_d$

## Probability of Leak Rate at $3.2xP_d$



**Random Number**

## Probability of Leak Rate at $3.2xP_d$

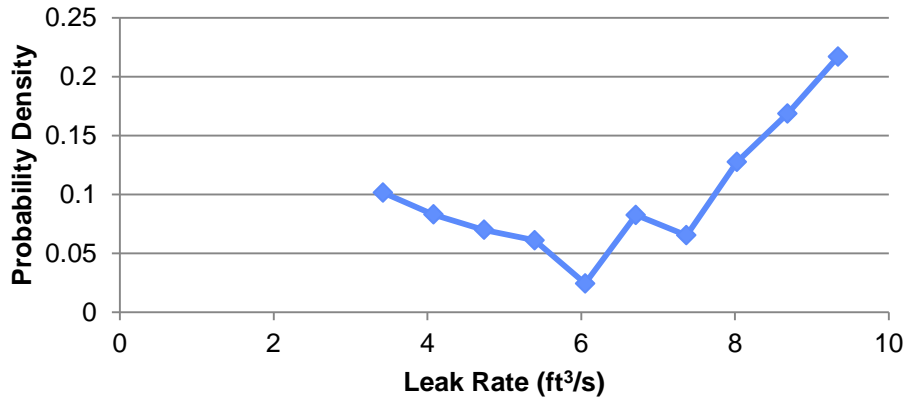


**Normal Distribution**



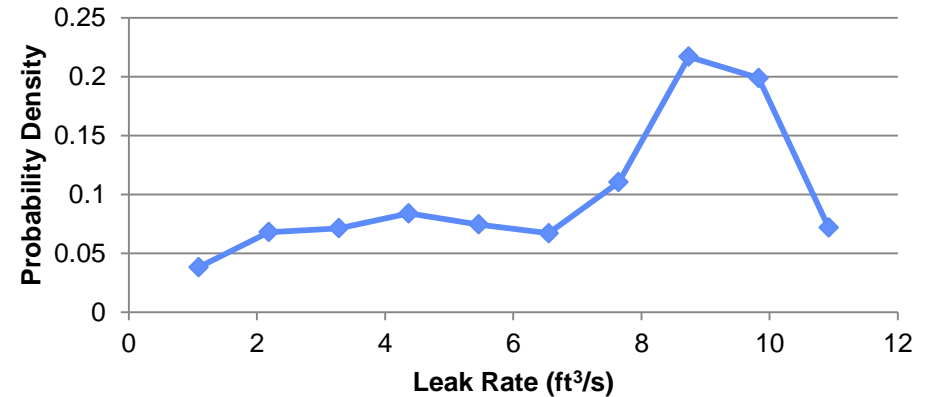
# Comparison of Probability Densities at $3.3xP_d$

## Probability of Leak Rate at $3.3xP_d$



**Random Number**

## Probability of Leak Rate at $3.3xP_d$



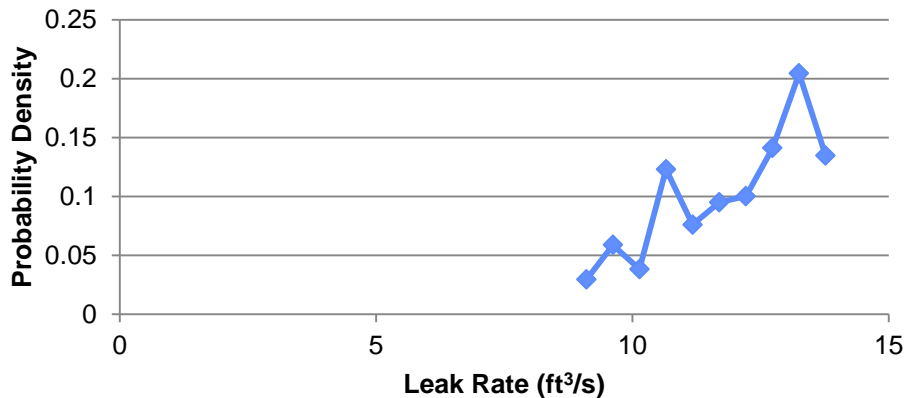
**Normal Distribution**





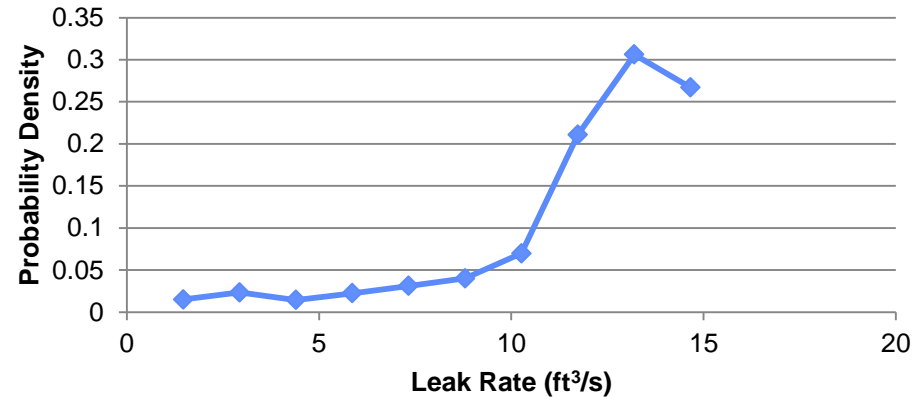
# Comparison of Probability Densities at $3.4xP_d$

## Probability of Leak Rate at $3.4xP_d$



**Random Number**

## Probability of Leak Rate at $3.4xP_d$

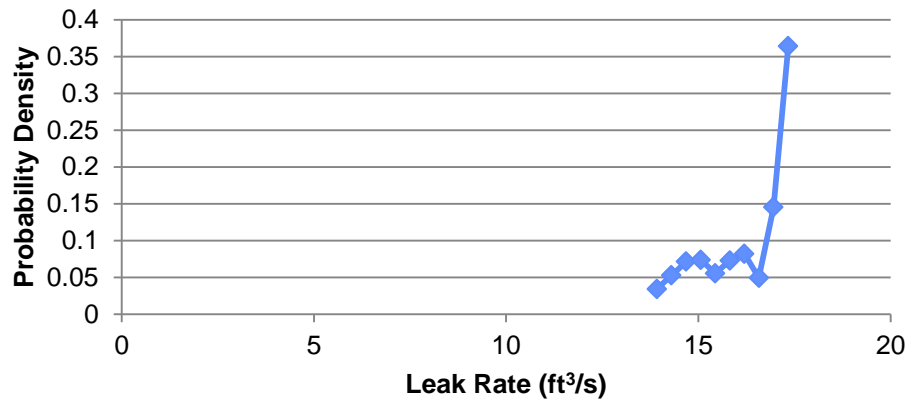


**Normal Distribution**



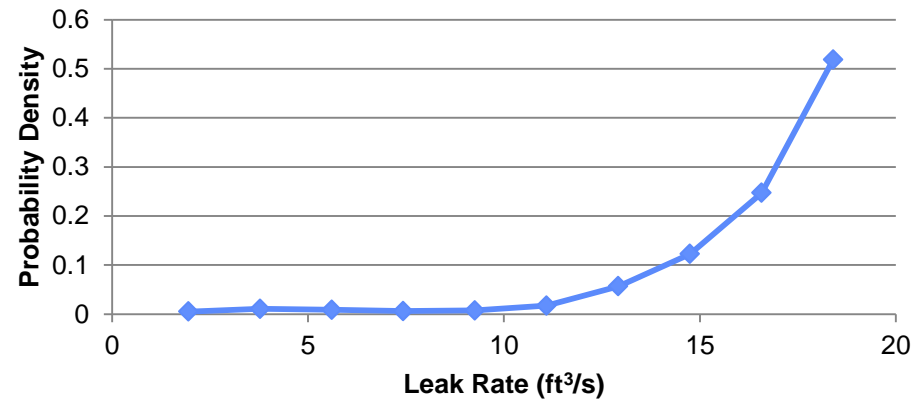
# Comparison of Probability Densities at $3.5xP_d$

## Probability of Leak Rate at $3.5xP_d$



**Random Number**

## Probability of Leak Rate at $3.5xP_d$

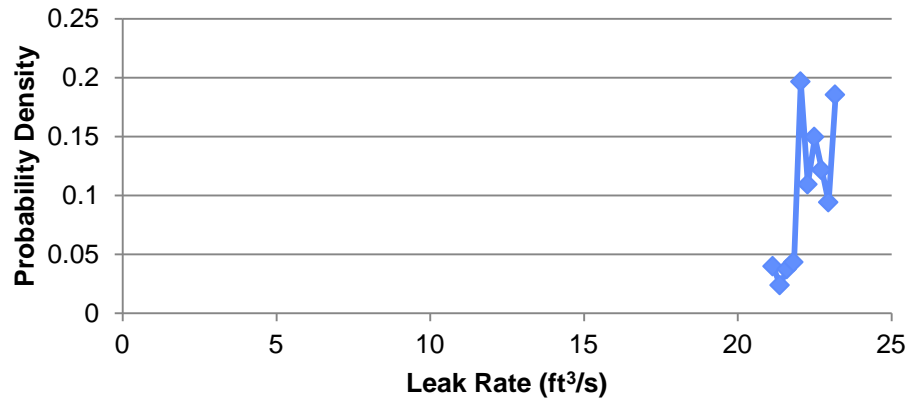


**Normal Distribution**



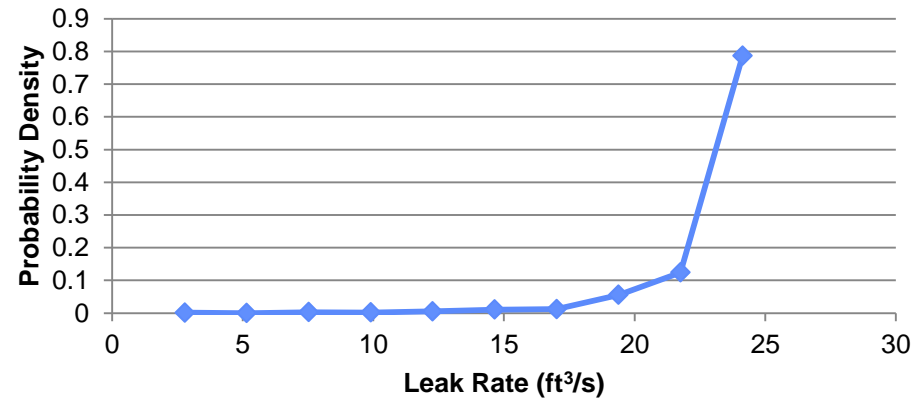
# Comparison of Probability Densities at $3.6xP_d$

## Probability of Leak Rate at $3.6xP_d$



**Random Number**

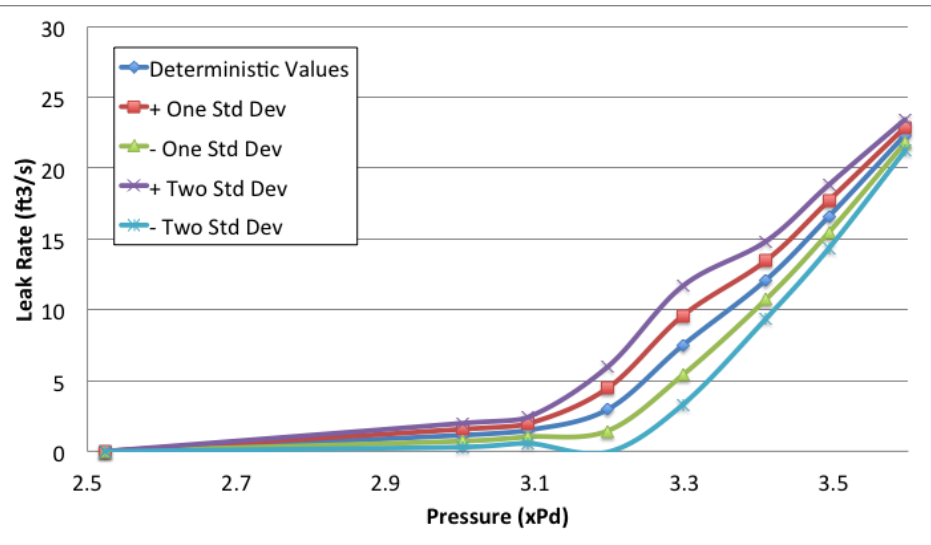
## Probability of Leak Rate at $3.6xP_d$



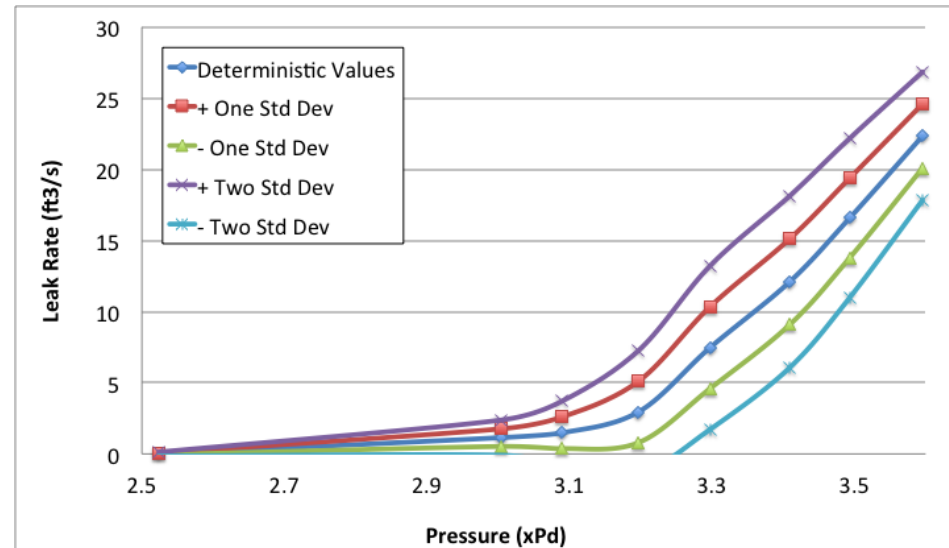
**Normal Distribution**



# Leak Rate Versus Pressure



Random Number



Normal Distribution





# Future Variations

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- **In Rizkalla equation, vary:**
  - L (wall thickness)
  - w (crack width)
  - B (crack height)
  - T (temperature for Case 1 and Case 2)
- **Apply Method Discussed Previously to Case 1 and 2 Data**