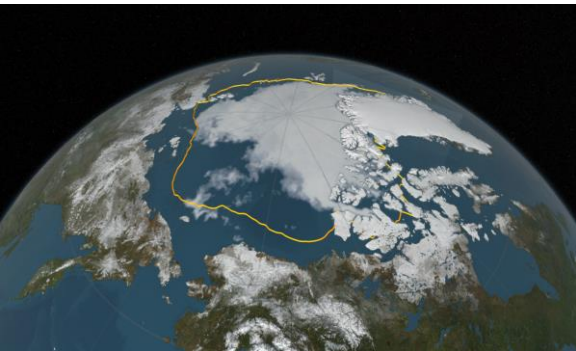


*Exceptional service in the national interest*



## Development of a novel thermo-mechanical model for simulating permafrost demise and Arctic coastal erosion

Jenn Frederick, Alejandro Mota, Irina Tezaur, Charles Choens, Diana Bull

Sandia National Laboratories, U.S.A.



Sandia National Laboratories is a multi-mission laboratory managed and operated by National Technology and Engineering Solutions of Sandia, LLC., a wholly owned subsidiary of Honeywell International, Inc., for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-NA0003525. SAND2019-7899 C

# Outline

- Motivation and background
- The Arctic Coastal Erosion (ACE) project
- Thermo-mechanical finite element model of permafrost
- Numerical results
- Summary
- Ongoing/future work

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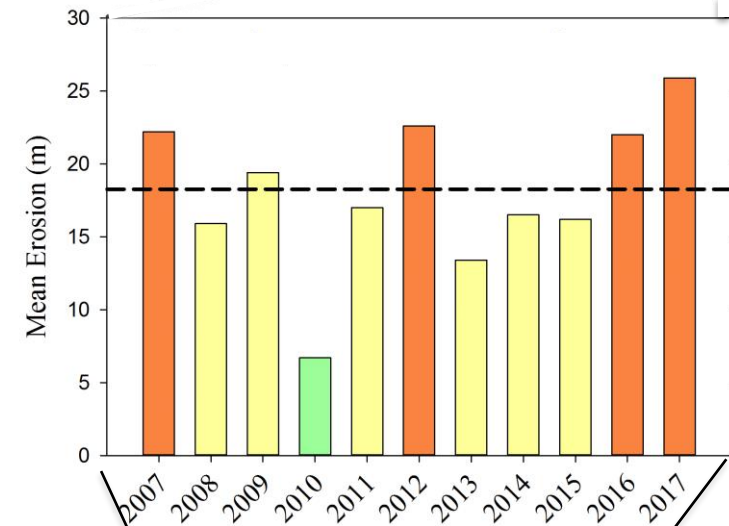
# Motivation

The Arctic is warming at **2-3 times** the rate of the rest of the globe resulting in **accelerated rates of coastal erosion!**

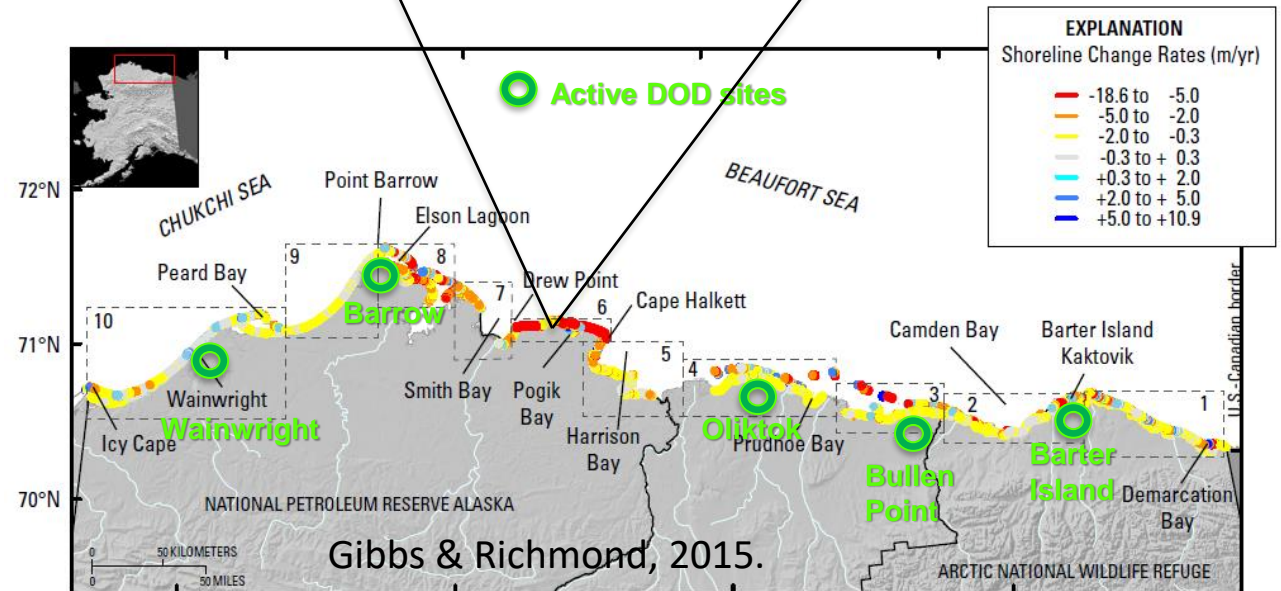
- Primary culprit is **loss of Arctic sea ice**: since 1979 sea ice has lost 51% in area and 75% in volume
  - Increasing **ice-free season**
  - Increasing **wave energy** and **storm surge**
  - Increasing **sea water** temperatures

## *Erosion is threatening:*

- Coastal communities**: threatened with displacement
- Coastal infrastructure**: active DoD sites, including toxic waste sites, in northern Alaska
- Global carbon balance**: permafrost stores greenhouse gases ( $\text{CO}_2$ ,  $\text{CH}_4$ ,  $\text{NO}_2$ ).



Certain locations lost ~200 m (~2 football fields in length) b/w 2007-2017!

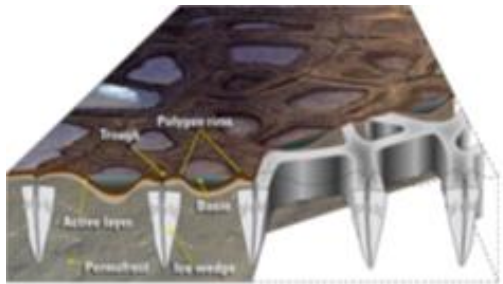




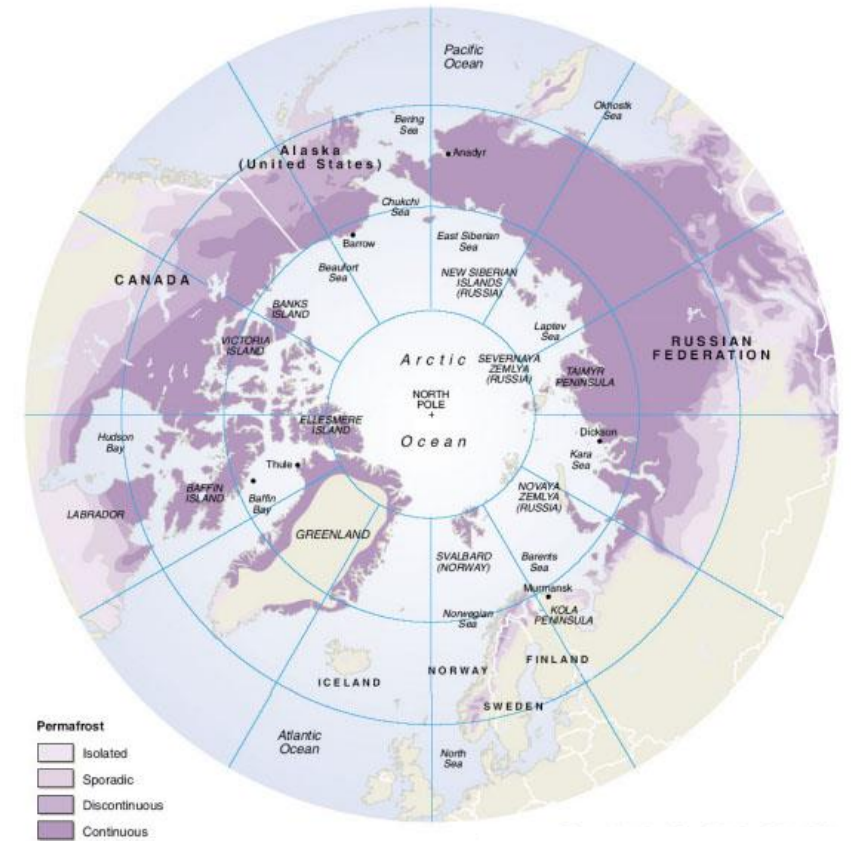
# Permafrost erosion

## What is permafrost?

- Ground, comprised of soil, rock, silt, clay and sand, held together by ice, that remains frozen for 2+ consecutive years.
- 24% of ice-free land area in Northern Hemisphere and 85% of Alaska, Greenland, Canada and Siberia sits on top of permafrost.



Left: schematic illustrating formation of ice wedges and ice-wedge polygon landscapes. Right: map of permafrost distribution in Arctic



Brown *et al.* 1998.

## Unique coastal permafrost erosion process in Arctic:

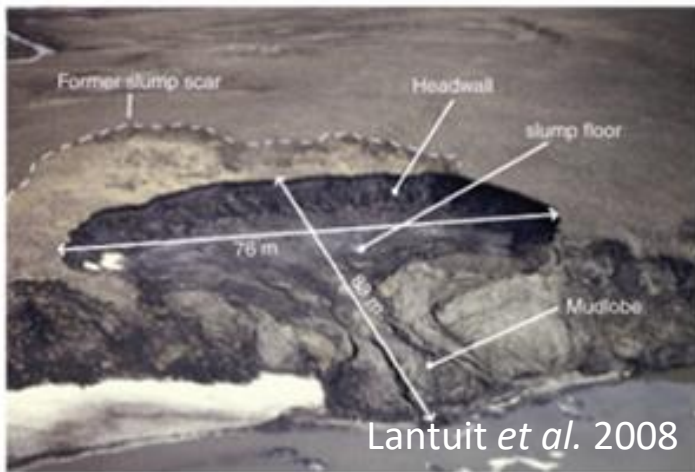
- Predominant geomorphology: **ice-wedge polygons**
  - Ice acts to **bind** unconsolidated soils in permafrost forming ice wedges.
  - Ice wedges **grow/expand** up to ms wide and 10s meters deep.
  - Melting of ice wedges causes permafrost **failure**.



Martin *et al.* 2009.

# Permafrost failure mechanisms

- **Retrogressive thaw slumping**: a slope failure characterized by thaw of exposed ground ice and slumping of thawed soil, typically caused by thermo-denudation<sup>1</sup>.
- **Active layer detachment**: failures are translational landslides that occur in summer in thawing soil overlying permafrost, typically caused by thermo-denudation<sup>1</sup>.
- **Block failure**: a niche (recess at bluff base) progresses landward until the overhanging material fails in a shearing or toppling mode known as block failure, caused by thermo-abrasion<sup>2</sup>.
  - Fallen blocks can disintegrate in the near-shore environment **within 1-2 weeks!**



Retrogressive thaw slumping



Active layer detachment



Block failure

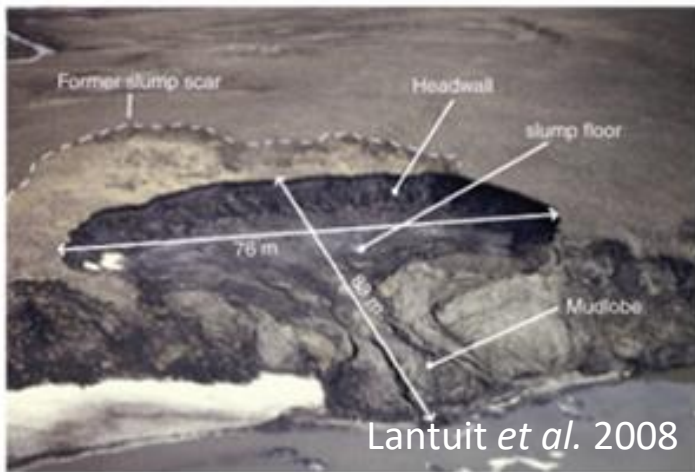


<sup>1</sup>Thawing of permafrost bluffs that proceeds under the influence of gravity. <sup>2</sup>Undercutting of permafrost bluff by warming ocean.



# Permafrost failure mechanisms

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Retrogressive thaw slumping



Active layer detachment



Block failure

**Dominant failure mechanism  
in northern Alaska**

Ravens et al. 2012



<sup>1</sup>Thawing of permafrost bluffs that proceeds under the influence of gravity. <sup>2</sup>Undercutting of permafrost bluff by warming ocean.



# Example of bluff erosion during 2019 UAV surveys\*



Fallen blocks can  
disintegrate in near-  
shore environment  
**within 1-2 weeks!**

\*Images courtesy of Ben  
Jones, UAF

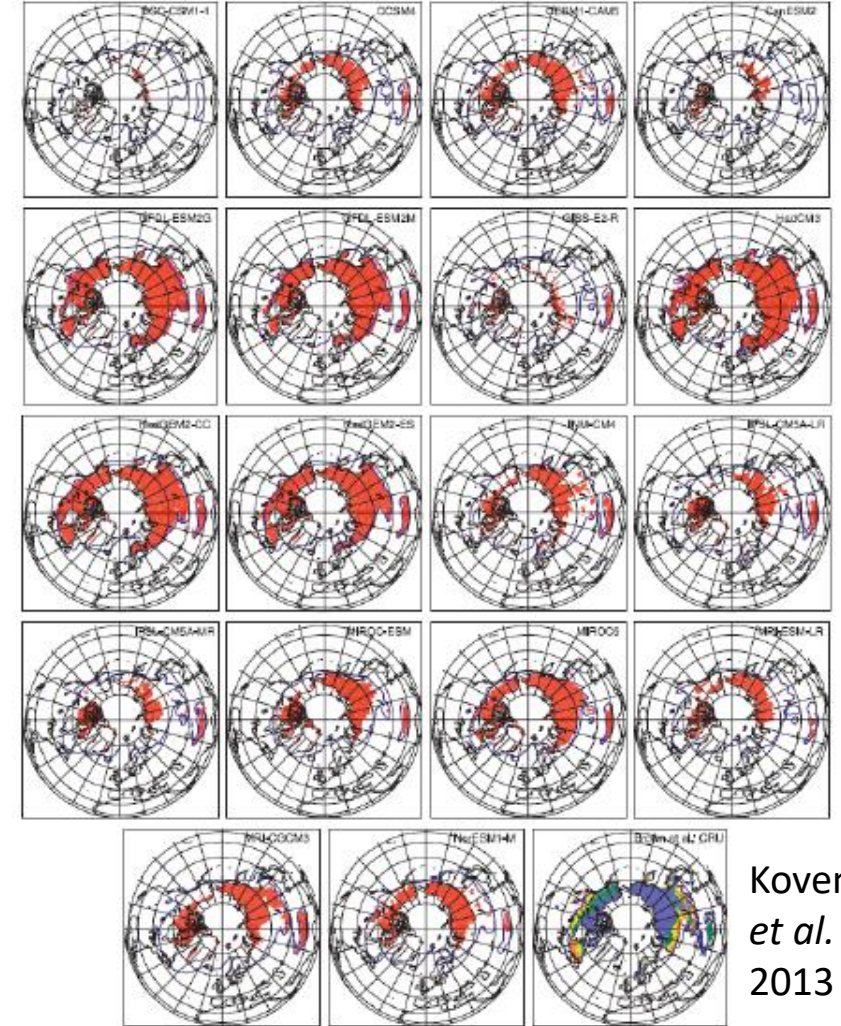


# State-of-the-art in permafrost modeling

When this project began in 2017, tools to **accurately predict** Arctic coastal erosion **did not exist!**

- Most existing models\* (including Earth System Model-, or ESM-, coupled models) are **primitive**:
  - Most models were based on **trend projection** and/or **empirical relationships**
  - **Limited PDE-based models**: primarily **thermal models**, e.g., 1D steady state heat flow (no mechanics/deformation)
  - Most models assumed a **particular type** of **erosion** (e.g., block failure)
  - Models **did not** include **realistic boundary conditions** and **did not** account for permafrost **geomorphologies** or **geophysics**.

**Premise behind the ACE project/model:** an accurate, predictive Arctic coastal erosion model must **couple** the influences of evolving **wave dynamics, thermodynamics** and **mechanics**.



Koven  
*et al.*  
2013

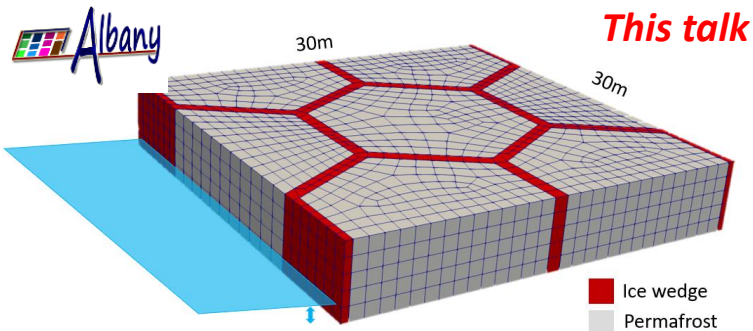
\* See (Frederick *et al.* 2016), Chapter 5, for extensive overview.

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# Proposed solution: multi-scale approach

Goal of the **Arctic Coastal Erosion (ACE)** project is to deliver a **field-validated predictive model of thermo-abrasive erosion** for the **permafrost Arctic coastline**



*This talk*

## Micro-Scale Model

10's of meters & storm duration

One set of input variables defining the geomorphology and geophysics of the terrestrial model.

- 3D heat transfer + mechanics-based plastic deformation
- Wave circulation BCs representing time-varying realizations of individual storm events.



## Meso-Scale Model

10's of kilometers & monthly duration

A number of micro-scale models that represent the stochastic distributions of input variables along a confined coastline.



## Macro-Scale Model

100's of kilometers & annual (+) durations

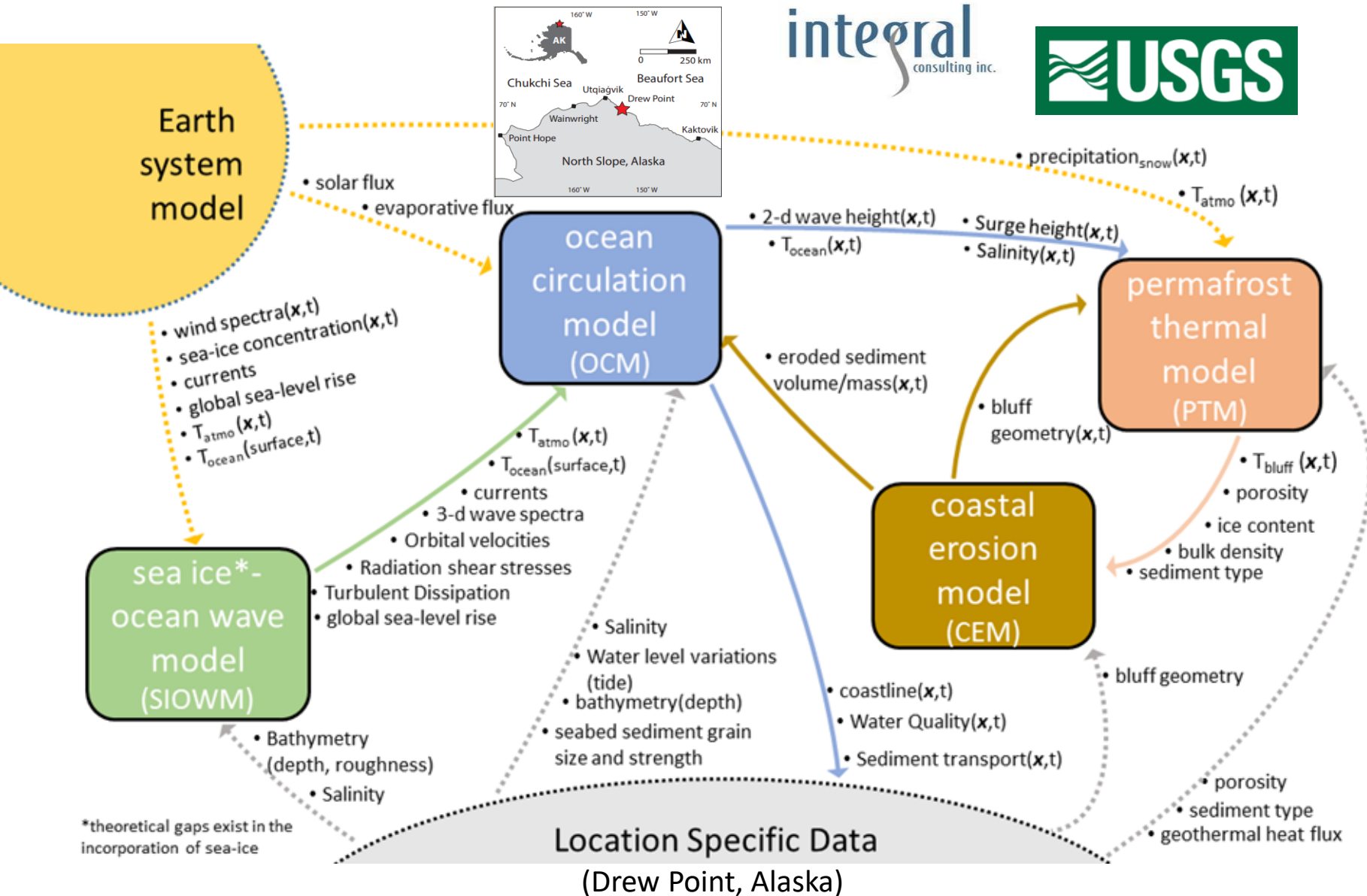
A number of meso-scale models representing different coastline types (delta, exposed bluffs, lagoons, etc.) along the AK coastline.

*Longer term vision:* upscale micro-scale model to meso- and macro-scales

*Create "catalog" of smaller-scale models for diff. Arctic locations, use catalog to derive (physics-based) statistical parameterizations of things like aggregate retreat rates*



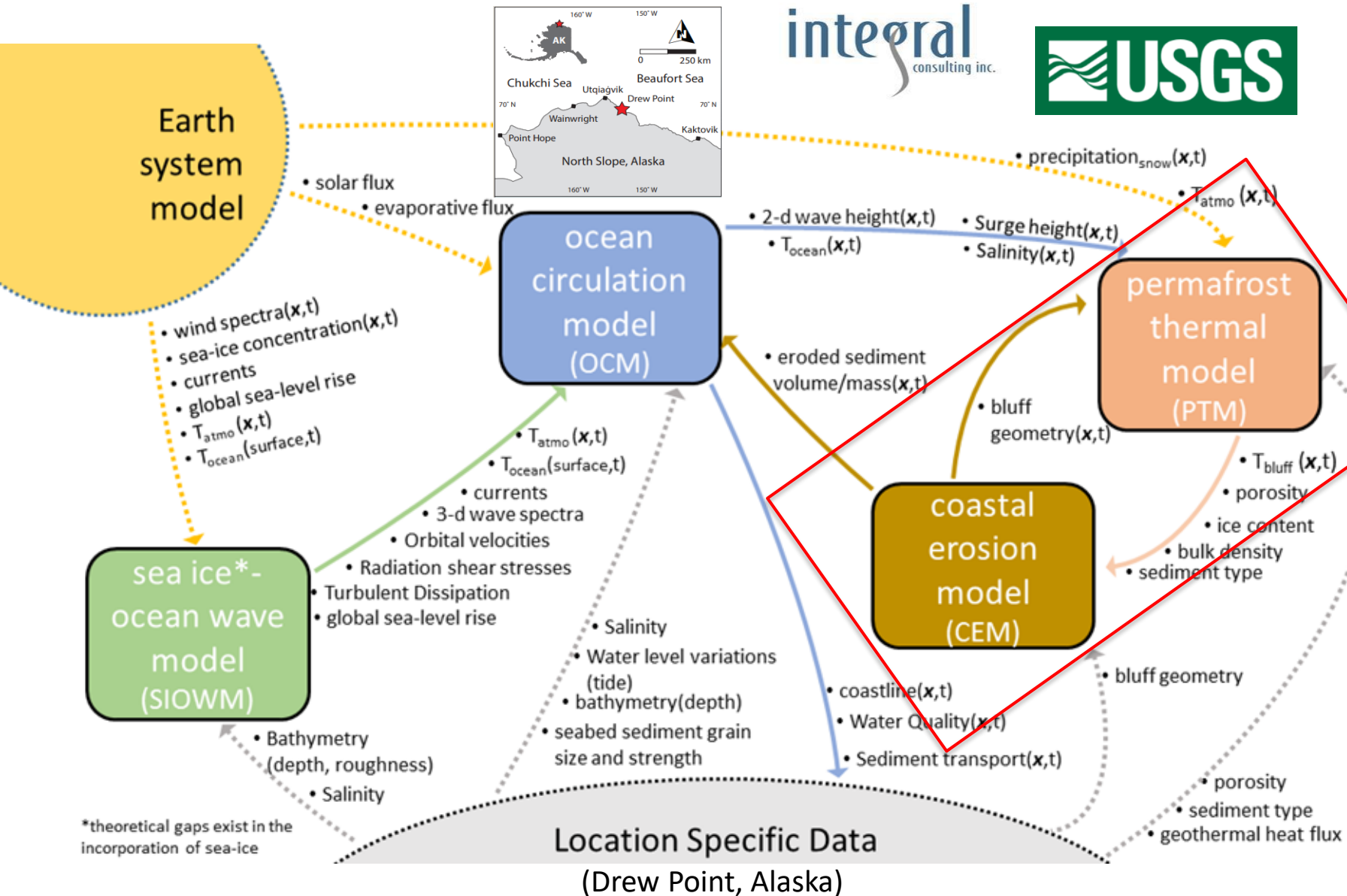
# ACE Model Component Coupling



**ACE project has many pieces!**

- Terrestrial model:** thermo-mechanical coupled FEM model that can simulate transient niche development.
- Oceanographic model:** WW3 + SWAN + Delft3D wave models for providing oceanic BCs (ocean temp/height) to terrestrial model.
- Geomechanical testing:** for characterization of permafrost parameters in terrestrial model.
- Field campaign:** offshore oceanographic measurements, bathymetric survey, niche measurements, etc.

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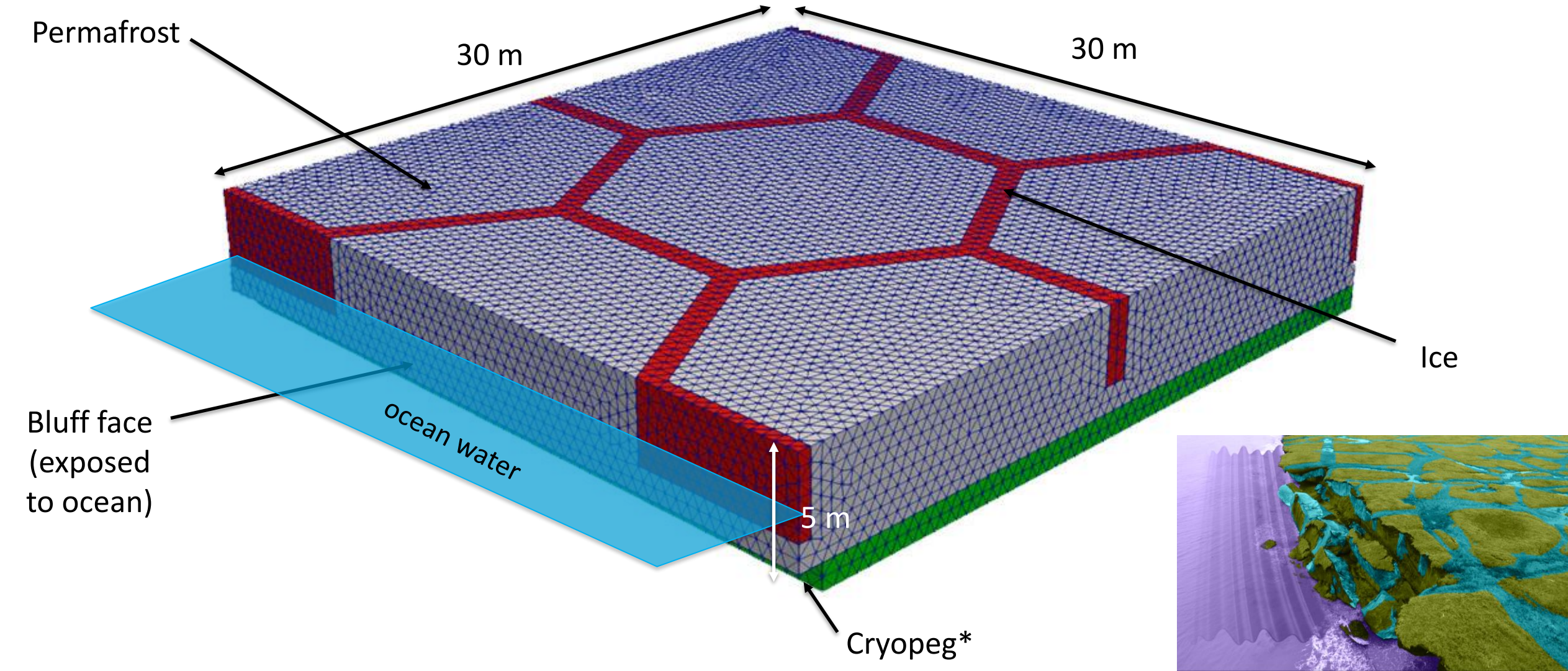
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# Anatomy of a canonical computational domain



\* Layer of unfrozen ground that is perennially cryotic (forming part of the permafrost) in which freezing is prevented.

# Mechanical model

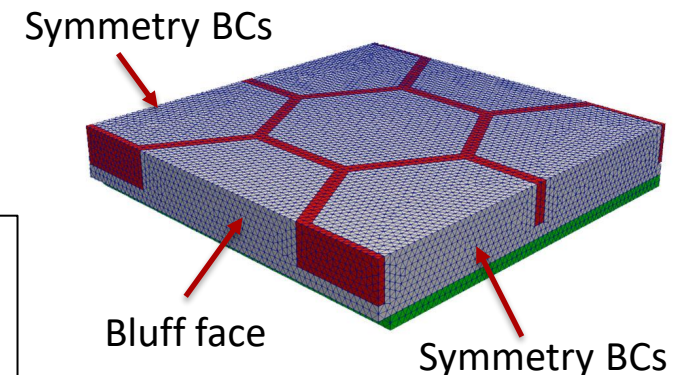
- Finite deformation **time-dependent** variational formulation for **solid mechanics problem** obtained by minimizing the energy functional:

$$\Phi[\boldsymbol{\varphi}] := \int_{\Omega} A(\mathbf{F}, \mathbf{Z}) dV - \int_{\Omega} \rho \mathbf{B} \cdot \boldsymbol{\varphi} dV - \int_{\partial_T \Omega} \mathbf{T} \cdot \boldsymbol{\varphi} dS$$

$A(\mathbf{F}, \mathbf{Z})$ : Helmholtz free-energy density  
 $\mathbf{Z}$ : material variables  
 $\mathbf{F}$ : deformation gradient ( $\nabla \boldsymbol{\varphi}$ )  
 $\rho$ : density  
 $\mathbf{B}$ : body force  
 $\mathbf{T}$ : prescribed traction

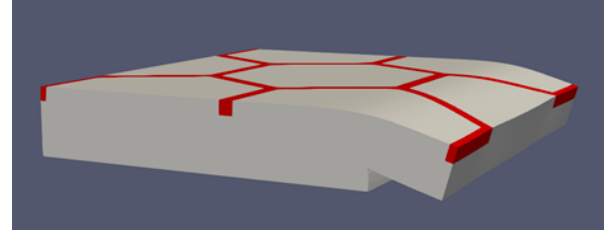
- Computes **displacements** and **new computational geometry** (following erosion)
- **$J_2$  plasticity** extended to large-deformation regime **constitutive model** for **ice** and **permafrost**
  - Incorporates all mechanisms that lead to deformation, plastic flow and creep of polycrystalline materials like ice; minimal calibration parameters; simplest material model w/ plastic behavior.
- **Boundary conditions:**
  - **Symmetry BCs** on lateral sides
  - **Wave pressure Neumann BC** on bluff face\* (from wave model).
- **Yield stress:**  $\sigma_0(T) := S_s \sigma_Y^{\text{soil}} + S_f f(T) \sigma_Y^{\text{ice}}$ 
  - Used in erosion failure criteria

$f$ : ice saturation ( $\in [0,1]$ )  
 $\sigma_Y^{\text{soil}} / \sigma_Y^{\text{ice}}$ : yield stress of soil/ice  
 $S_s / S_f$ : soil/ice volume fraction



# Erosion failure criteria

- **Erosion criterion:** when material exposed to water reaches a critical exposure time.
- **Stress criterion:** when material reaches a critical value of the yield stress.
- **Kinematic criterion:** when material has tilted excessively, it is assumed to have fallen as part of block erosion.

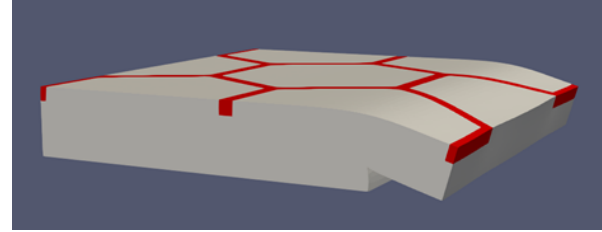


Once **failure criterion** is reached, “failed” elements are **removed** from mesh.

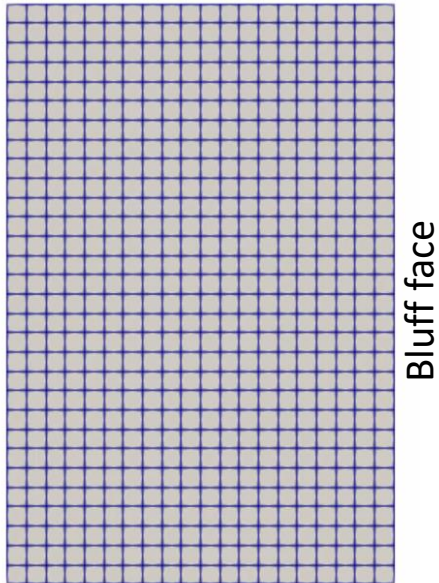


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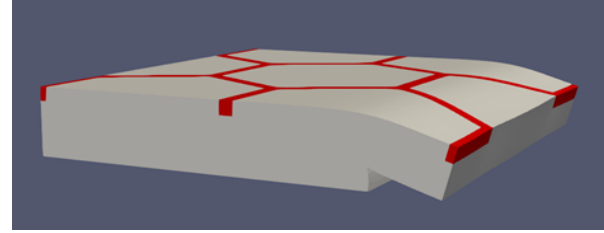


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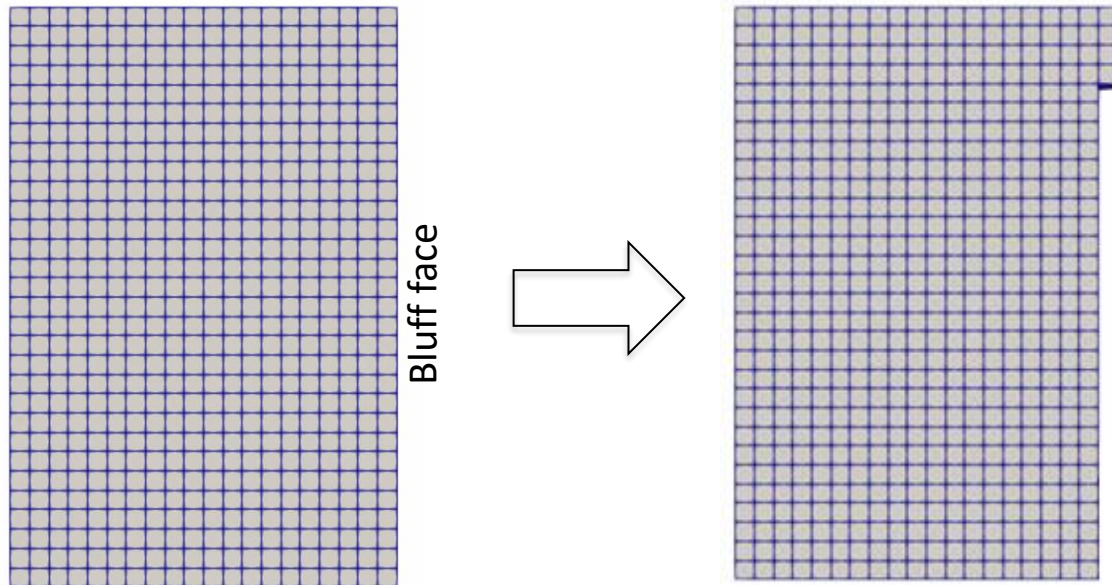


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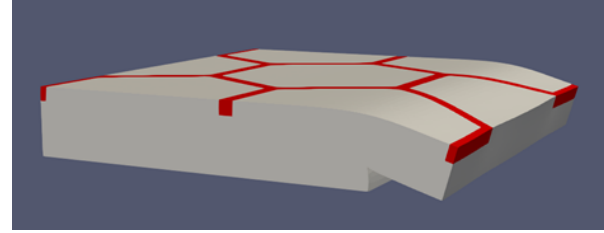


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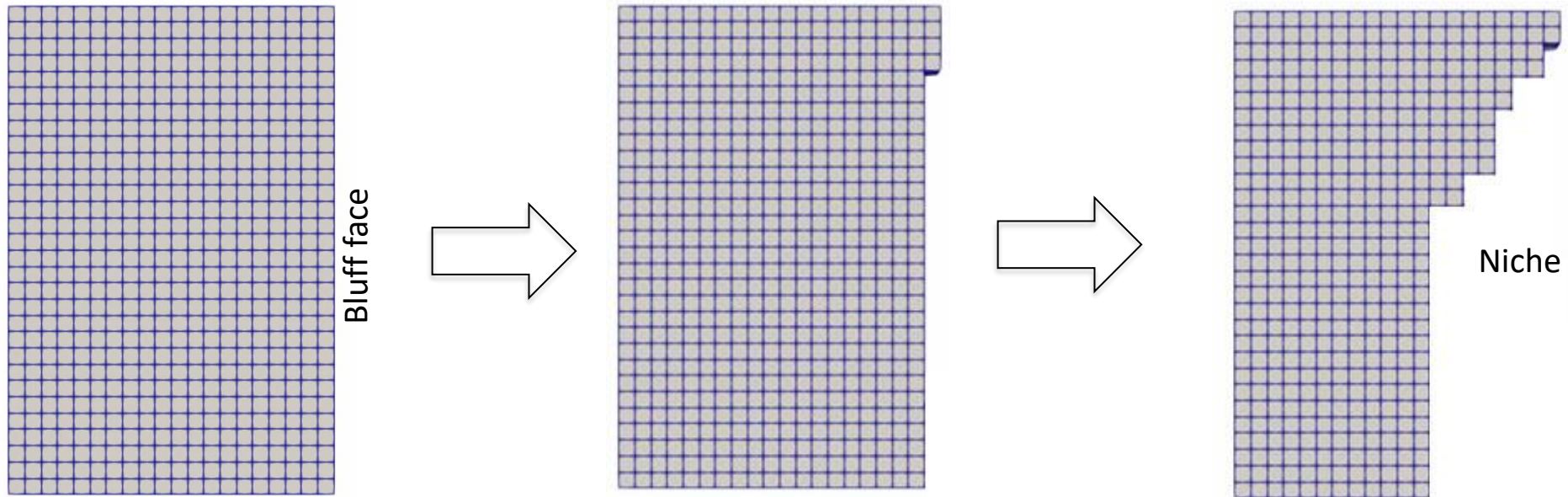


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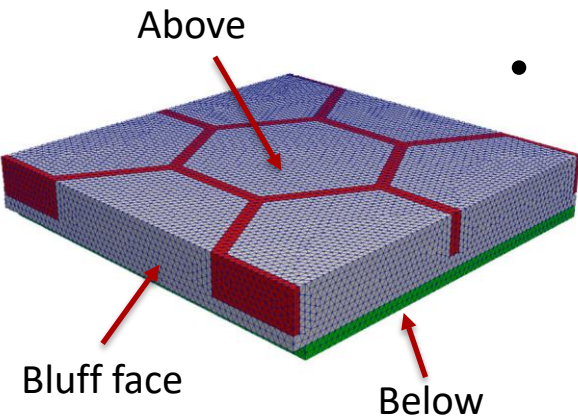
# Thermal model

- **Transient heat conduction** in a non-homogeneous porous media with water-ice phase change:

$$(\overline{\rho c_p} + \tilde{\Theta}) \frac{\partial T}{\partial t} = \nabla \cdot (\mathbf{K} \cdot \nabla T)$$

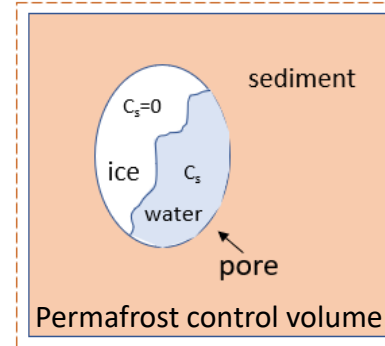
where  $\tilde{\Theta} := \rho_f L_f \frac{\partial f}{\partial T}$  incorporates phase changes through soil freezing curve,  $\frac{\partial f}{\partial T}$ .

- Computes **temperature**  $T$  and **ice saturation**  $f$

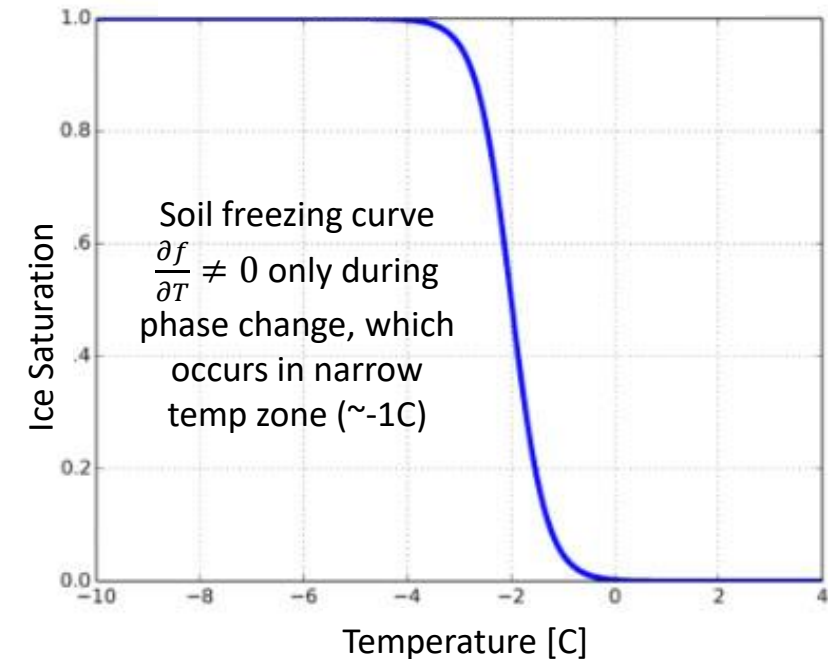


- **Boundary conditions** (from wave model/data)

- Local geothermal heat flux from below
- Mean annual air temp from above
- Air/ocean temp at bluff face



$\bar{\rho}$ : density from mixture model  
 $\bar{c_p}$ : specific heat from mixture model  
 $\mathbf{K}$ : thermal diffusivity tensor  
 $\rho_f$ : ice density  
 $L_f$ : latent heat of water-ice phase change  
 $f$ : ice saturation ( $\in [0,1]$ )  
 $\frac{\partial f}{\partial T}$ : soil freezing curve (depends on salinity)



# Parameters & inputs

## Parameters estimated from lab experiments:

- Elastic modulus, Poisson's ratio, yield stress
- Sand/silt/clay fractions with depth
- Porosity with depth

## Parameters from literature:

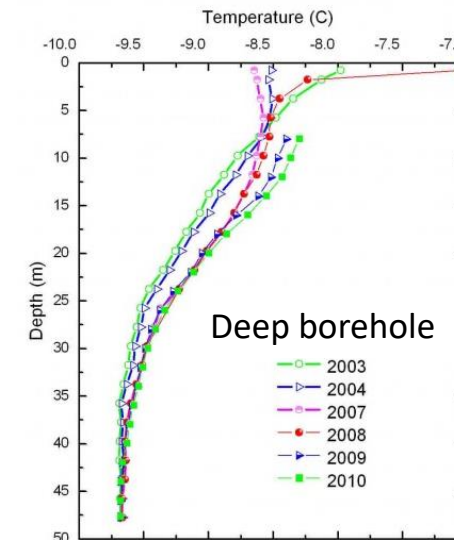
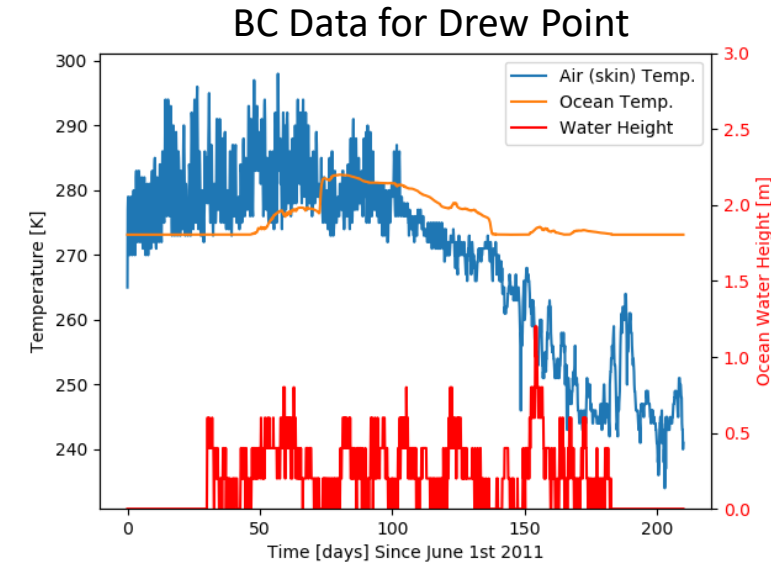
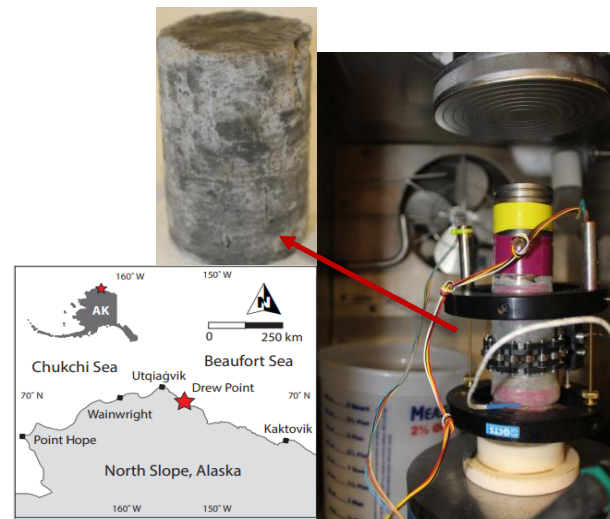
- Ice/water/sediment densities, thermal conductivities, heat capacities
- Freezing curve/width as function of sediment type
- Bluff salinity with depth

## Parameters estimated from observational data at Drew Point, AK:

- Skin temp w/ time, initial bluff temp (USGS weather station data)
- Geothermal heat flux (borehole at Barrow, AK)
- Polygon dimension, ice wedge thickness and depth, bluff height, living organic layer thickness (Aug. 2019 field campaign)

## Parameters from wave model (WW3+SWAN+Delft3D):

- Ocean temperature, salinity and sea-level w/ time (for thermal & wave pressure BCs)

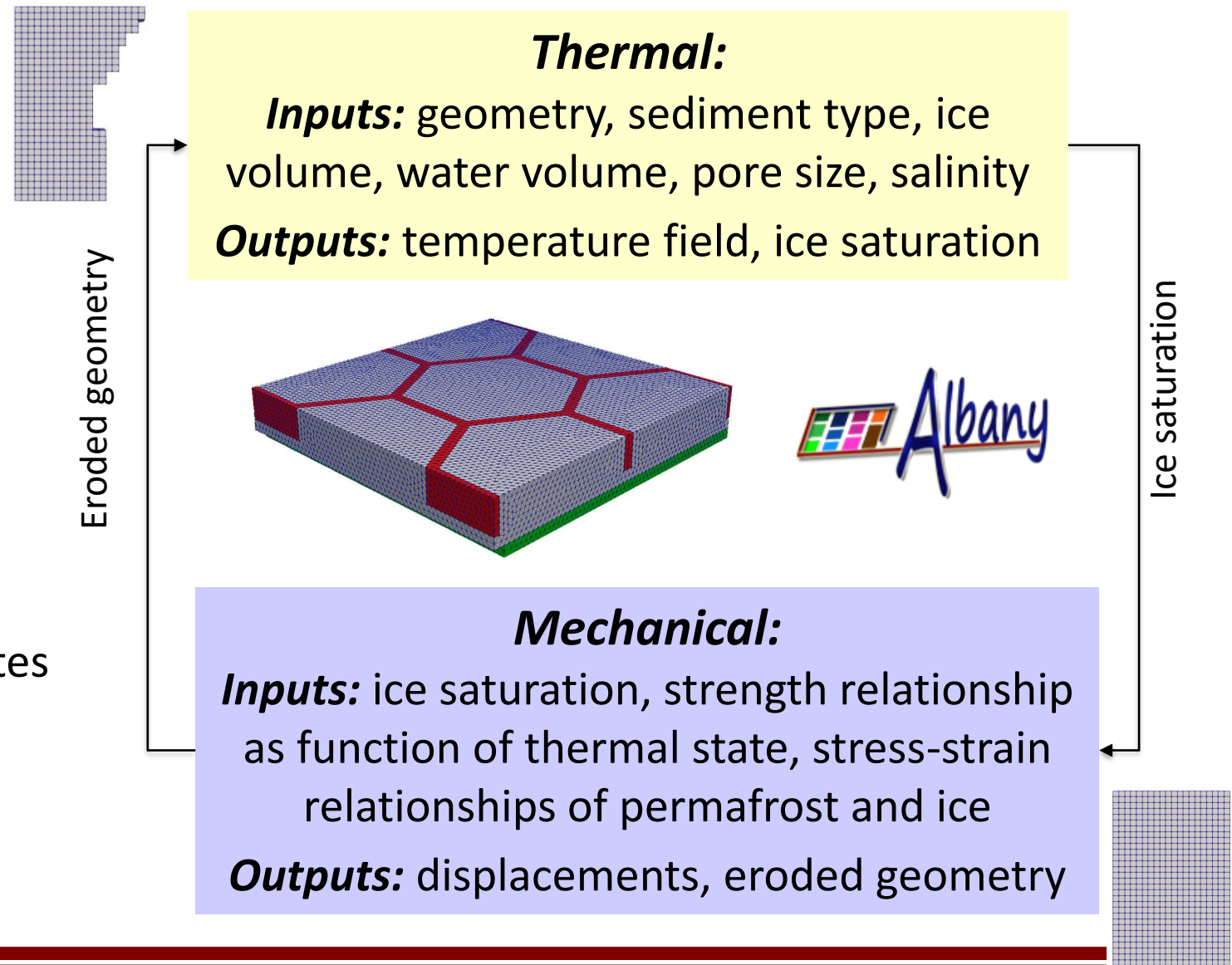


# Coupled thermo-mechanical formulation

## *Potential key advantages:*

- Failure modes develop from **constitutive relationships** in FEM model (no empirical relationships!)
- 3D unsteady heat flow can include **chemistry**
- Thermal and mechanical problems can be advanced using **different time-steppers** (e.g., implicit-explicit coupling)
- **Tightly coupled** strength + thermal states

***Unique characteristic of coupled model:*** coupling happens at the level of material model





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# Finite element implementation within *Albany*-LCM



The ***thermo-mechanical Arctic Coastal Erosion (ACE)*** model is implemented within the ***LCM project*** in Sandia's open-source parallel, C++, multi-physics, finite element code, ***Albany***.



<https://github.com/SNLComputation/LCM>

- ***Component-based*** design for rapid development.
- Contains a wide variety of ***constitutive models***.
- Extensive use of libraries from the open-source ***Trilinos*** project.
  - Use of the ***Phalanx*** package to decompose complex problem into simpler problems with managed dependencies.
  - Use of the ***Sacado*** package for ***automatic differentiation***.
- Coupled to the ***DOE's Energy Exascale Earth System Model (E3SM)*** through MPAS - Albany Land Ice (MALI) component.
- All software available on ***GitHub***.



<https://github.com/trilinos/trilinos>



# Numerical results summary

## Mechanics-only simulation<sup>1</sup>



## Thermo-mechanical simulations<sup>2</sup>

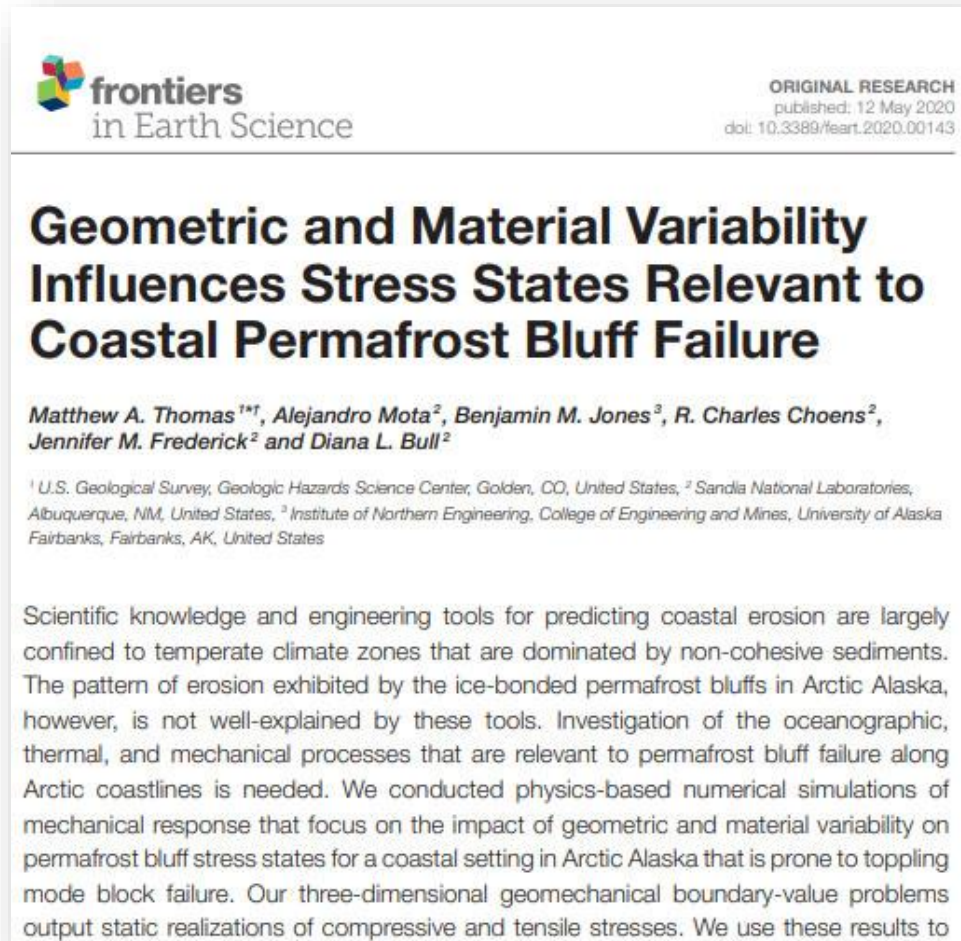


<sup>1</sup> M. Thomas et al. *Frontiers in Earth Science* 8, April 2020. <sup>2</sup> Frederick, Mota, Tezaur, Bull, *J. Comput. Appl. Math.* 2021.



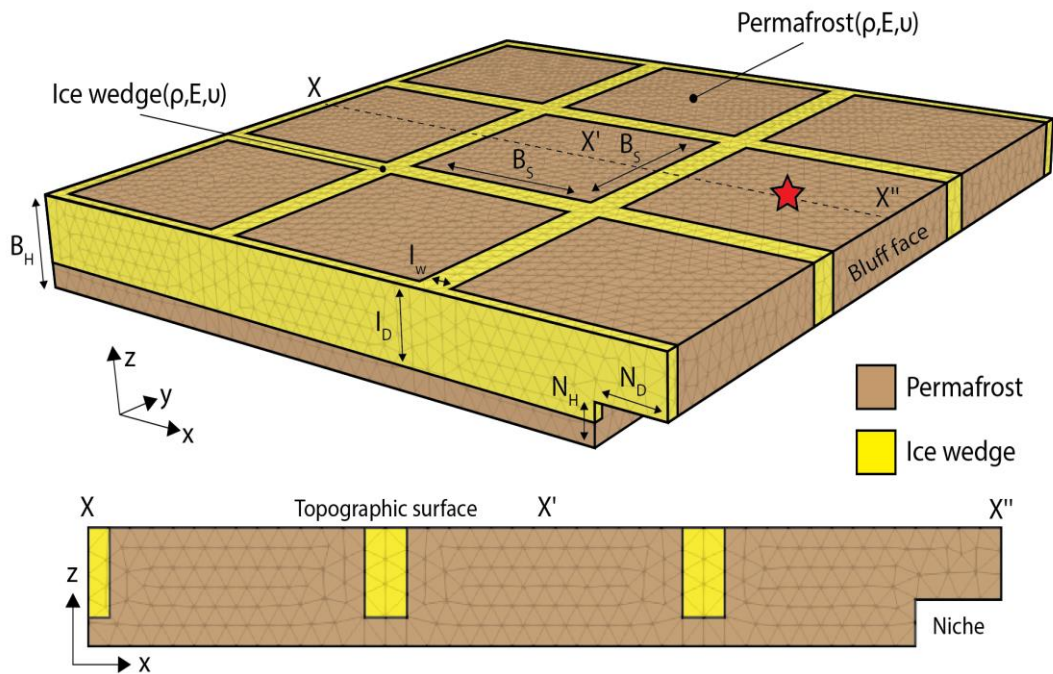
# Mechanics-only simulation

## Mechanics-only simulation\*



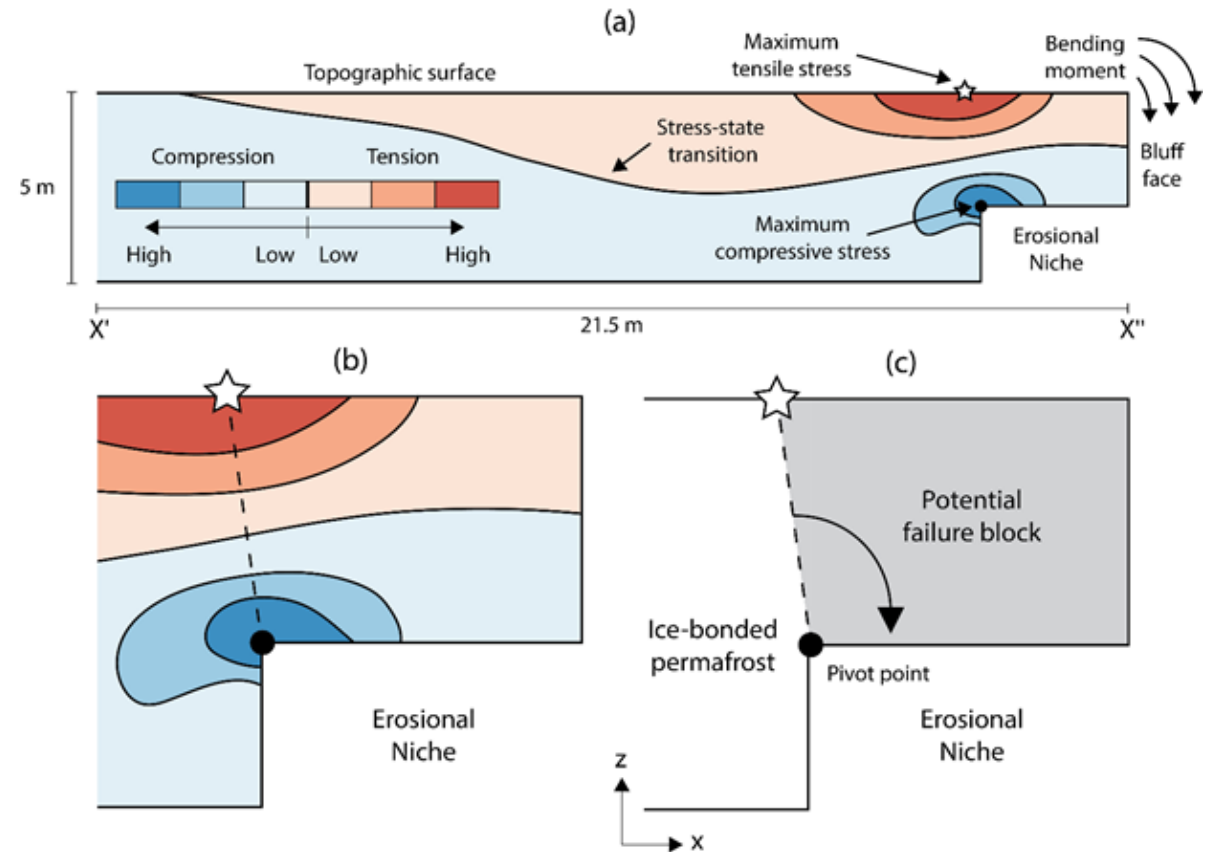
\* M. Thomas *et al.* *Frontiers in Earth Science* 8, April 2020.

# Mechanics-only simulation\*



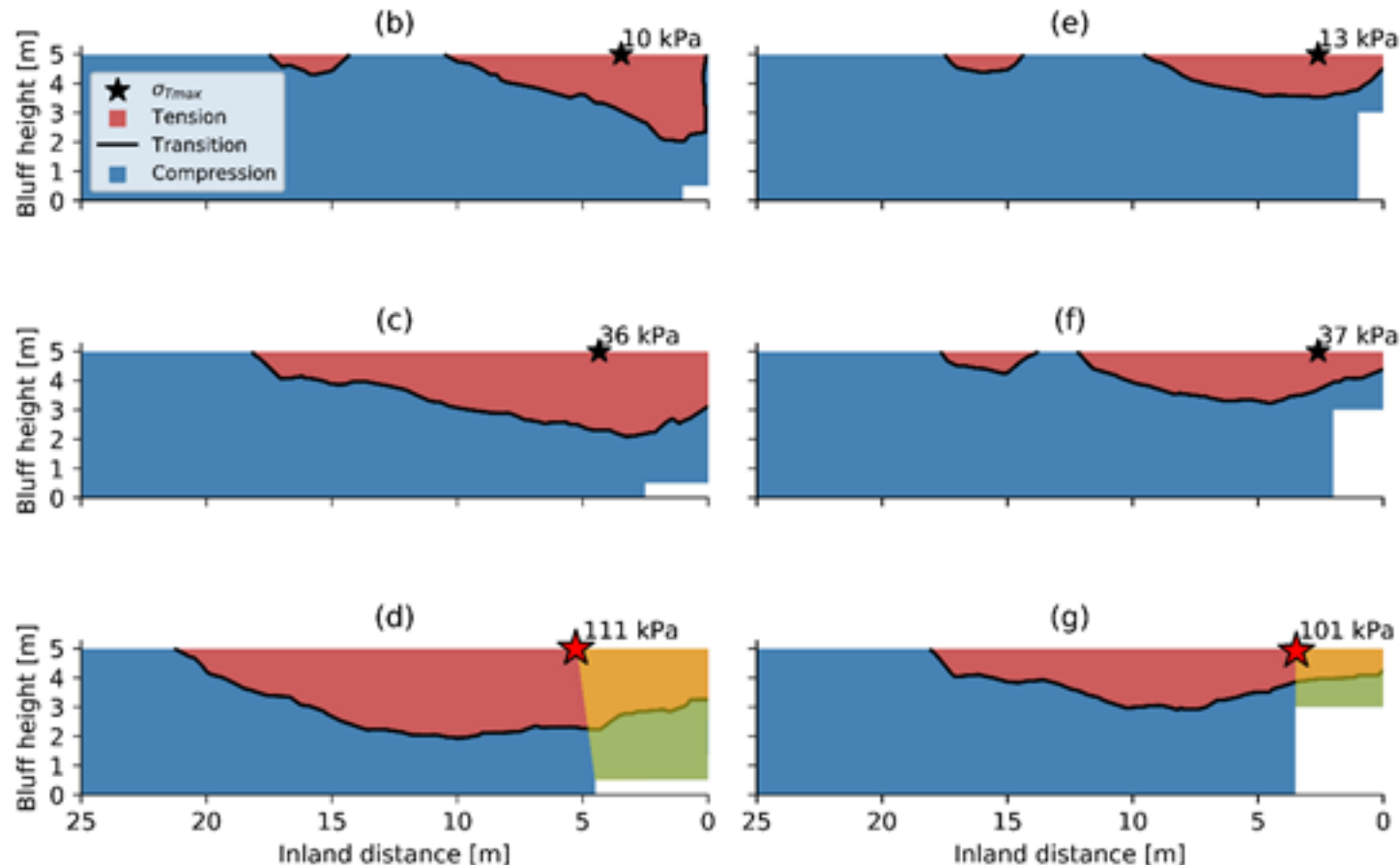
- Simulations facilitated examination of **stress patterns** within bluff and identification of **location** and **magnitude** of **max tensile stress** ( $\sigma_{T_{\max}}$ )

- 3D elastic mechanics-only** simulations assessed impact of **bluff geometry** and **material variability** on stress states leading up to bluff failure
  - Only load is gravitational.



# Mechanics-only simulation\*: main takeaways

**Niche dimension** affects location and magnitude of simulated **max tensile stress** ( $\sigma_{T_{\max}}$ ) more than the bluff height, ice wedge polygon size, ice wedge geometry, bulk density and Poisson's ratio



- Inland extent of niche was advanced for 6 erosional niche heights from 0.1-3 m

**Taller and narrower erosional niches** promote smaller failure masses compared to those with shorter and deeper niches

- Lower bound for tensile stress from lab measurements: 100 kPa
- Orange/green shading highlights potential failure areas.

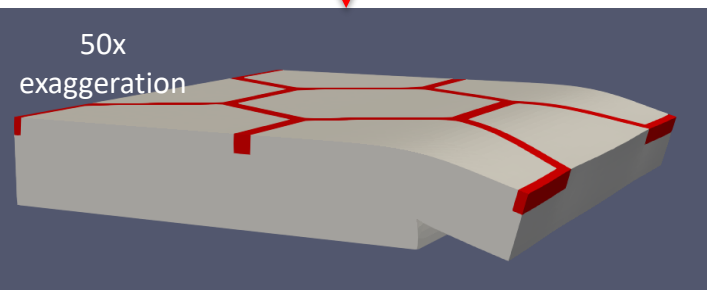
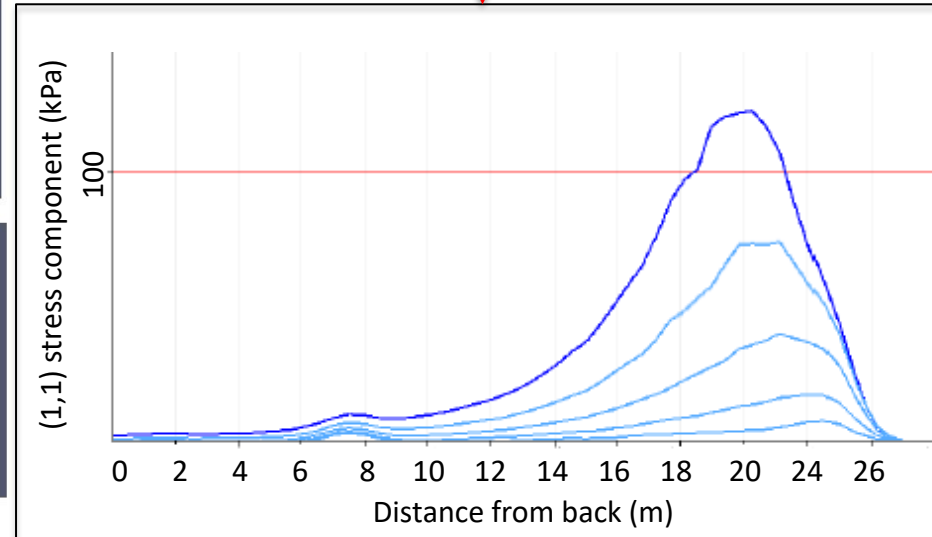
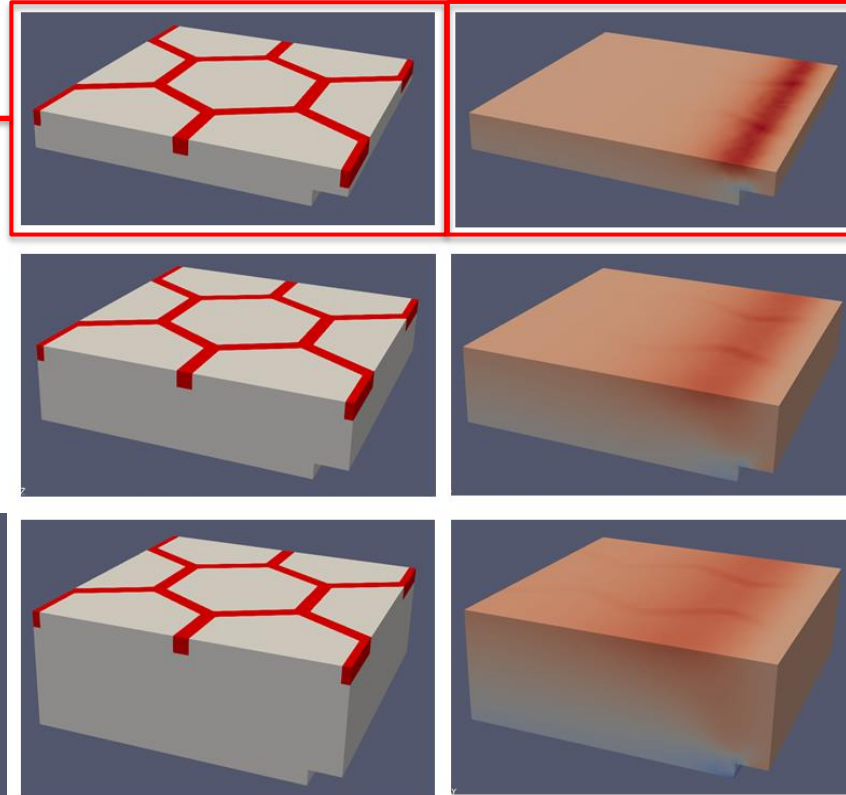
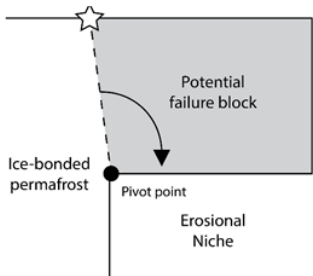


# Mechanics-only simulation\*: main takeaways

**Taller and narrower erosional niches** promote smaller failure masses compared to those with shorter and deeper niches

As niche advances into the block, an overhanging section in the block acts as **cantilever**.

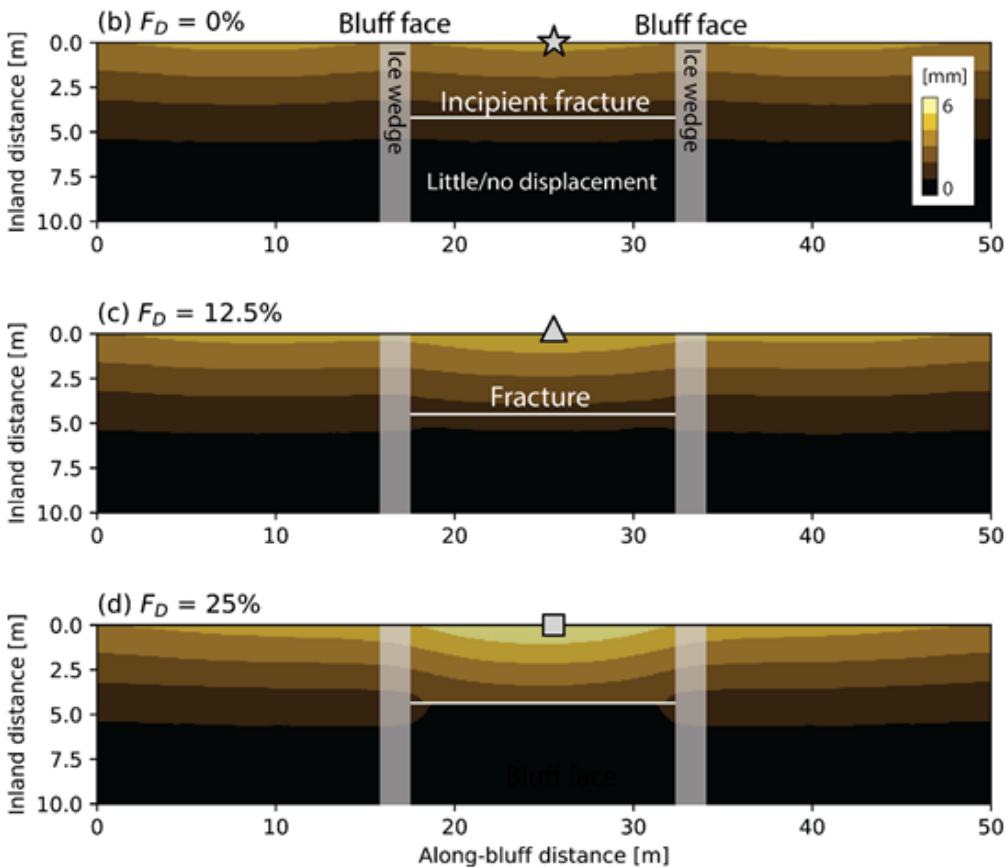
Highest **tensile stresses** develop on top surface where cantilever meets rest of block



\* M. Thomas *et al.* *Frontiers in Earth Science* 8, April 2020.

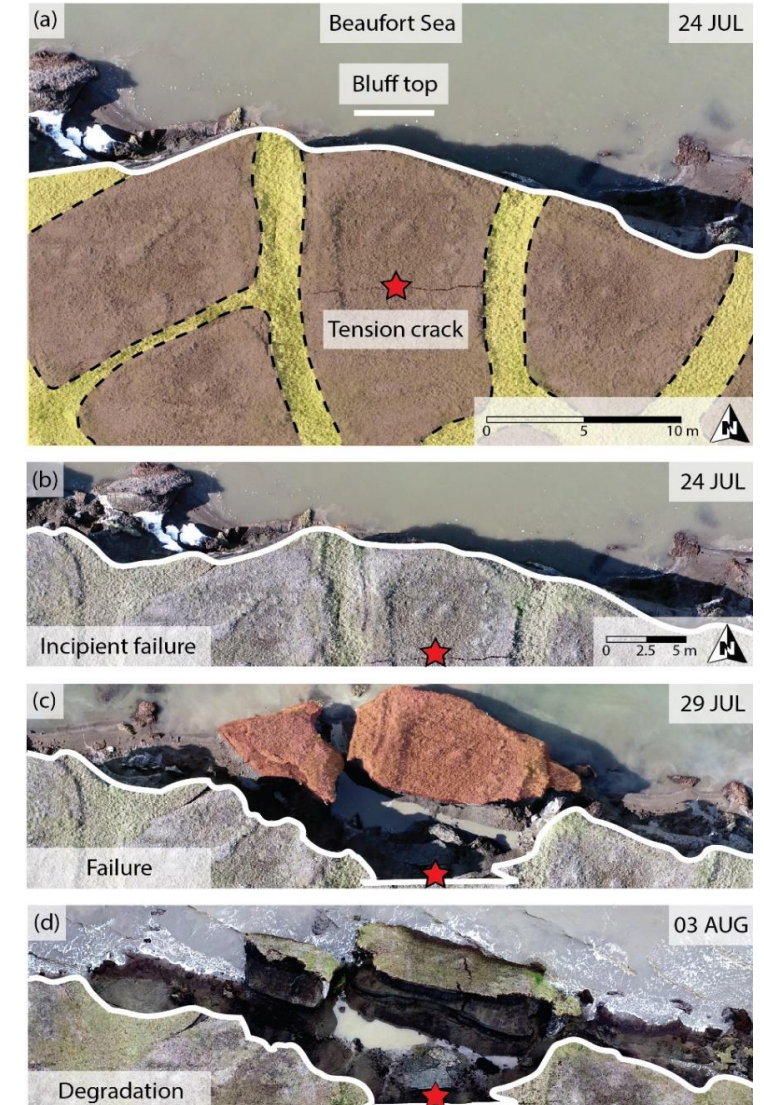
# Mechanics-only simulation\*: main takeaways

- It has been observed that **failure** can occur along **tension cracks** in ice wedge polygon centers.



- Simulations suggest **tension cracks** can form within the range of niche depths/heights considered here.
- Even relatively **shallow vertical cracks** can **concentrate strain** within ice-bonded permafrost bluffs.

$F_D$ : fracture depth



# Thermo-mechanical 2.5D slice simulation

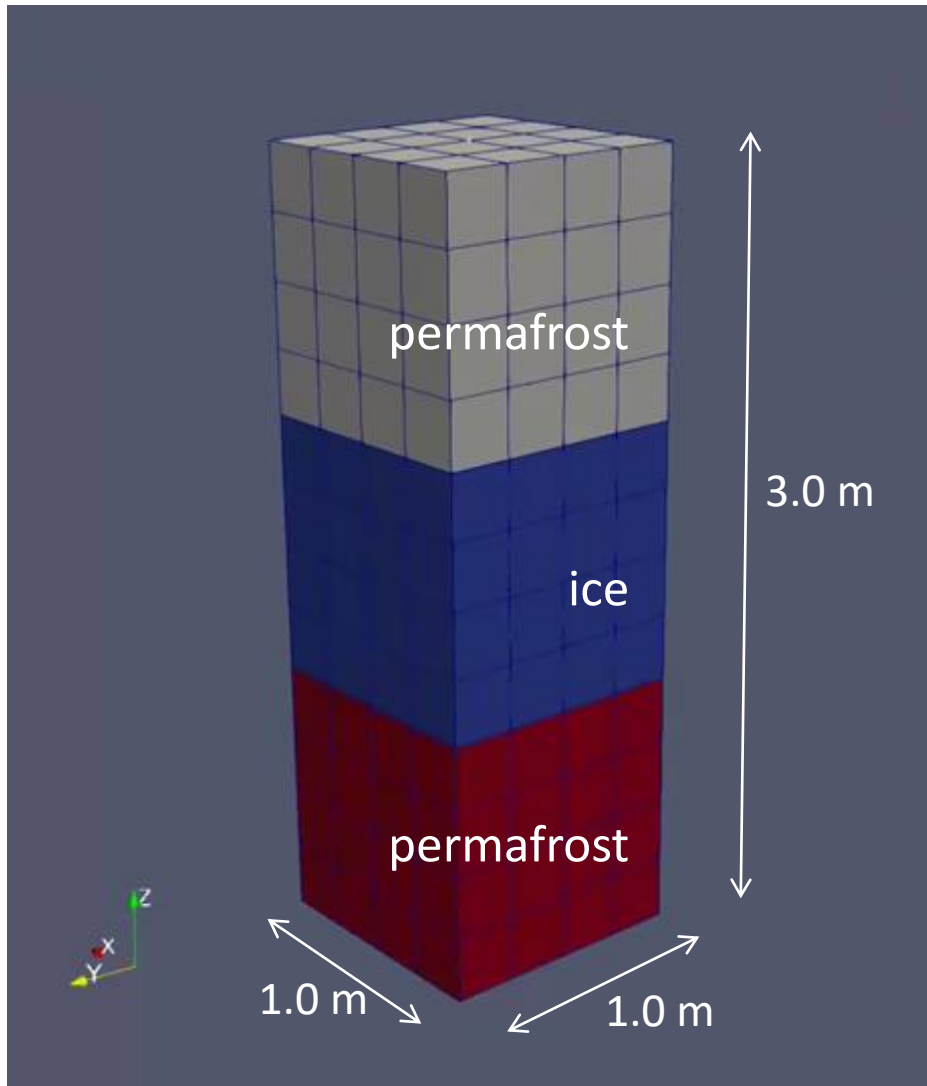
## Thermo-mechanical simulations\*



\* Frederick, Mota, Tezaur, Bull, *J. Comput. Appl. Math.* 2021.



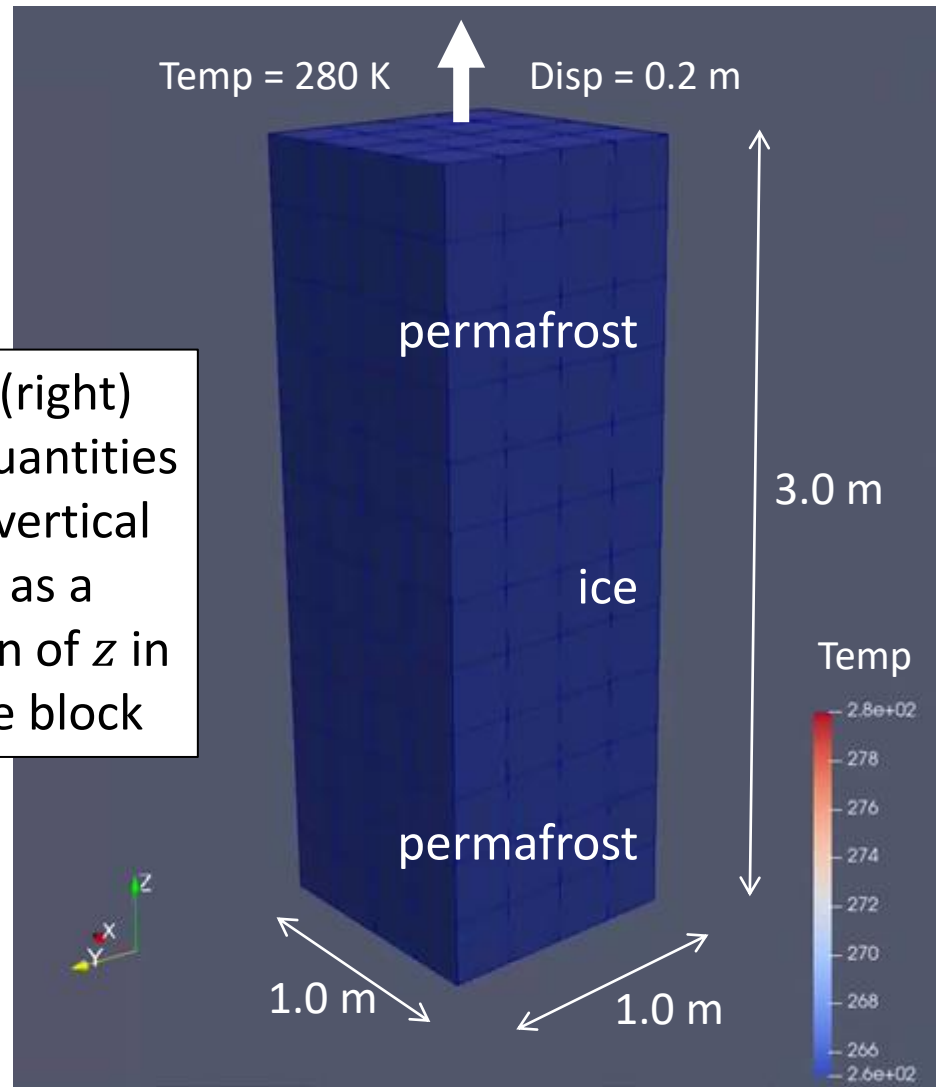
# Thermo-mechanical coupling: cuboid problem



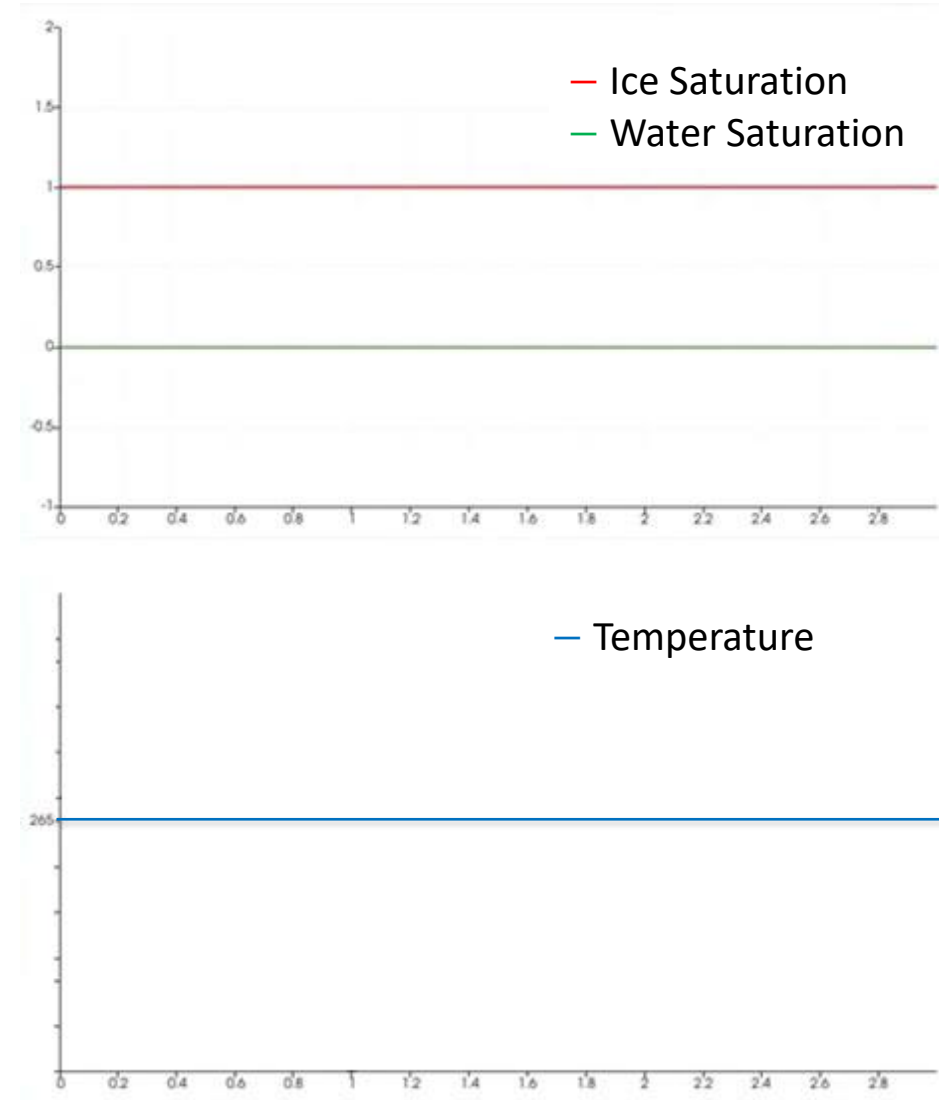
- Cuboid is comprised of block of **ice** material, **wedged** between two blocks of **permafrost** material.
- Cuboid subjected to **simultaneous heating** and **stretching** from the **top**
- Cuboid is **affixed** to the **bottom** and with **symmetry boundary conditions** on the **sides**.
- **Temperature** is initialized to 265K.



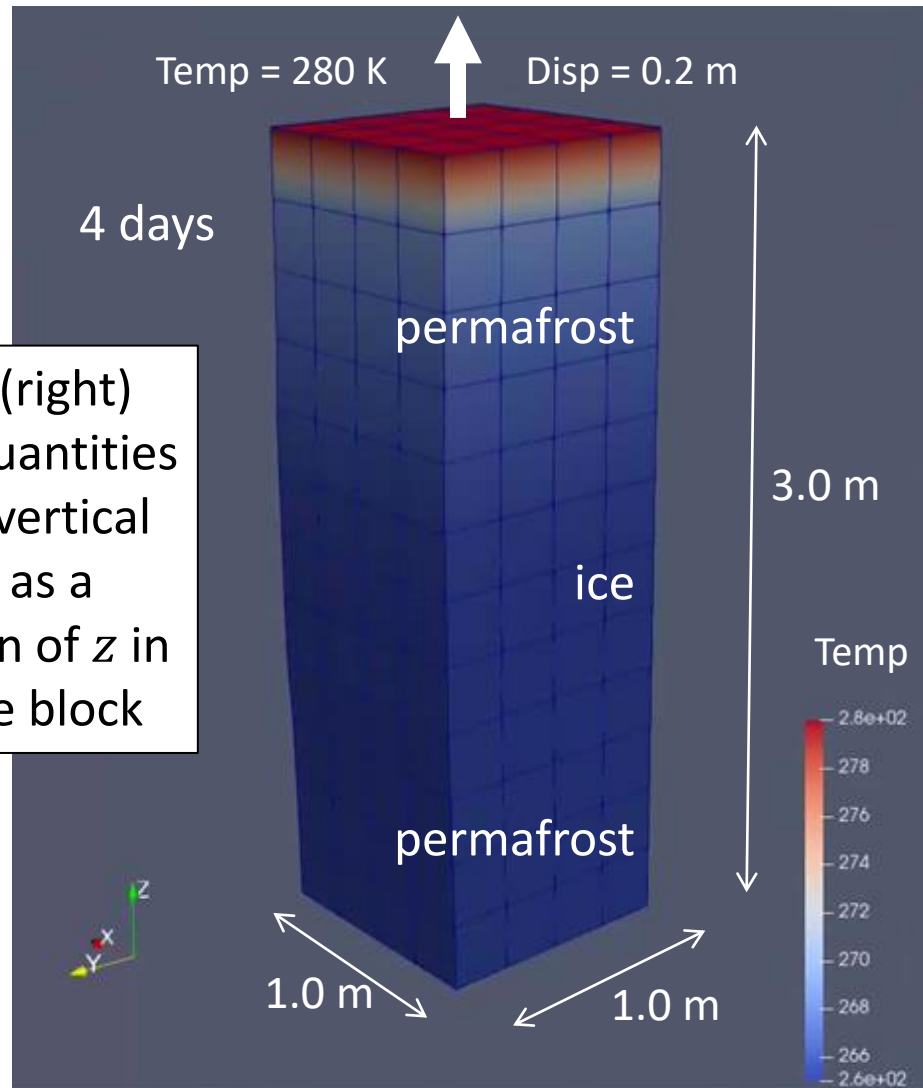
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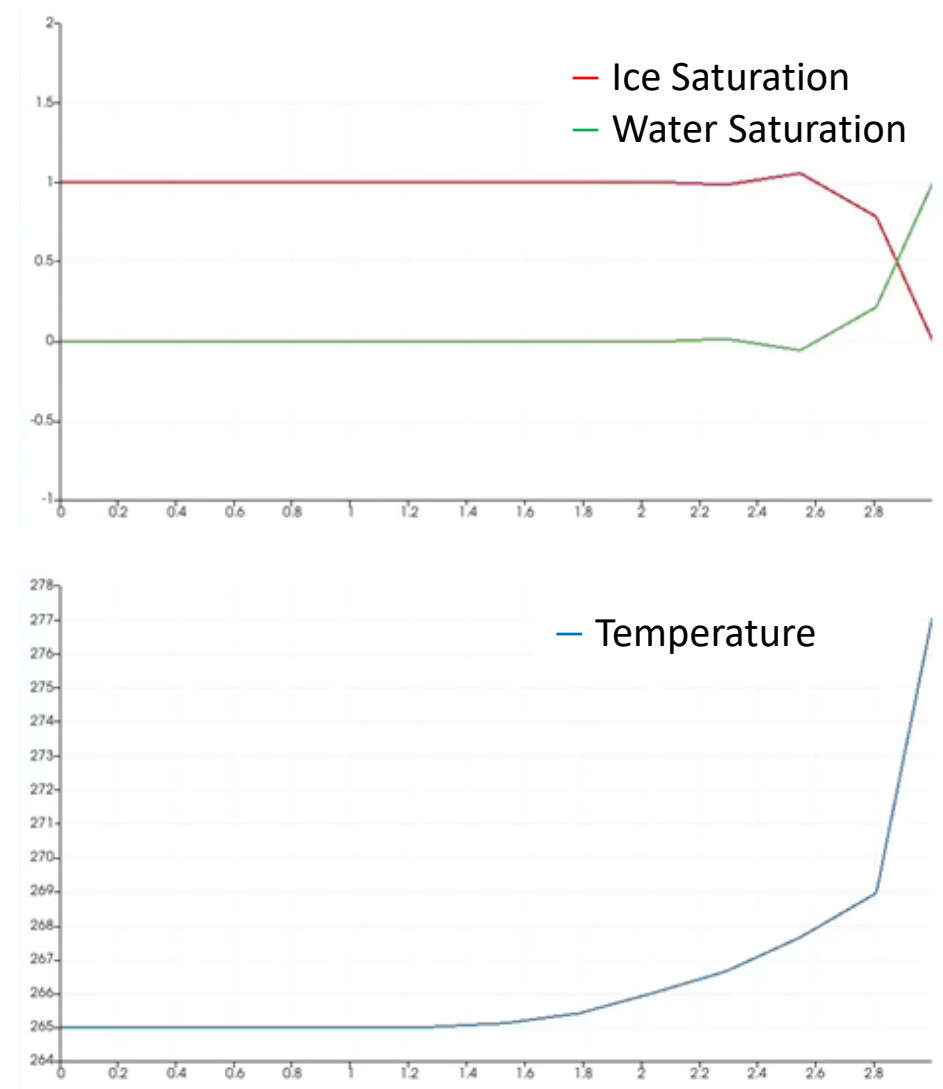
Plots (right) show quantities along vertical line as a function of  $z$  in the ice block



# Thermo-mechanical coupling: cuboid problem

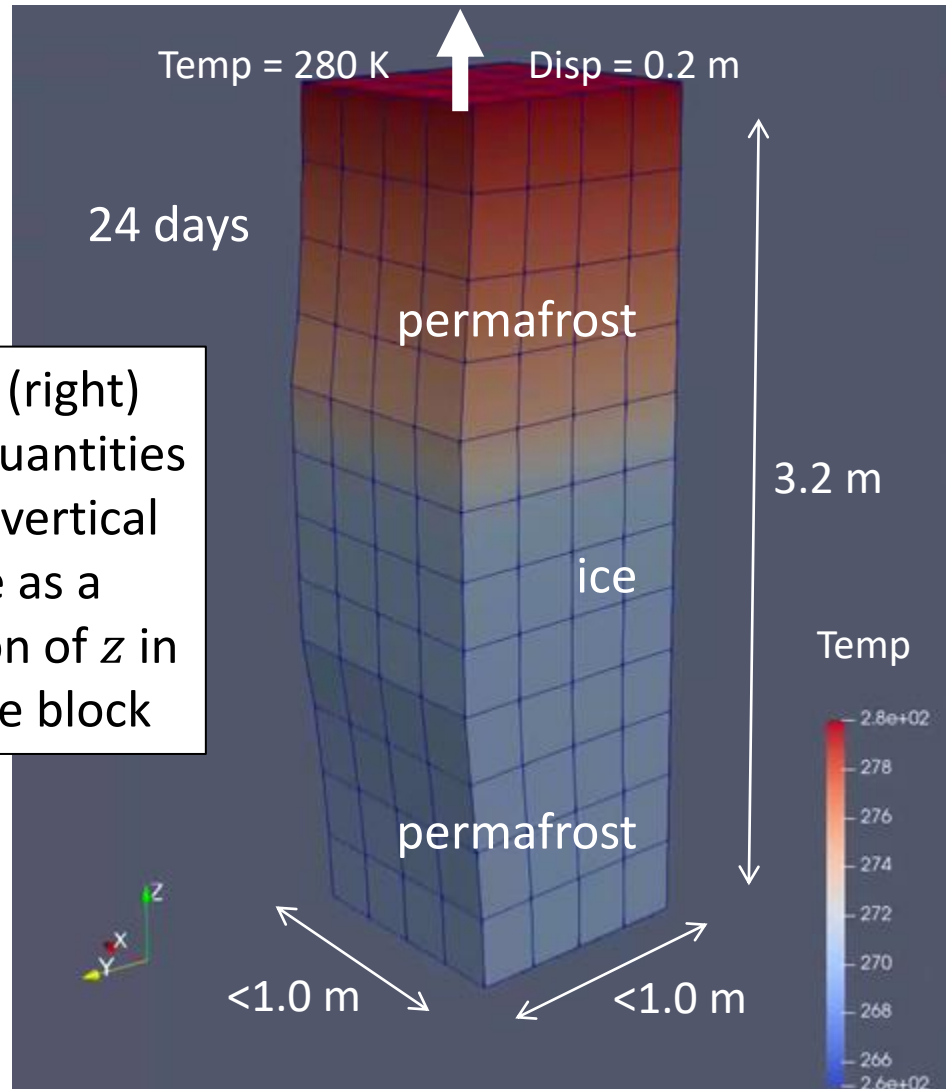


Plots (right)  
show quantities  
along vertical  
line as a  
function of  $z$  in  
the ice block

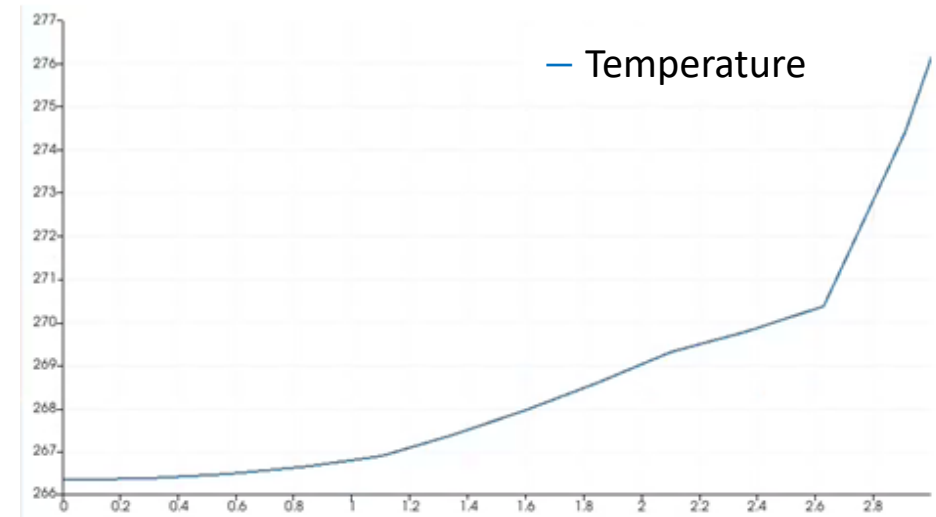
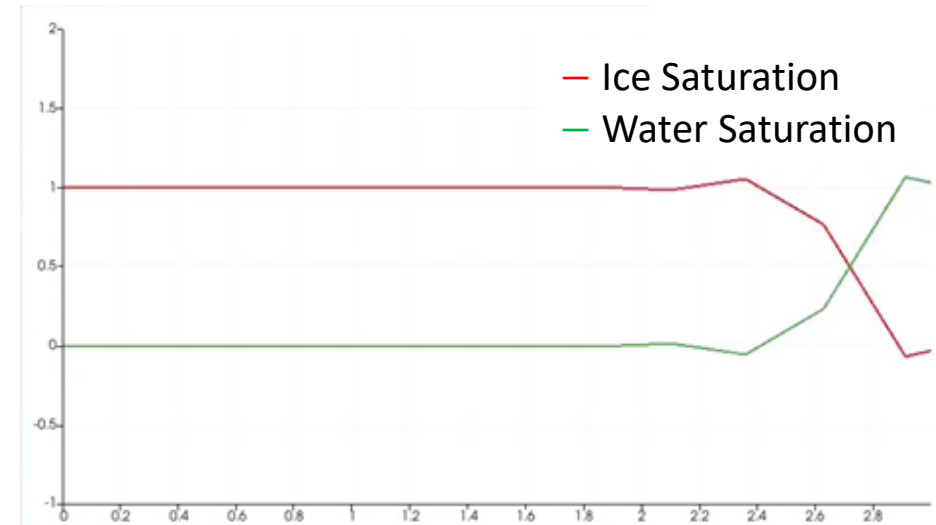




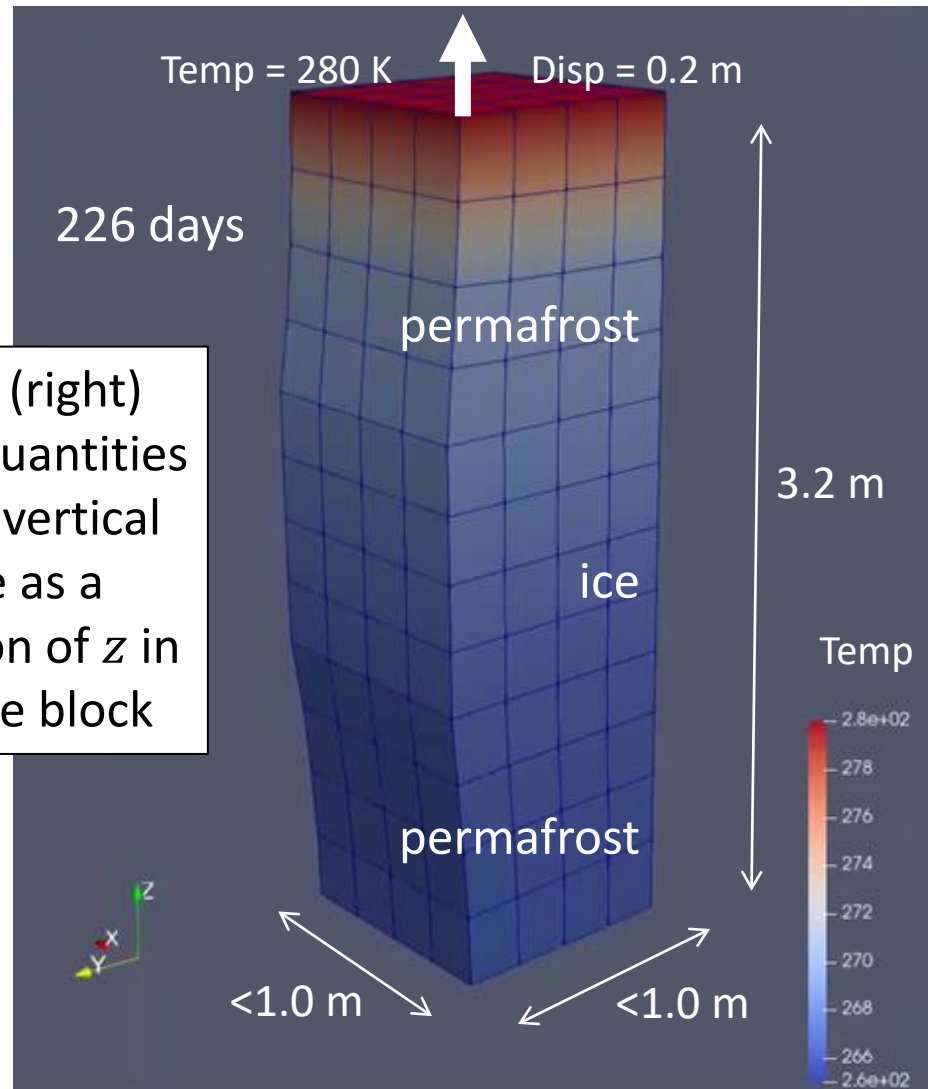
# Thermo-mechanical coupling: cuboid problem



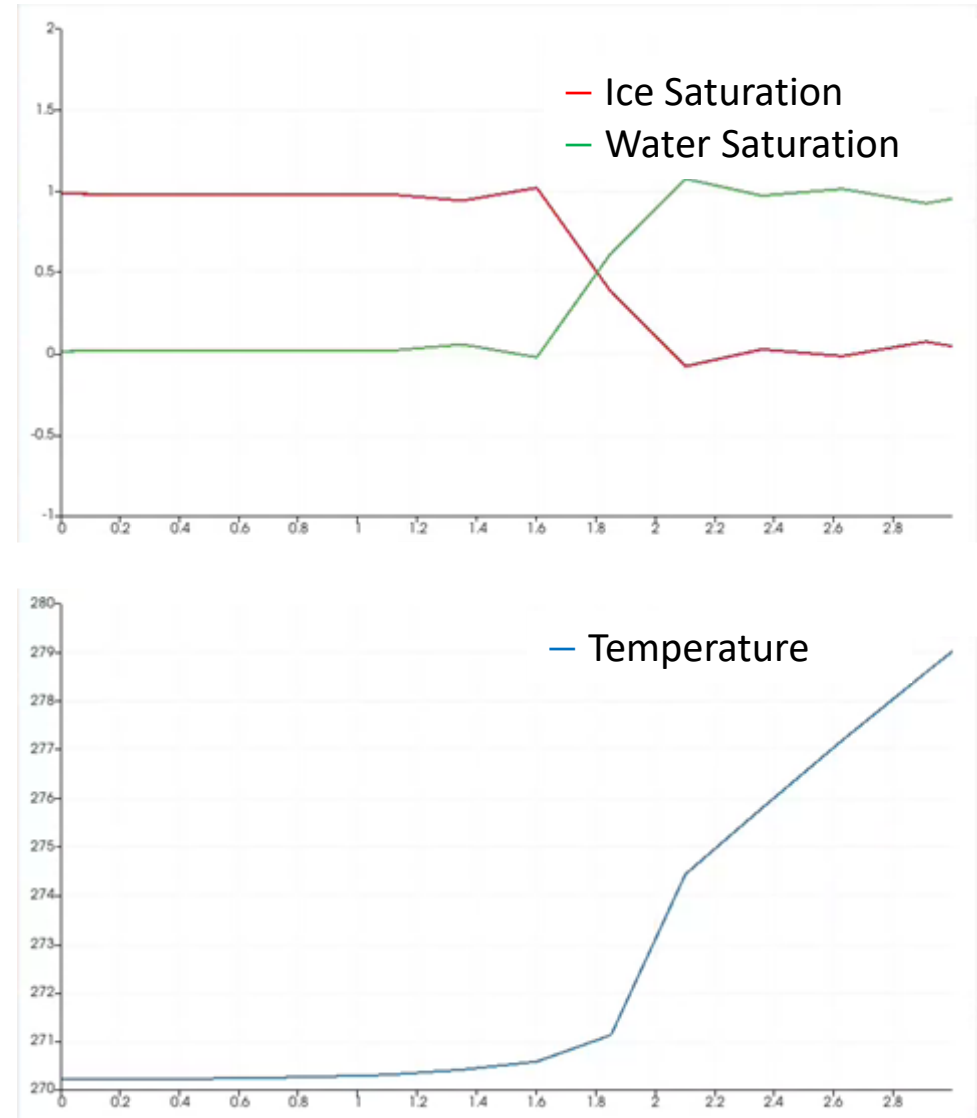
Plots (right) show quantities along vertical line as a function of  $z$  in the ice block



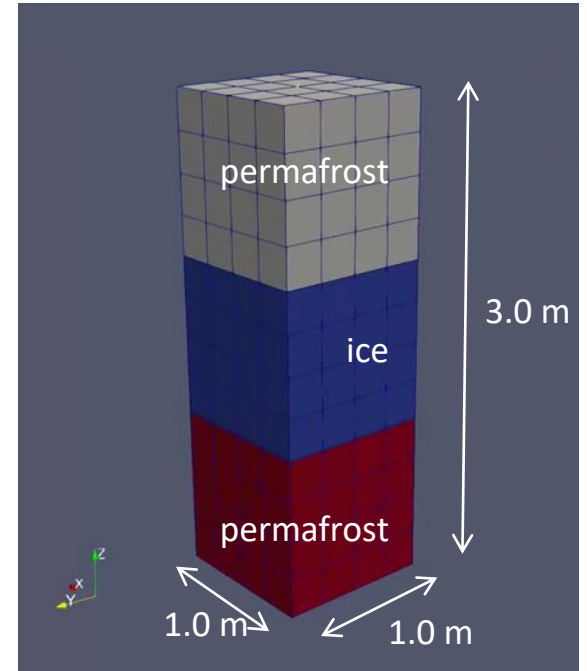
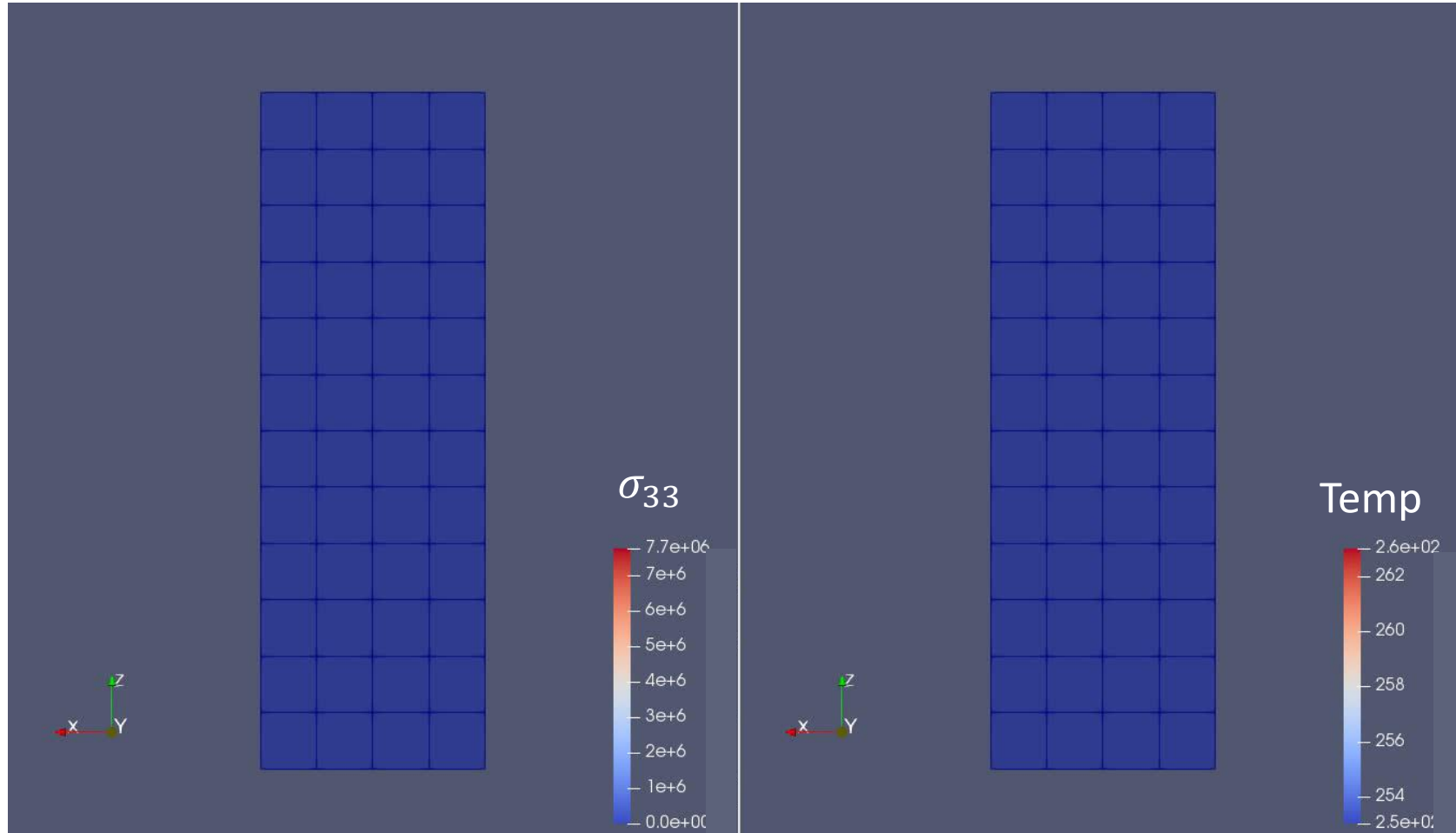
# Thermo-mechanical coupling: cuboid problem



Plots (right)  
show quantities  
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line as a  
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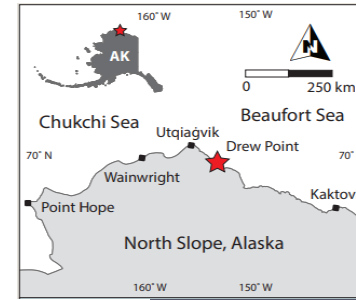
# Thermo-mechanical coupling: cuboid problem



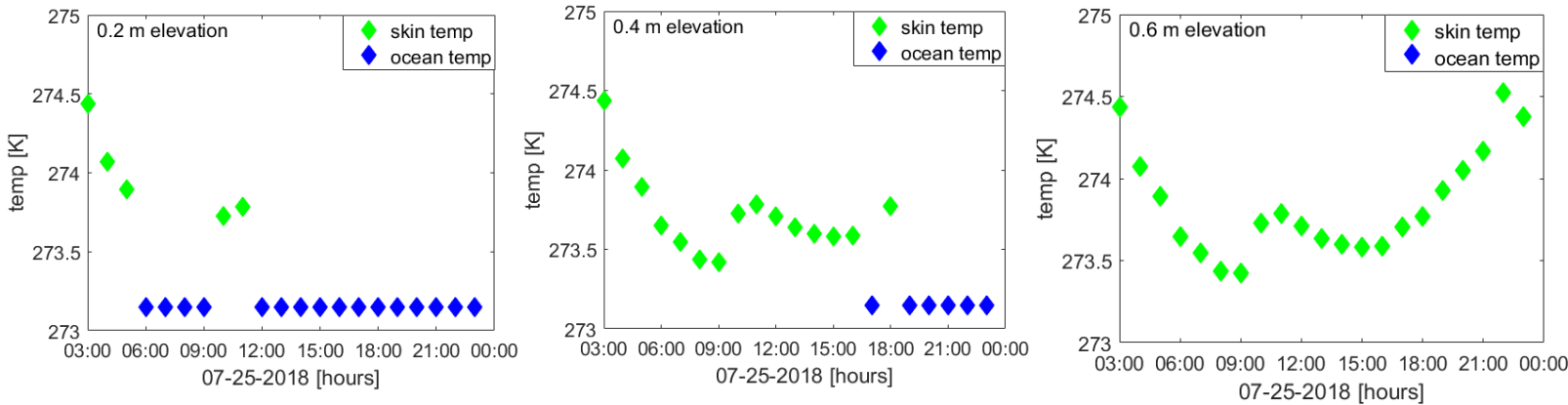
As cuboid is heated and stretched at top, heat propagates down, ***melting ice*** and causing ***failure***.



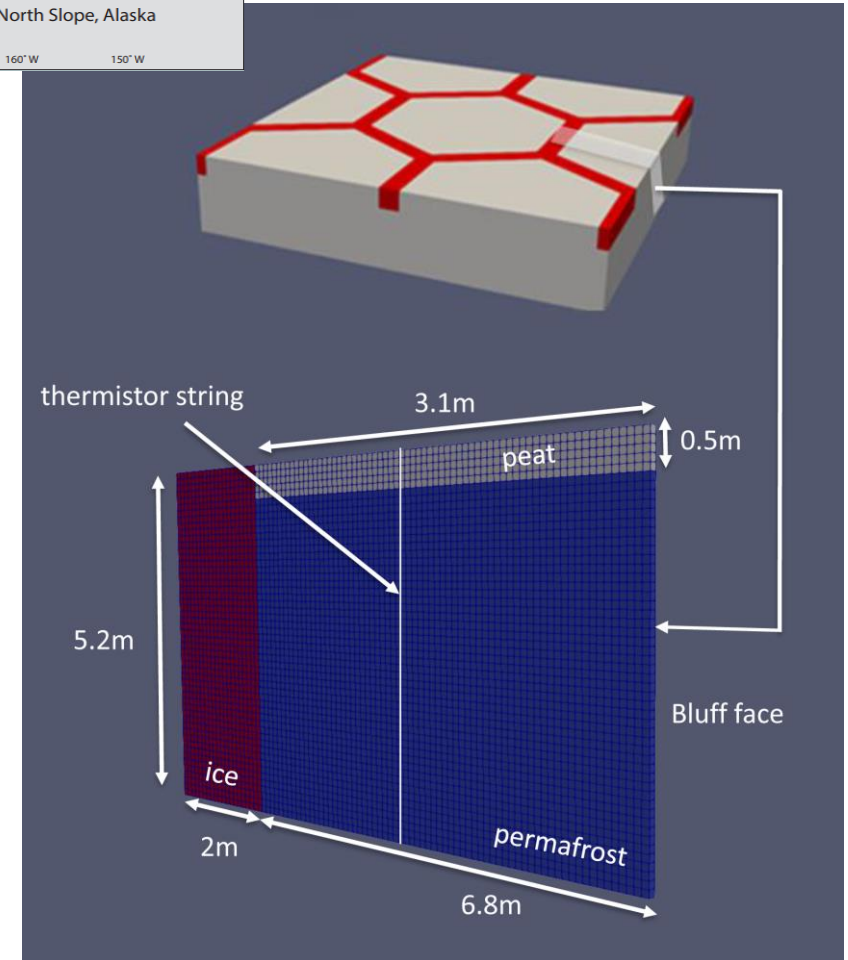
# 2.5D slice at Drew Point, Alaska\*



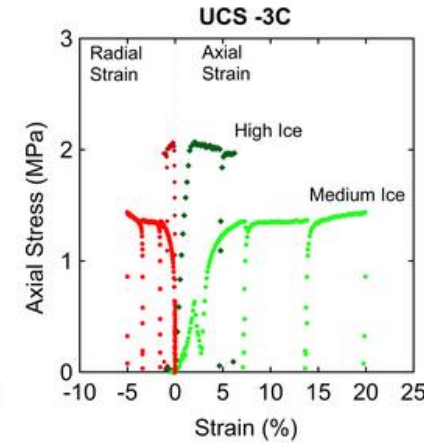
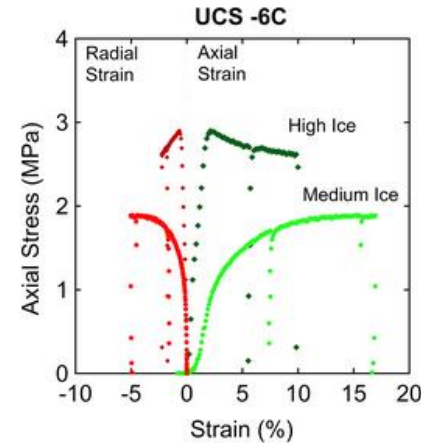
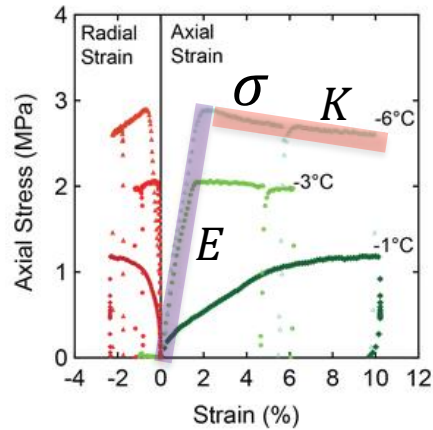
- Computational domain is **2.5D cross-section** of archetypal 3D bluff geometry discretized using a uniform hex grid.
  - Slice of permafrost is exposed to **realistic BC data** occurring at Drew Point, Alaska in July 2018 (pseudorealistic problem)



- **Initial temperature field** obtained from vertical thermistor string placed into DP1-1 ice core at Drew Point.
- **Material properties** determined from laboratory experiments on frozen soil samples from Drew Point, Alaska (next slide)
- **Implicit** Newmark for mechanical, **explicit** forward Euler for thermal (stable  $\Delta t = 1$  hour)

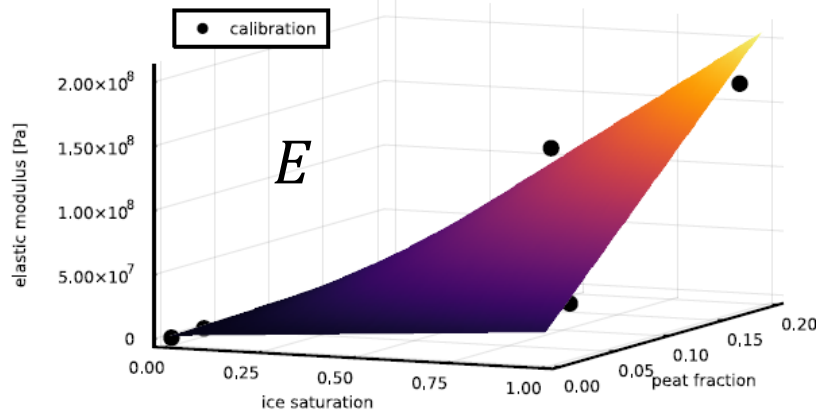


# Material Model Calibration to Experimental Data

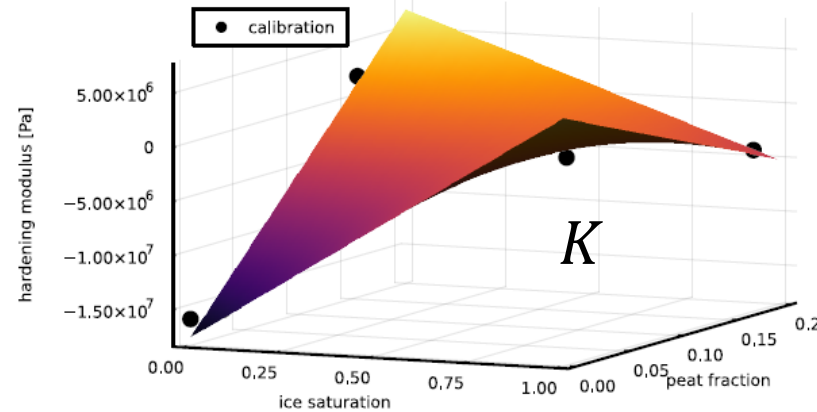


Experimental results on permafrost core samples were analyzed to create fits for parameters\*  $E$ ,  $K$ ,  $\sigma$  as a function of **ice saturation** and sediment fractions (**peat content**).

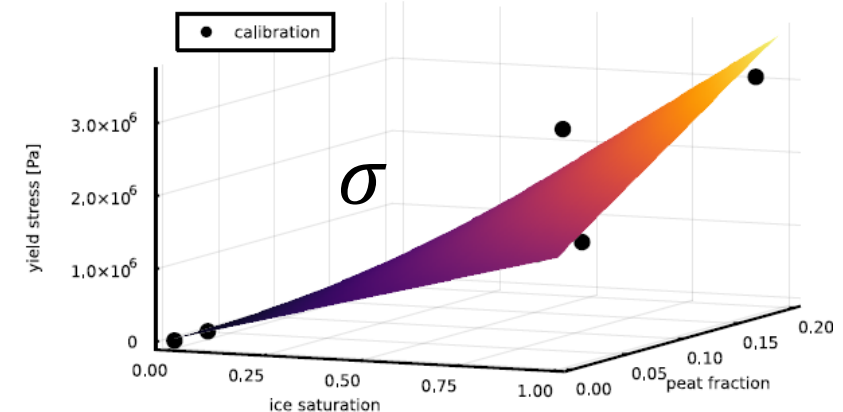
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bilinear: 0.980  
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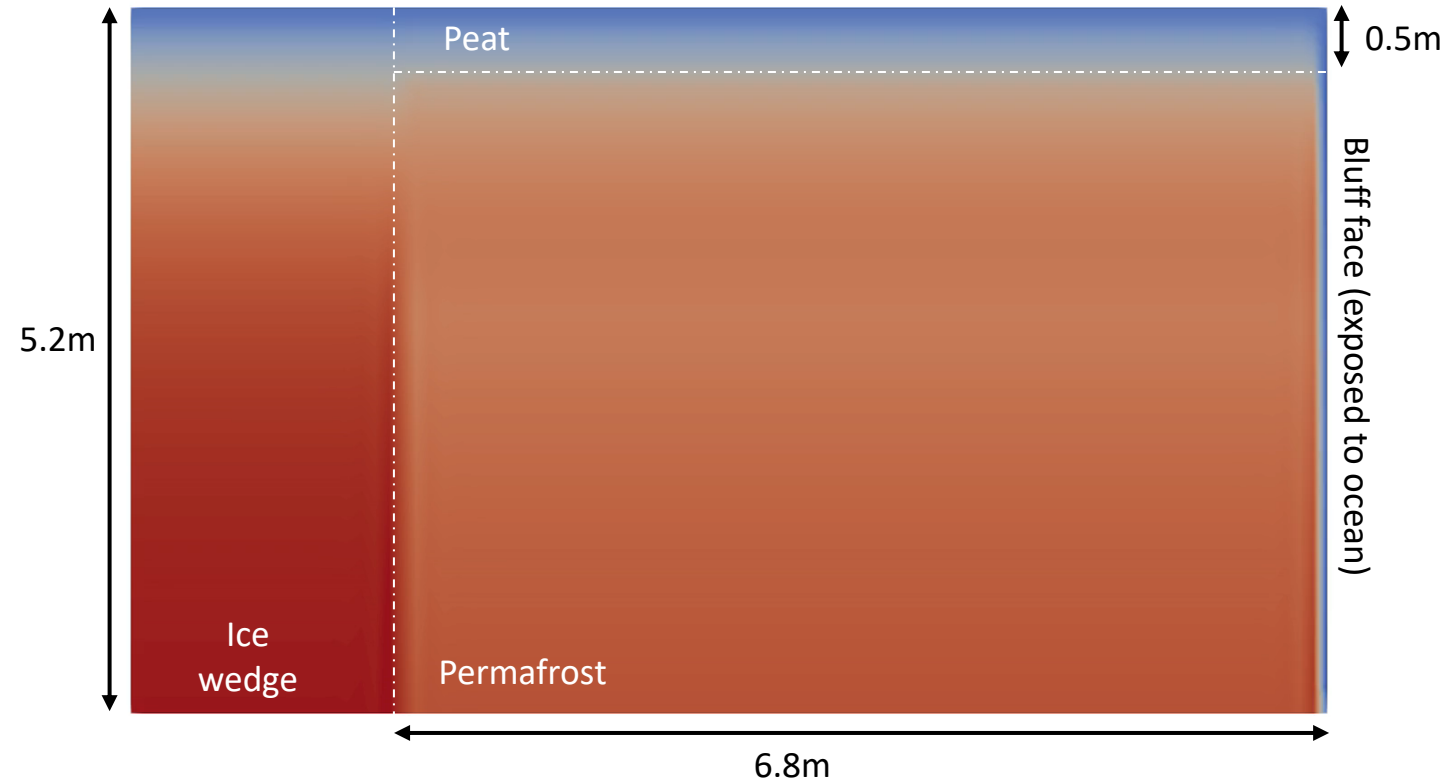


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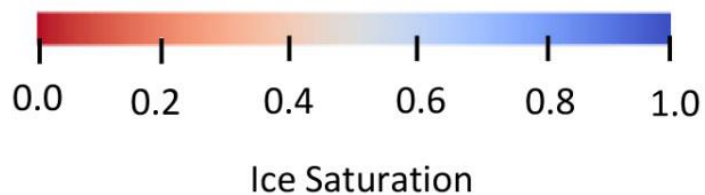


\* $E$  = elastic modulus,  $K$  = hardening modulus,  $\sigma$  = yield stress (value of stress where sample fails)

# 2.5D slice at Drew Point, Alaska\*

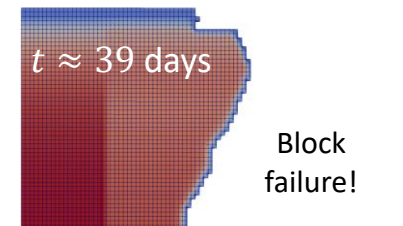
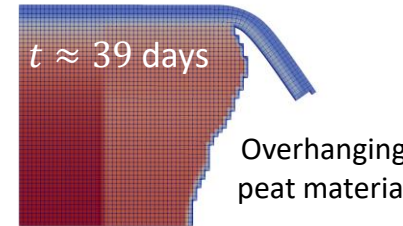
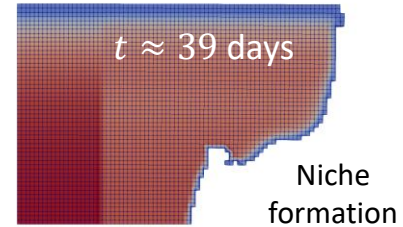
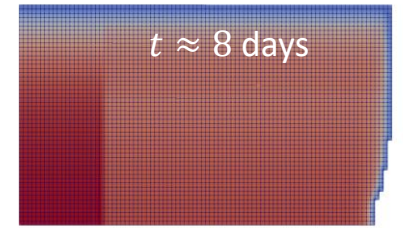


Qualitative  
comparison to  
observations



Simulation showing **niche progression** beginning at the bluff toe and **block failure/collapse event**\*

- ~3m deep *niche* forms before a *block collapse event* similar to observed collapse at Drew Point, Alaska in early fall 2018.

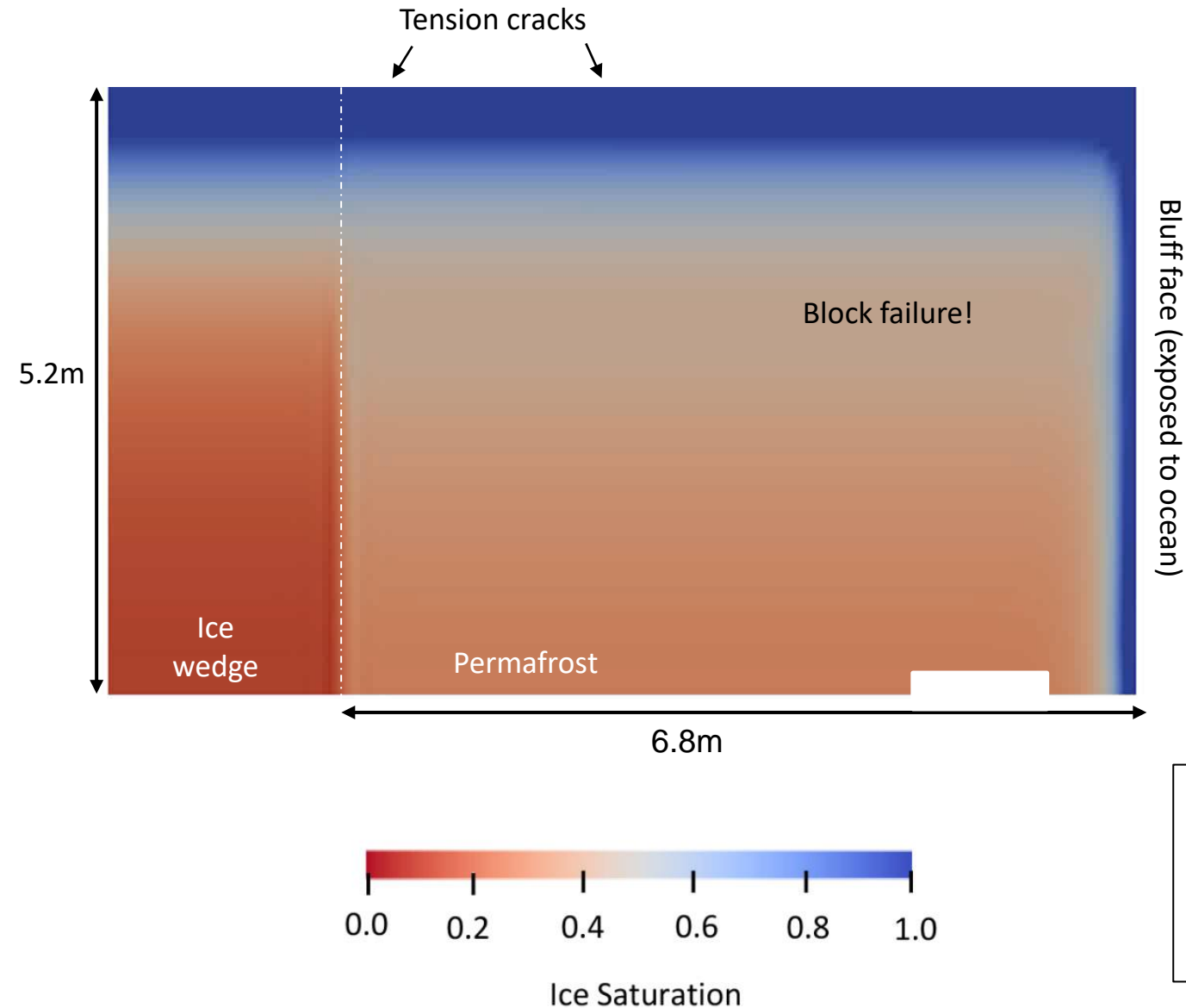


- *Thermal denudation* simultaneously with realistic *niche geometry* development.

\* For details, see: Frederick, Mota, Tezaur, Bull, *J. Comput. Appl. Math.* 2021.

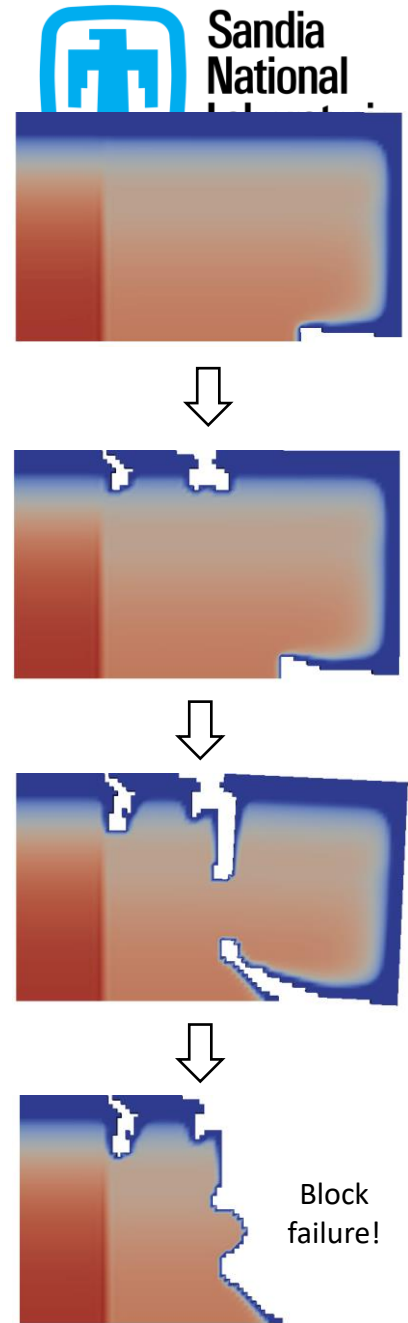


# 2.5D slice problem variant



**No-peat variant of the 2.5D slice problem with slightly different material parameters**

Once niche advanced far enough, *tension crack development* in response to niche formation is observed

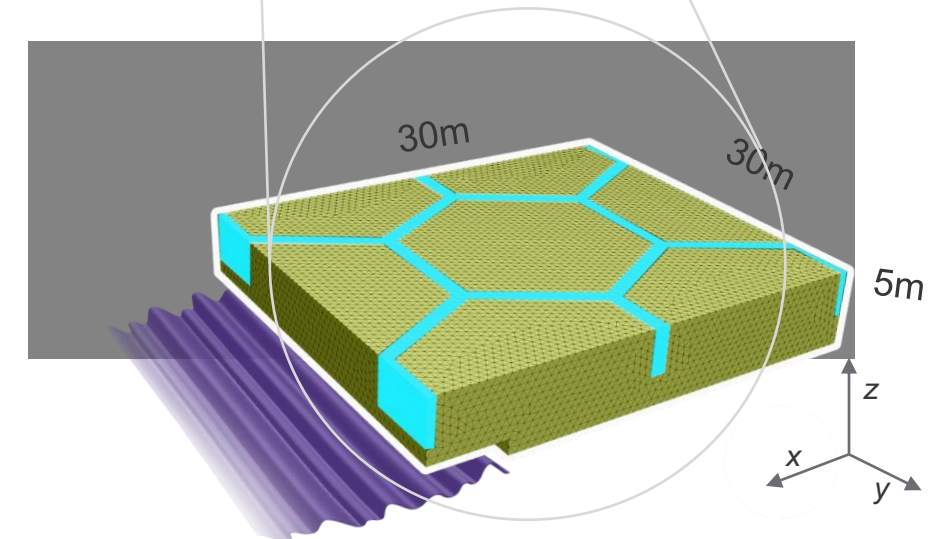
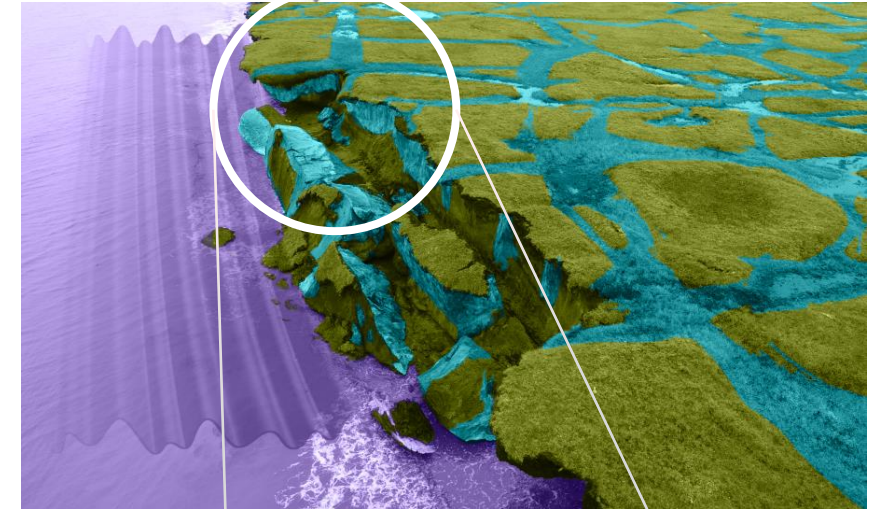


# Outline

- Motivation and background
- The Arctic Coastal Erosion (ACE) project
- Thermo-mechanical finite element model of permafrost
- Numerical results
- **Summary**
- Ongoing/future work

# Summary

- We have developed a ***thermo-mechanical*** coupled FEM model, ***ACE***, that can simulate ***transient niche development*** and ***permafrost erosion*** within Albany.
- The model was ***calibrated*** using data from a series of ***experiments*** on frozen soil samples from Drew Point, Alaska that were performed at Sandia's Geomechanics Laboratory, as well as ***observational data*** collected at the same location.
- The model incorporates ***boundary conditions*** from the ***WW3+SWAN+Delft3D*** wave models and observational data from field campaigns at Drew Point, Alaska.





# Outline

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# Ongoing/future work

## Near term:

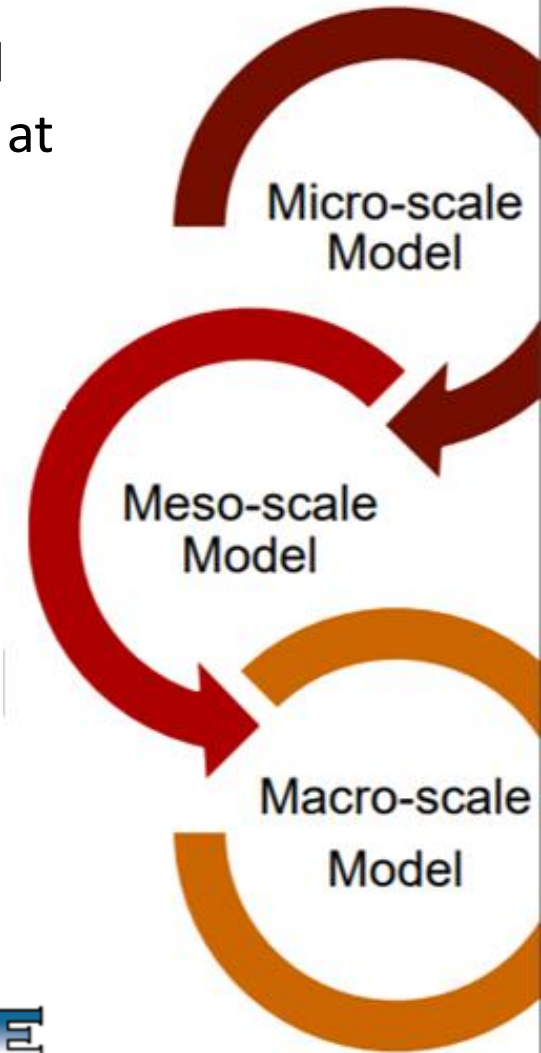
- **Quantitative validation study** in which the ACE model predictions are compared to available observational data collected during the 2018-2019 summer seasons at Drew Point, Alaska (2.5D slice + 3D).
- Testing/tuning of ACE **thermo-denudation** simulation capabilities.
- Further **calibration** and **sensitivity studies** using a range of environmental, geomorphological and numerical parameters for thermo-mechanical model.
- **Manuscript** on above work is **in preparation**.

## Longer term:

- Integrate **chemical transport** into thermal model.
- Infer **statistical meso-/macro-scale models** and relevant **physics-based parameterizations** from ACE micro-model, towards integration into ESMs.
  - ACE is member of the DOE- sponsored **InterFACE project**\* focused on coastal processes in Arctic.



INTERFACE



# References

- [1] J. Frederick, M. Thomas, D. Bull, C. Jones, J. Roberts. “The Arctic Coastal Erosion Problem”. Sandia National Laboratories Report, SAND2016-9762, 2016.
- [2] A. Gibbs, B. Richmond. “National assessment of shoreline change – historical shoreline change along the north coast of Alaska, U.S.-Canadian border to Icy Cape”. U.S. Geological Survey Open-File Report, 2015-1048, 2015.
- [3] P. Martin *et al.* “Wildlife response to environmental Arctic change: predicting future habitats of Arctic Alaska”. Report to WildREACH: Predicting Future Habitats of Arctic Alaska Workshop, Fairbanks, Alaska, 2008.
- [4] J. Brown and O. Ferrians and J. Heginbottom, E. Melnikov. “Circum-Arctic map of permafrost and ground conditions. Boulder, CO: National Snow and Ice Data Center, Digital Media, 1998.
- [5] H. Lantuit, W. Pollard. Fifty years of coastal erosion and retrogressive thaw slump activity on Herschel Island, southern Beaufort Sea, Yukon Territory, Canada. *Geomorphology*, 95, 84-102, 2008.
- [6] T. Ravens, B. Jones, J. Zhang, C. Arp, J. Schmutz. “Process-based coastal erosion modeling for Drew Point, North Slope, Alaska”. *Journal of Waterway, Port, Coastal, and Ocean Engineering*, 138, 2, 122-130, 2012.
- [7] C. Koven, J. Riley, A. Stern. “Analysis of permafrost thermal dynamics and response to climate change in the CMPI5 Earth system models”. *J Climate*, 26, 1877-2900, 2009.
- [8] M. Thomas, A. Mota, B. Jones, C. Choens, J. Frederick, D. Bull. “Bluff geometry and material properties influence stress rates relevant to coastal permafrost block failure”. *Frontiers in Earth Science* 8, 2020.
- [9] J. Frederick, A. Mota, D. Bull, I. Tezaur. “Thermo-chemo-mechanical coupling for Arctic Coastal Erosion”, *J. Comput. Appl. Math.* 397 113533, 2021.
- [10] D. Bull, C. Flanary, C. Jones, J. Frederick, A. Mota, I. Tezaur, J. Kasper, E. Brown, B. Jones, M. Jones, E. Bristol, C. Choens, C. Connolly, J. McClelland. “Arctic Coastal Erosion: Modeling and Experimentation”. Sandia National Laboratories report, SAND2020-10223, 2020.



Sandia  
National  
Laboratories



The University of Texas at Austin  
Marine Science Institute

# Acknowledgements

## *Research Team*

**SNL:** D. Bull (PI), J. Frederick, A. Mota, C. Choens, I. Tezaur, L. Criscenti

**USGS:** M. Thomas, B. Jones

**UAF:** J. Kasper, E. Brown

**Integral Consulting:** C. Jones, C. Flanary

**U Texas:** J. McClelland, E. Bristol, C. Connolly





# Start of Backup Slides

# Potential impacts

- **3D model** capable of predicting erosion from the material's constitutive relationships capturing all types of **deformation (block & denudation)** leading to:
  - **Data-driven** understanding of the characteristics that cause erosion
  - A tool to guide **military** and **civil infrastructure** investments
  - An improved understanding of **coastal food web impacts** and **carbon-climate feedbacks**
- **Redistributed eroded sediment** in the environment enables:
  - Prediction of deposition locations
  - Estimates of fluxes (biogeochemical, toxins, etc.)

Approach for moving from mechanistic micro-scale to stochastic meso-scale model sets stage for **integration** into **global climate models** built upon parametric analyses of input variables



# Oceanography in Mechanistic Model

WW3

Development of wave field in the Arctic to develop nearshore BCs

- surface winds
- ice cover
- temperature (surface and ocean)
- solar radiation
- persistent currents

SWAN

Wave set-up conditions 2-way coupled with circulation

- high resolution near shore environment
- capture set-up (storm surge and runup)
- wave energy inclusive of induced current effects

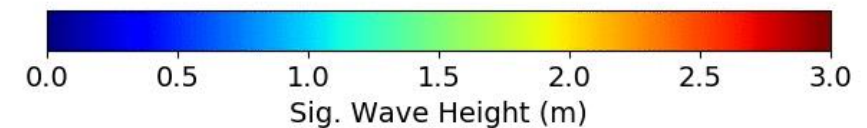
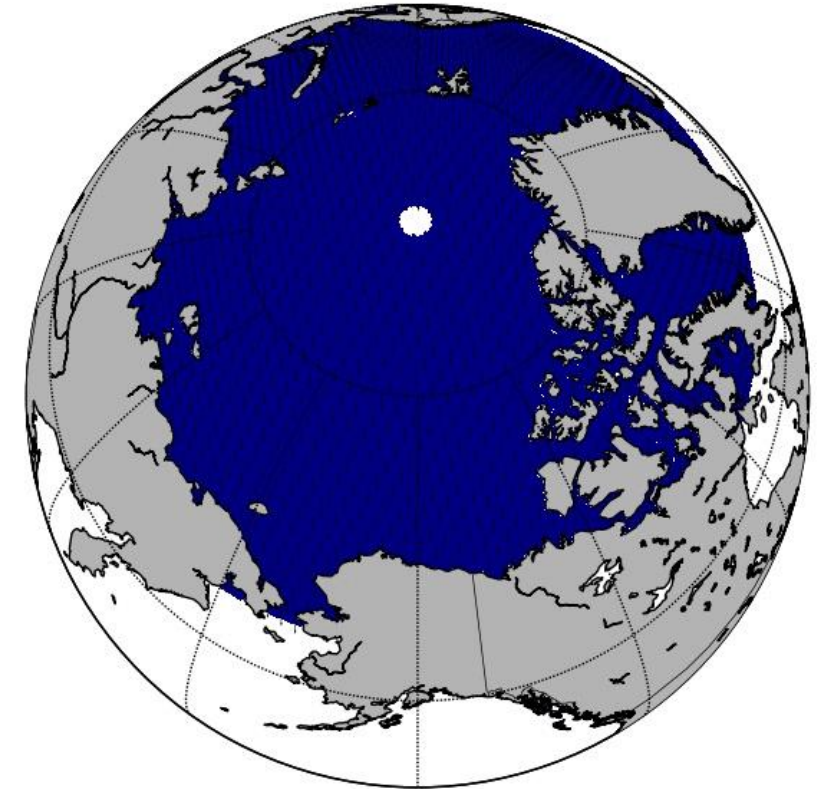
Delft3D

Circulation and thermodynamic mixing 2-way coupled with waves

- ability to model mixing of temperature and salinity clines
- capture induced currents in nearshore

## ■ Potential Key Advances

- Inclusion of ice coverage for fetch limited wave growth
- Knowledge of wave energy along broad coastline
- Set-up determination inclusive of bathymetry and wave energy
- Ability to accurately predict temperature at bluff face through mixing of clines in the ocean



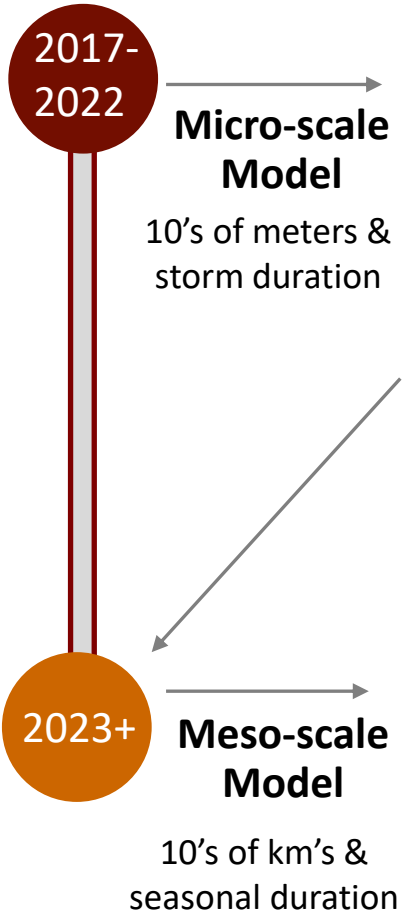
WW3 polar stereographic model initially developed by NRL (Erick Rogers) and NOAA (Arun Chawla)

# Proposed solution

INTERFACE

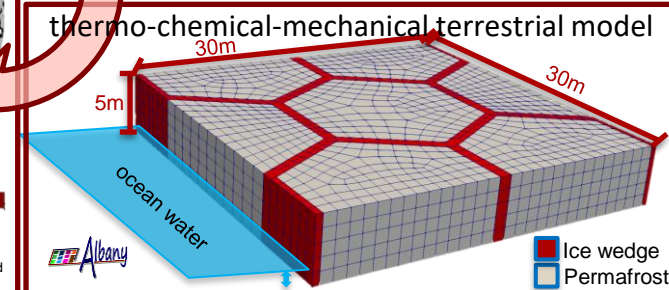
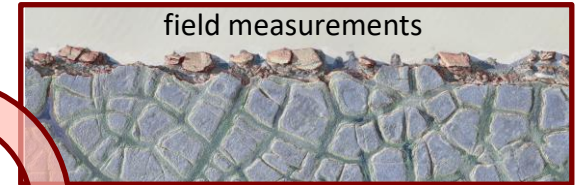
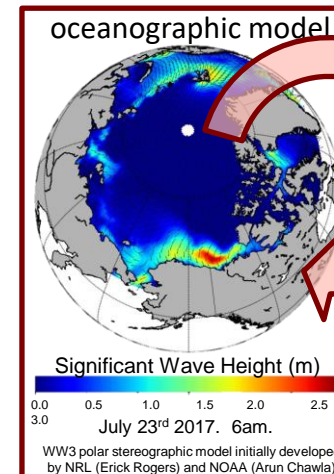


Goal of the **Arctic Coastal Erosion (ACE)** project is to deliver a **field-validated predictive model of thermo-abrasive erosion** for the **permafrost Arctic coastline**

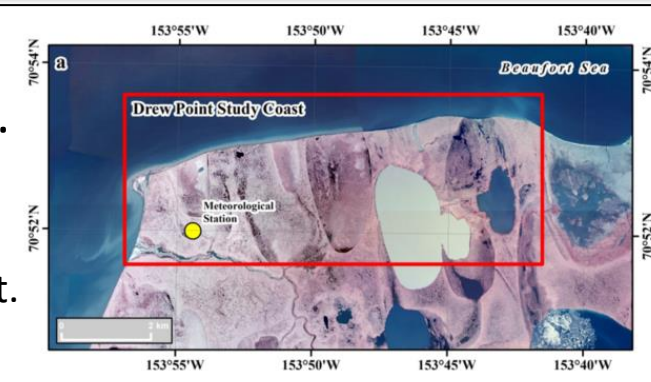


- **Multi-physics finite element model** of an archetype of the coastline coupled with high-fidelity model of storm intensities
  - Input variables define geomorphology & geophysics
  - Plastic deformation model of material (J2 class)
  - Geomechanical testing to determine coupled thermal-mechanical strength characteristics
  - Time-varying ocean BCs (water level, temp, salinity)
  - Eroded sediment and biogeochemical flux tracking

**This talk**

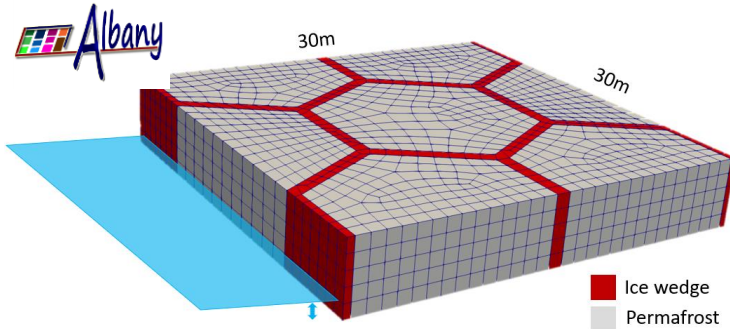


- A “catalog” of micro-scale models that represent the statistical distributions of input variables along a ~10km stretch of coastline.
  - Probability distribution functions of geomorphology and geophysics used to weight erosion output
    - Will validate approach with decade long annual measurements at Drew Point.
  - Evaluating ocean “exposure metrics” to represent time-varying ocean





# Multi-scale approach



## Micro-Scale Model

10's of meters & storm duration

One set of input variables defining the geomorphology and geophysics of the terrestrial model.



## Meso-Scale Model

10's of kilometers & monthly duration

A number of micro-scale models that represent the stochastic distributions of input variables along a confined coastline.



## Macro-Scale Model

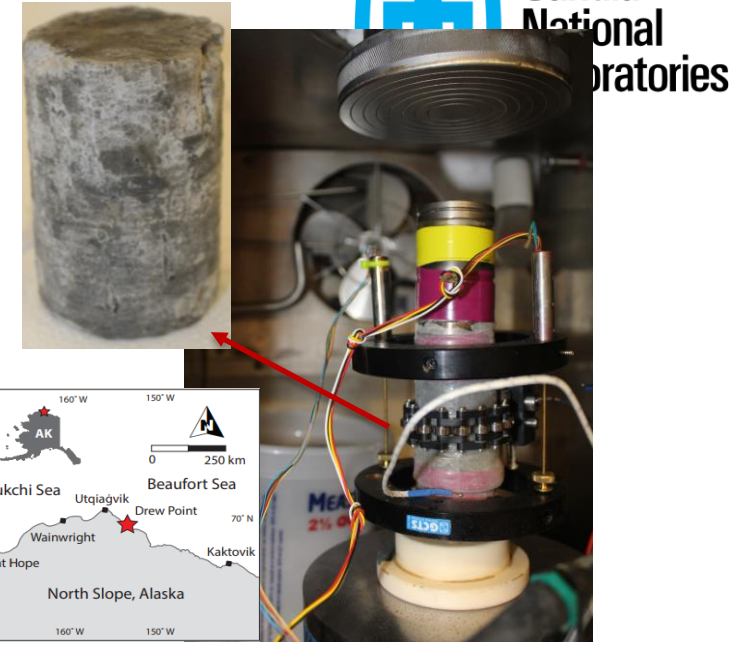
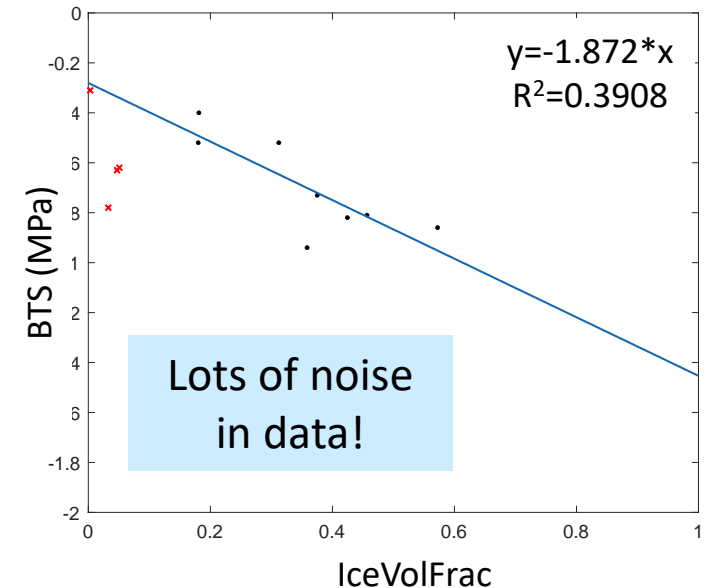
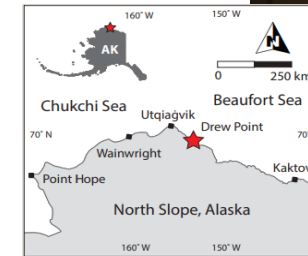
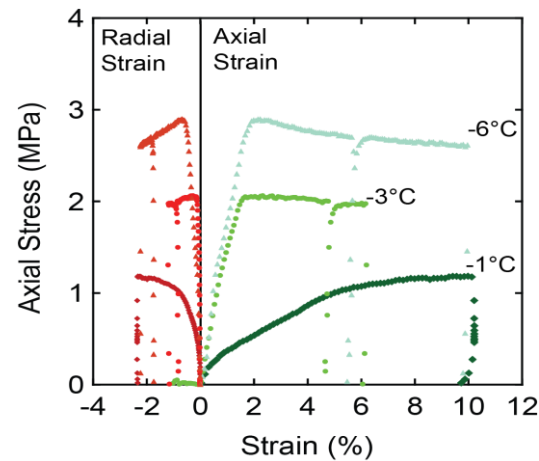
100's of kilometers & annual (+) durations

A number of meso-scale models that represent the diversity of coastline types (delta, exposed bluffs, lagoons, etc.) along the AK coastline.

- Working towards a series of fully coupled studies to determine **terrestrial model sensitivities** to:
  - Height of water on bluff face
  - Exposure time of bluff face to water
  - Temperature of water
  - Salinity of water

# Parameters & inputs

- Permafrost properties depend on **ice content**, **unfrozen water content** and **frost susceptibility**.
- Few mathematical relationships exist** that describe changes in tensile strength, shear strength and cohesion of ice/permafrost with changes in temperature.
- Series of **experiments** (UCS<sup>1</sup>, BTS<sup>2</sup>, DT<sup>3</sup>) on frozen soil samples at different temps (-6C, -3C, -1C) and ice content from Drew Point, AK were performed at SNL's Geomechanics Laboratory to estimate:
  - Strength: 1-3 MPa
  - Young's modulus: 0.01-0.16 GPa
  - Poisson's ratio: 0.1-0.35
  - Porosity values: 40-95%



<sup>1</sup> Unconfined compressive test. <sup>2</sup> Brazilian tensile tests. <sup>3</sup> Direct tensile tests.