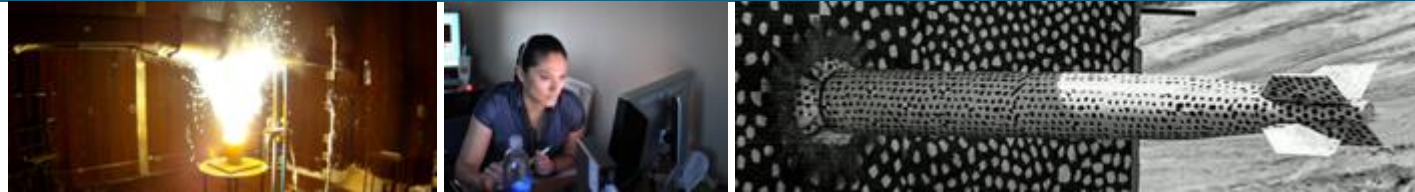


# Model Reduction at Sandia National Laboratories



*PRESENTED BY*

**Irina Tezaur**

Principal Member of Technical Staff  
Quantitative Modeling & Analysis Department  
Sandia National Laboratories, Livermore, CA

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# About Sandia National Labs (SNL)

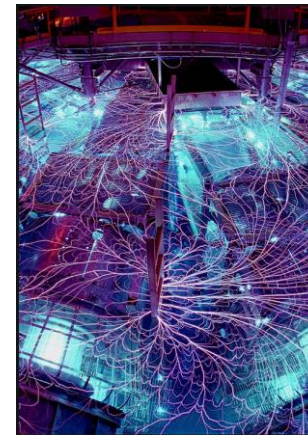


Sandia's **primary mission** is ensuring the U.S. nuclear arsenal is safe, secure and reliable, and can fully support our nation's deterrence policy.

We have **programs** in the following areas:

- Nuclear Deterrence
- Defense Nuclear Nonproliferation
- National Security
- Global Security
- Energy & Climate
- Advanced Science & Technology

- Sandia is a **multidisciplinary** national lab and Federally Funded Research & Development Center (FFRDC).
- Contractor for the U.S. DOE's National Nuclear Security Administration (NNSA).
- **Two main sites:** Albuquerque, NM and Livermore, CA (above).



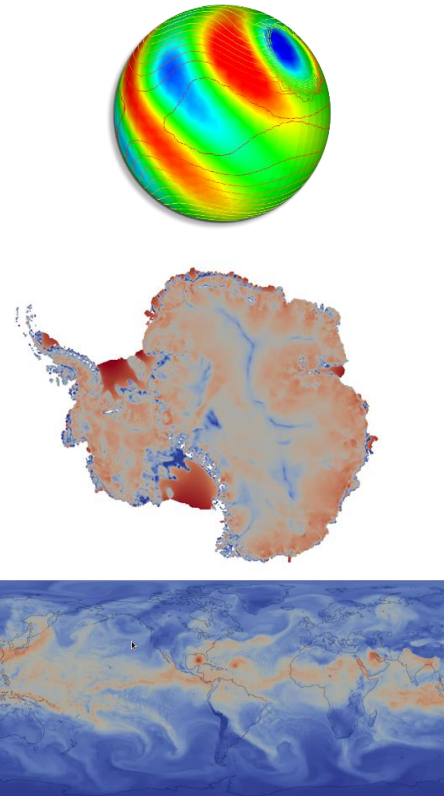
# SNL Applications Requiring ROMs



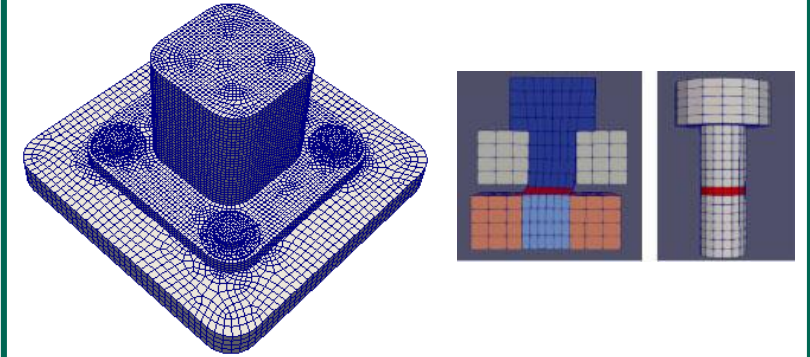
## Re-Entry/Captive-Carry Problems



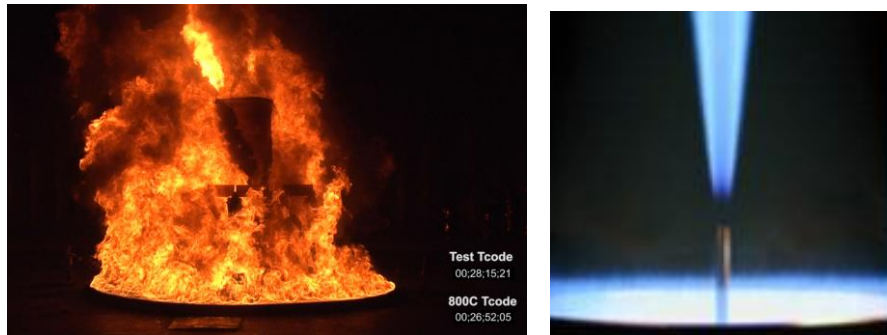
## Climate



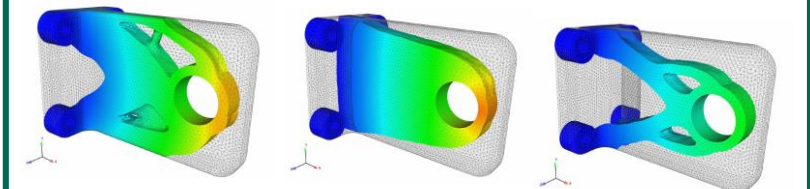
## Fastener Modeling



## Heat Transfer/Turbulent Combustion



## Topology Optimization/ Additive Manufacturing



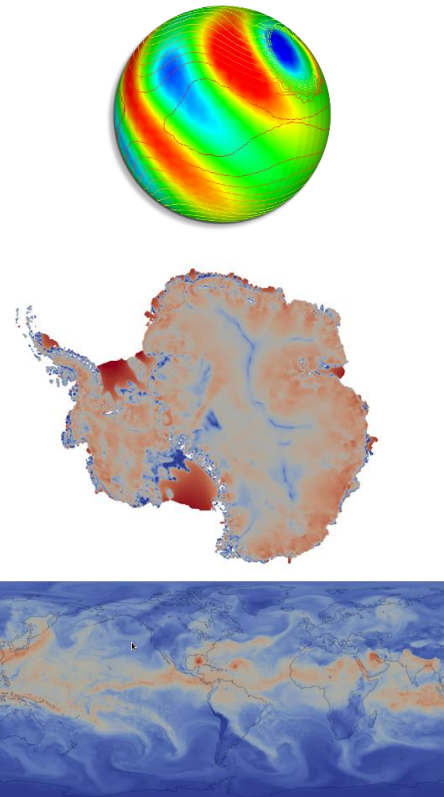




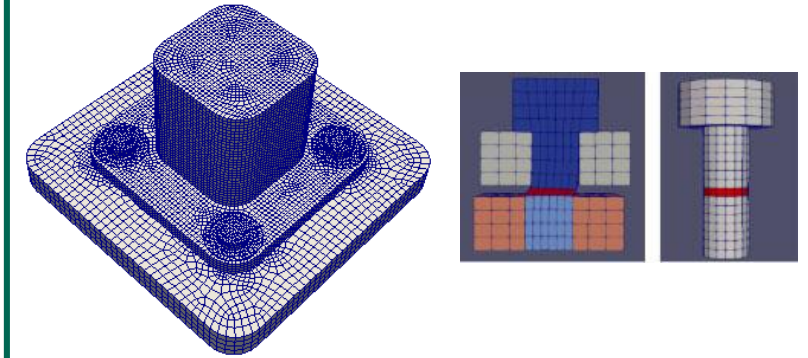
## Re-Entry/Captive-Carry Problems



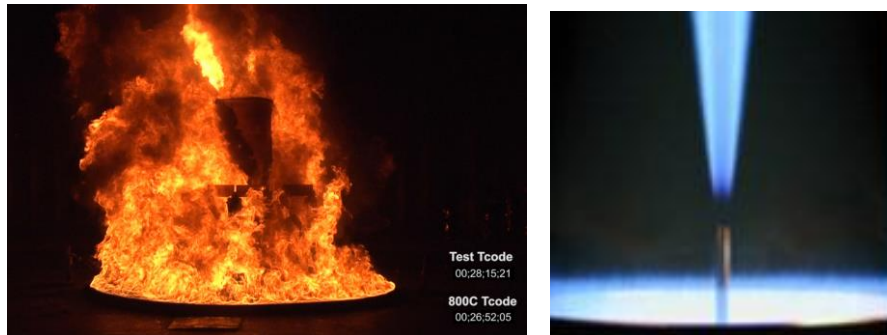
## Climate



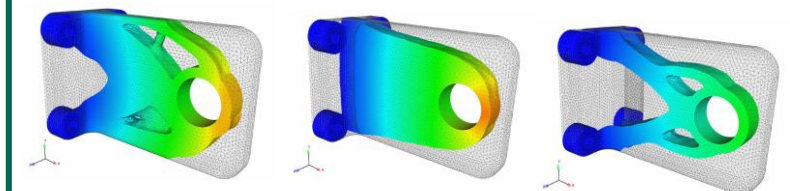
## Fastener Modeling



## Heat Transfer/Turbulent Combustion



## Topology Optimization/ Additive Manufacturing



*These are not toy problems that are prevalent in the ROM literature!*

# Sandia's ROM Development/Deployment Strategy

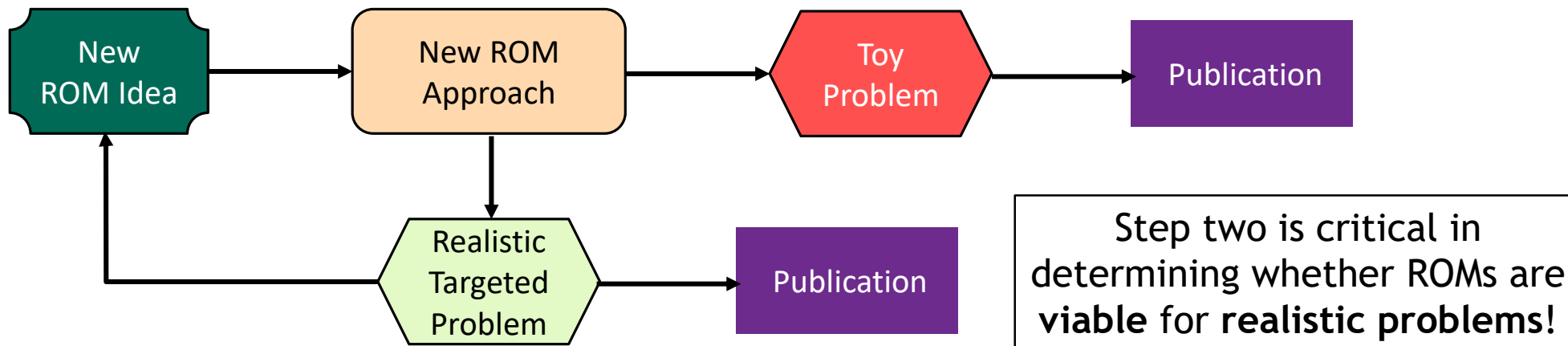


Targeted problems present **unique numerical challenges** that you don't run into with toy problems!

(e.g., strong nonlinearities, huge differences scales, turbulence/chaos, multiphysics, multi-D shocks, etc.)

## Approach:

- **Step 1:** New ideas/methods are first verified/prototyped on **simple benchmarks** (e.g., 1D Burgers).



- **Step 2:** Apply methods to targeted **realistic problems** - presents new challenges, requiring new R&D

To facilitate step two, we have been developing an **open-source tool** called



An **open-source\*** **non-intrusive** computational framework aimed at providing performant projection-based ROMs for generic application codes

### Main idea:

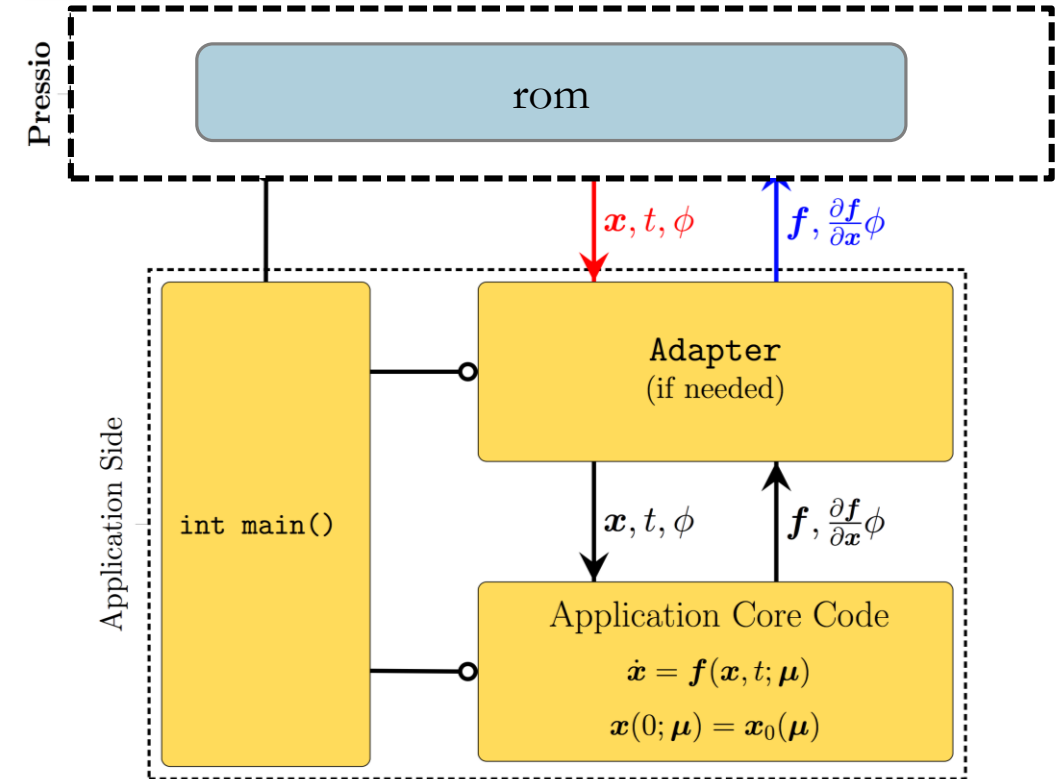
- Separate the “application” and the ROM
- ROM methods are contained in the Pressio framework
- Pressio “plugs in” to an application code

### Salient features:

- Header-only C++ library
- Supports HPC performance portability via Kokkos
- Supports Python API
- Supports Galerkin, LSPG, and WLS ROMs (with hyper-reduction)
- Pressio’s API requires application to expose two main routines: residual and applyJacobian

### Advantages:

- Pressio can be used to easily add ROM capabilities to any generic HPC code!
- Methods added to Pressio are at the fingertips of users of HPC codes hooked up to Pressio!



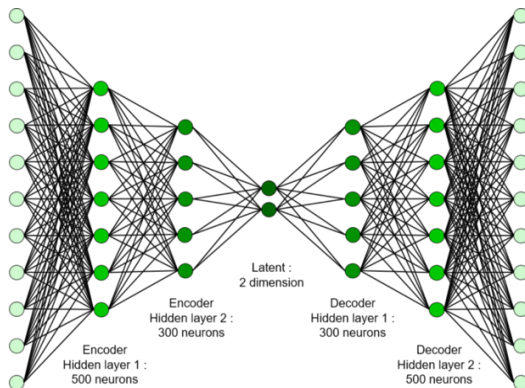
\* <https://github.com/Pressio>

### Research Gaps:

- ROMs with quantified/guaranteed accuracy/robustness in the **predictive regime**.
- ROMs for practical nonlinear multiscale problems exhibiting **shocks, chaos**, slow decay of Kolmogorov  $n$ -width (**convection-dominated**).
- Relative dearth of ROMs for **compressible flows**.

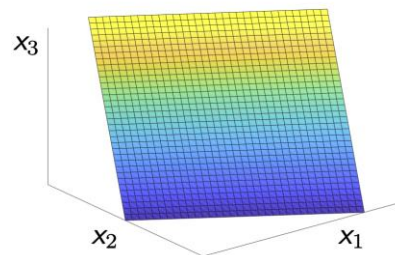
### Current Research Directions at Sandia:

- Windowed least-squares (WLS) ROMs [Parish, Carlberg, 2020; Shimizu, Parish, 2021].
- ROM preconditioners to improve ROM predictability [Fike, Lindsay, Tezaur, Carlberg, 2021].
- Domain decomposed ROMs for networks [Hoang, Choi, Carlberg, 2020].
- Nonlinear manifold ROMs using autoencoders [Lee, Carlberg, 2020].



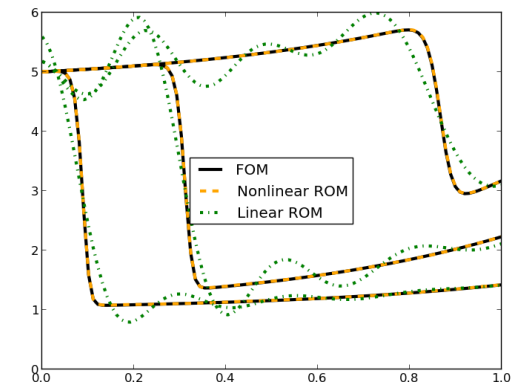
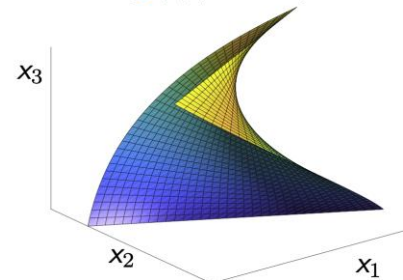
#### Linear trial subspace

$$\text{range}(\Phi) := \{\Phi \hat{\mathbf{x}} \mid \hat{\mathbf{x}} \in \mathbb{R}^p\}$$



#### Nonlinear trial manifold

$$\mathcal{S} := \{\mathbf{g}(\hat{\mathbf{x}}) \mid \hat{\mathbf{x}} \in \mathbb{R}^p\}$$





*There should be benchmarks that go beyond simple 1D/2D toy problems.*

- How to “release”/formulate these is a challenge, as high-fidelity code is likely required.
- Software like Pressio can help bridge the gap between ROM and application developers and give ROM developers access to more realistic problems to test their methods.
- Publishing problem formulations/datasets may help researchers set up more realistic tests in their own codes (“bake-of” problems or “model intercomparison” problems).

*It's important to evaluate ROMs in the predictive regime.*

- Many researchers/authors never make it past reproductive regime.

*In evaluating ROMs, one needs to carefully design relevant QOIs/metrics of success.*

- Very application specific - e.g., for compressible flow ROM, analysts care about pressure PSD, not entire solution field.
- While ROMs cannot be expected to reproduce the entire solution field to a specified tolerance for an arbitrarily complex predictive problem, there *is* some hope of a ROM reproducing some relevant QOI.

Applying ROM to more **realistic** problems using appropriate **QOIs/metrics** will tell us how **viable** ROMs can be beyond the space of “toy” problems.



# Research Team



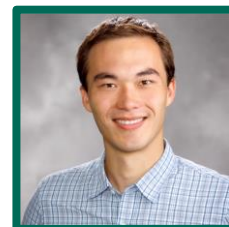
Marco Arienti



Patrick Blonigan



Victor Brunini



David Ching



Jeff Fike



Chi Hoang



Micah Howard



Kookjin Lee



Samuel Majors



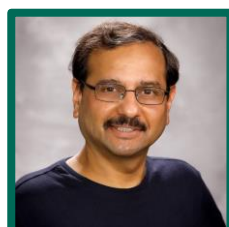
Eric Parish



Flint Pierce



Kevin Potter



Jaideep Ray



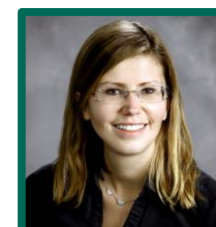
Francesco Rizzi



Yuki Shimizu



John Tencer



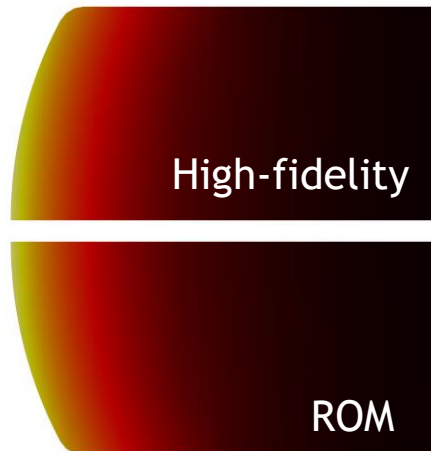
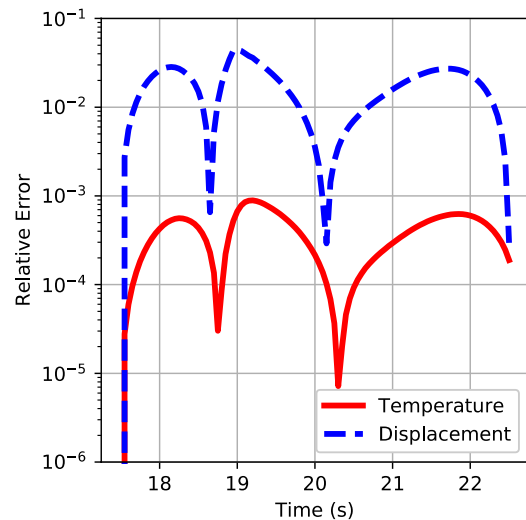
Irina Tezaur



Karen Willcox

### ROM accelerates **ablation** simulation with SPARC compressible flow solver

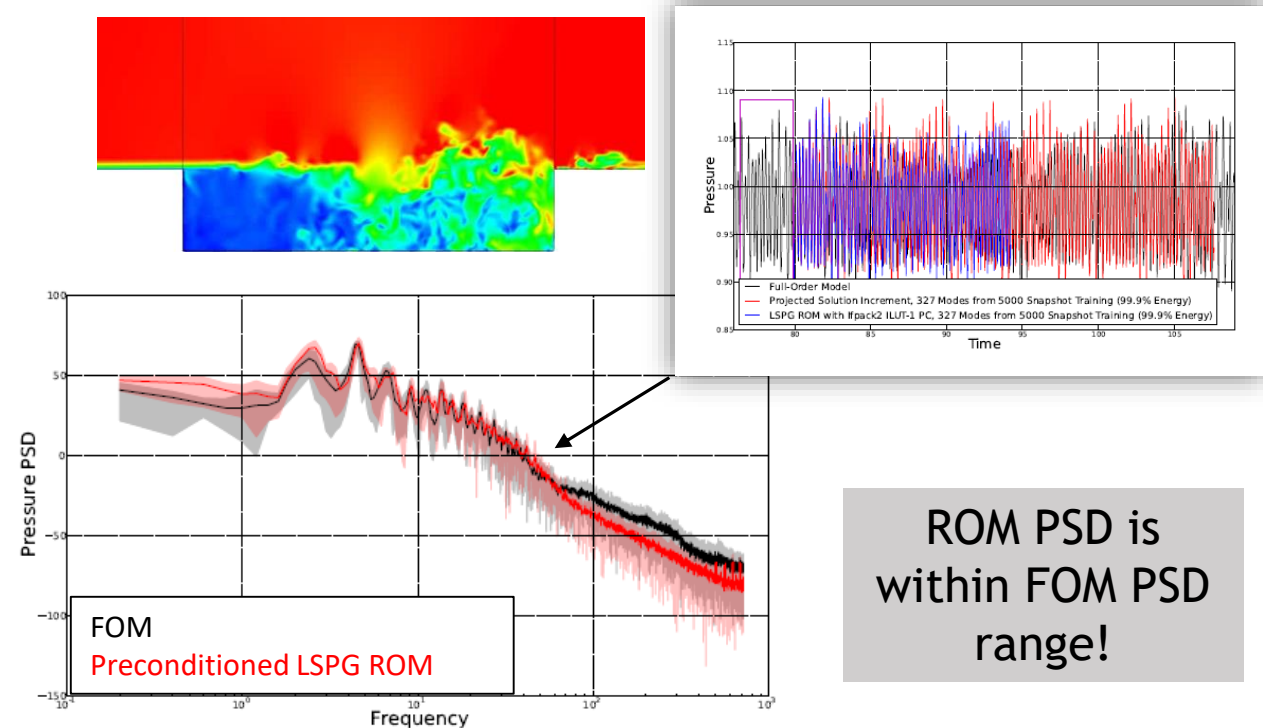
- First applications of ROMs to ablation
- Large differences in scales (7 orders of magnitude)
- Iso-q with prescribed axisymmetric heat- and mass-transfer boundary conditions



~17x savings in core-hours  
 <0.1% error in temp, <4% error in disp

### Time-predictive preconditioned **captive-carry** ROM in SPARC demonstrated to have sufficiently accurate pressure PSD

- Laminar compressible cavity problem ( $Ma = 0.6$ ,  $Re = 3000$ ).
- Primarily interested in prediction in time.

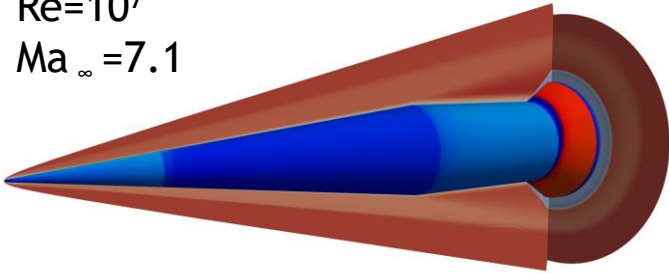


ROM PSD is within FOM PSD range!

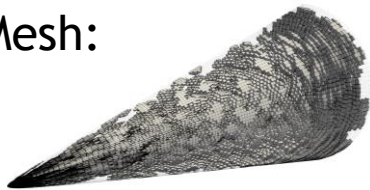
# Recent ROM Successes at SNL (cont'd)

ROM accelerates **hypersonics** simulation (HiFIRE-1 experiment) using in-house compressible flow solver (SPARC)

$Re=10^7$   
 $Ma_\infty=7.1$



- Prediction across param space ( $Ma$ ,  $\rho$ )
- POD-LSPG + Sample Mesh:



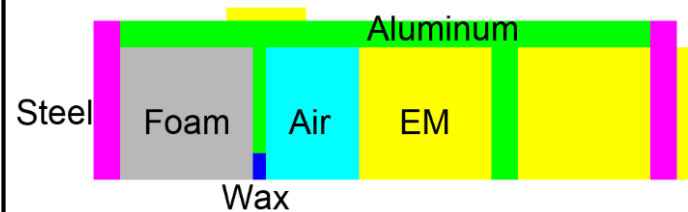
~300-1000x savings in core-hrs  
<1% error in density, momentum, energy  
~1-2% error in integrated wall heat flux

[Blonigan, Carlberg, Rizzi, Howard, Fike, 2020]

## ROM accelerates transient conduction/thermochemistry in Aria

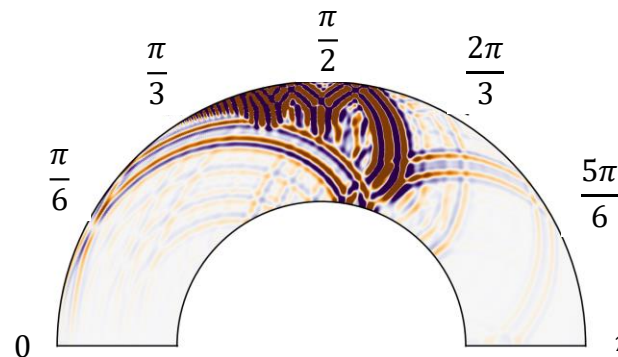
- Transient thermochemistry test
  - Foam decomposition
  - Heat conduction
  - Exothermic chemical reactions

~9000x savings in core-hrs  
<1°C error in temp.



## ROM accelerates seismic wave propagation

- Synthetic seismogram data
- One shot UQ: simultaneous simulation of many trajectories



~950x savings in wall-time  
<1% error

