Update on Sandia *Albany/FELIX* First-Order Stokes (FELIX-FO) Solver

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FY15 Progress Highlights



Sandia's Role in the PISCEES Project: to develop and support a robust and scalable unstructured grid finite element land ice solver based on the "First-Order" (FO) Stokes approximation→Albany/FELIX*



- Albany/FELIX is verified, scalable, robust.
- Albany/FELIX is portable to next-generation machines via Kokkos.
- We have written/are writing several *journal articles* on *Albany/FELIX*.
- We have looked at the effect of *earth curvature* using stereographic projection.
- Albany/FELIX is coupled to MPAS and CISM; mostly coupled to ACME (via MPAS).
 →We have developed a stable semi-implicit coupling method for thickness-FO Stokes (implemented in MPAS-Albany).
- Codes are *running* on *Hopper, Edison, Titan, Mira*.

Additional Progress & Future Work (other talks):

- Deterministic inversion (talk by M. Perego).
- Uncertainty quantification: Bayesian calibration, forward propagation of uncertainty (talk by J. Jakeman).

*FELIX = Finite Elements for Land Ice eXperiments





Verification of Albany/FELIX



Stage 2: code-to-code comparisons on canonical ice sheet benchmarks (*Albany/FELIX* – left; *LifeV* – right).



Stage 3: full 3D mesh convergence study on Greenland w.r.t. reference solution.



Stage 4: reasonable solutions for large-scale realistic GIS & AIS problems (*Albany/FELIX* – left; reference solution – right)



Scalability via Algebraic Multi-Grid Preconditioning with Semi-Coarsening

We achieve *excellent scalability* (even with ice shelves!) via new algebraic multi-grid (AMG) preconditioner with semi-coarsening.

FY15 progress:

rilinos

- Demonstration of good *scalability/ performance* of AMG solver on Antarctica: 30x faster than ILU solver!
- 3 *papers* featuring new AMG preconditioner.
- New AMG preconditioner has been implemented in *MueLu* (T. Wiesner).



Planned work:

- Speeding up *MueLu* AMG preconditioner (*MueLu* solver slower than *ML*).
- Performance studies (optimizations?) on new architectures (template on 3rd dimension?) and/or with dynamical cores.

I. Tezaur, M. Perego, A. Salinger, R. Tuminaro, and S. Price, GMD, 2015.

I. Tezaur, R. Tuminaro, M. Perego, A. Salinger, S. Price, Procedia CS, 2015.

R. Tuminaro, M. Perego, I. Tezaur, A. Salinger, S. Price, SISC, 2015.



Improved Linear Solver Performance through Removal of Hinged Peninsulas

Islands/hinged peninsulas lead to **solver failures**



FY15 Progress:

- An algorithm has been developed to detect/remove *hinged peninsulas* & islands based on coloring & repeated use of connected component algorithms.
- Solves ~2x faster with hinges removed.

Planned work:

• Integration of algorithm for hinge removal into dynamical cores?





Resolu-	ILU –	ILU – no	ML –	ML – no
tion	hinges	hinges	hinges	hinges
8km/5	878 sec,	693 sec,	254 sec,	220 sec,
layers	84 iter/solve	71 iter/solve	11 iter/solve	9 iter/solve
4km/10	1953 sec,	1969 sec,	285 sec,	245 sec,
layers	160 iter/solve	160 iter/solve	13 iter/solve	12 iter/solve
2km/20	10942 sec,	5576 sec,	482 sec,	294 sec,
layers	710 iter/solve	426 iter/solve	24 iter/solve	15 iter/solve
1km/40		15716 sec,	668 sec,	378 sec,
layers		881 iter/solve	34 iter/solve	20 iter/solve

Greenland Problem



Performance Portability via Kokkos

Performance portability achieved through *Kokkos* programming model/*Trilinos* library.



Kokkos abstractions allow device-specific memory layout and parallel kernel launch \rightarrow same code can run on diverse devises with different memory models (multi-core, many-core, GPUs)

FY15 Progress:

- *Finite element assembly (FEA)* in *Albany* has been converted to *Kokkos*.
- Demonstrated performance portability with *CUDA/OpenMP* on Sandia clusters; with *OpenMP* on *Titan*.

with I. Demeshko

Planned work:

- Journal *article* in preparation (I. Demeshko).
- Running on **GPUs** of *Titan*: awaiting gcc-4.7.2 compiler support from Cray.

I. Demeshko, A. Salinger, W. Spotz, I. Tezaur, in prep for J. HPC Appl., 2015.





MPI-Only ——MPI+2 OpenMP threads per 1 MPI — MPI+4 OpenMP threads per 1 MPI Laboratories

FO Stokes Equations on Spherical Grids

Current ice sheet models are derived using *planar geometries* (reasonable, especially for Greenland)... The effect of Earth's *curvature* is largely unknown and may be nontrivial for Antarctica!

FY15 Progress:

- We have derived a FO Stokes model on sphere using *stereographic projection* and implemented it in *Albany/FELIX*.
- **Preliminary results:** curvature has some effect on Antarctica simulations.

Planned work:

- Verification.
- Try transient simulations with dycores on curved geometry and investigate effect on quantities of interest (e.g., sea-level rise).
- Journal article.



Surface velocity magnitude [m/yr], ice sheet thickness not at scale (100 X)

CISM-Albany Update

CISM-Albany dycore: Albany/FELIX has been coupled to CISM for transient simulations.

FY15 Progress:

- Floating ice & kinematic Dirichlet BCs have been implemented in CISM-Albany for realistic problems.
- CISM-Albany was used for 50 year UQ forward propagation study (see J. Jakeman's talk)

→ demonstrated **robustness** of CISM-Albany: all 66 forward UQ runs with highly perturbed β converged on Hopper out-of-the-box! with S. Price,

J. Jakeman

Planned work:

- Fine-resolution GIS validation test case towards science runs using CISM-Albany (with S. Price).
- Science paper using CISM-Albany (with S. Price).
- Improved **UQ demonstration** (with J. Jakeman).





MPAS-Albany Update: Semi-Implicit Thickness-FO Stokes Coupling

FY15 Progress:

- Improved *interface* between *MPAS* and *Albany*.
- Improved BCs (*nonlinear basal BCs*/ grounding line* parametrization**).
- Developed and implemented *semi-implicit*** thickness-FO Stokes* discretization in MPAS-Albany: can use larger time steps (advective vs. diffusive CFL). H at t=4 yrs

$$-\nabla \cdot \left(\mu \tilde{\mathbf{D}}\left(\mathbf{u}\right)\right) = -\rho g \nabla \left(b + \mathbf{H}\right) \text{ in } \Omega_{H^{n}} \qquad \frac{\mathbf{H} - H^{n}}{\Delta t} + \nabla \cdot \left(\bar{\mathbf{u}} H^{n}\right) = \theta^{n}$$

Planned work:

- Continue investigating robustness/efficiency/ accuracy of the semi-implicit method and grounding line parametrization.
- Coupled science simulations under ACME.



** Using high-order quadrature.

*** *u* computed in *Albany/FELIX* with implicit solve; *MPAS* uses velocity to march in time explicitly.

w/ M. Perego, S. Price, M. Hoffman





Dome test case: sequential approach unstable with dt = 1yr; semi-implicit approach stable with dt = 5yrs.



New GL parametrization

new

3km var.

old

Summary of Ongoing/Planned Work for FY16

<u>Albany/FELIX:</u>

- *MueLu* speed-ups; optimizations for new architectures?
- Continue porting to new architecture machines (e.g., GPUs on *Titan*), and performance-portability paper.
- Testing under LIVV.
- Finish optimization capabilities (see next talk by M. Perego).
- Coupling with hydrology model (with L. Bertagna; see next talk by M. Perego).
- Improved Bayesian calibration UQ demonstration (see J. Jakeman's talk).

CISM-Albany:

- Greenland validation test case.
- Science runs using CISM-Albany, and science paper
- Grounding line parametrization.
- Improved forward propagation UQ demonstration (see J. Jakeman's talk).
- Testing under LIVV.
- Linear solver performance studies/optimizations? Integration of hinge removal algorithm?

MPAS-Albany:

- Coupled science simulations under ACME.
- Continue investigating robustness/efficiency/accuracy of the semi-implicit method and grounding line parametrization.
- Testing under LIVV.
- Linear solver performance studies/optimizations? Integration of hinge removal algorithm?